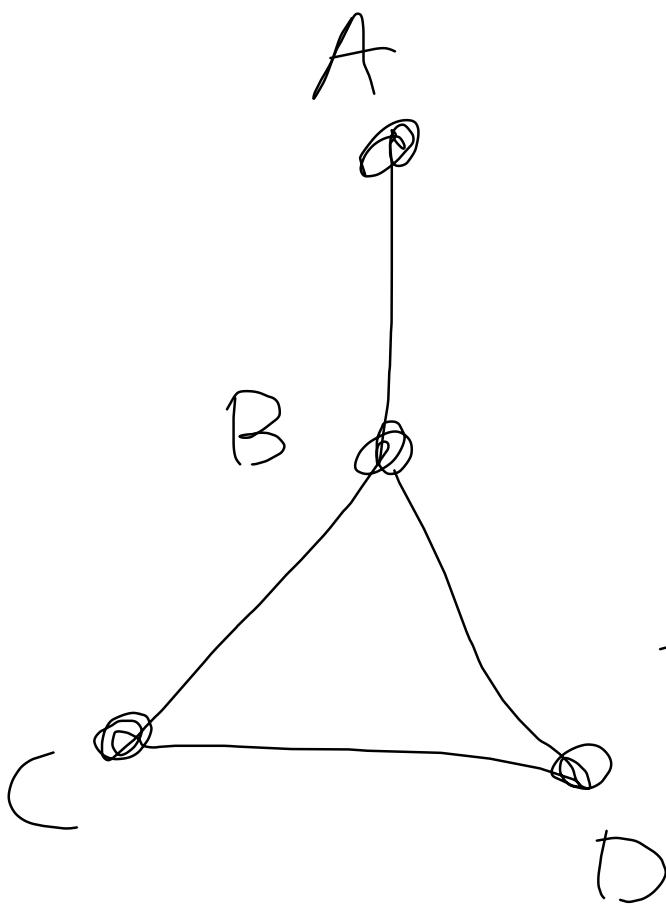


0001



$A \xrightarrow{\quad} A$
 $B \xrightarrow{\quad} B$
 $C \xrightarrow{\quad} C$
 $D \xrightarrow{\quad} D$

$A \xrightarrow{\quad} A$
 $B \xrightarrow{\quad} B$
 $C \xrightarrow{\quad} D$
 $D \xrightarrow{\quad} C$

v_1

\vdots

v_n

$$S \leq d(v_1) \leq \Delta$$

$$S \leq d(v_2) \leq \Delta$$

...

$$S \leq d(v_n) \leq \Delta$$

$$\overline{vS} \leq \sum_{i=1}^n d(v_i) \leq n\Delta$$

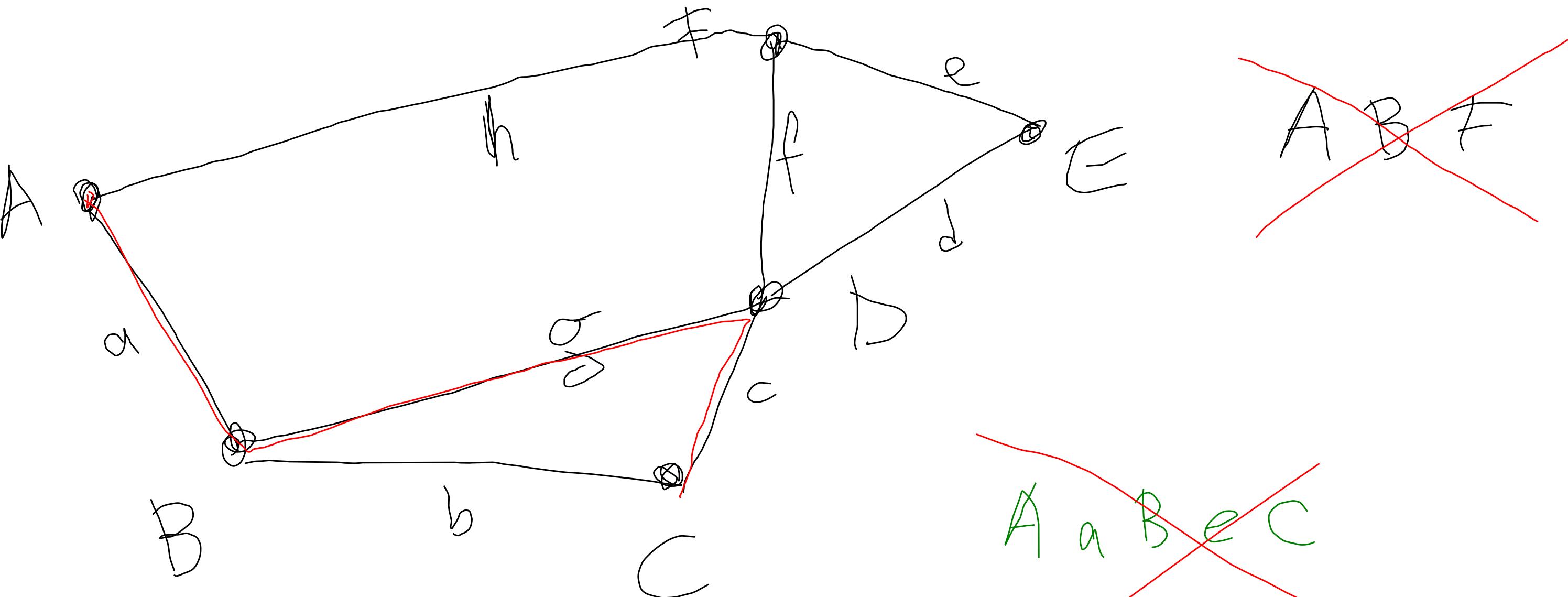
||

$$2\varepsilon$$

$$\frac{1}{2}$$

$$\overline{vS} \leq 2\varepsilon \leq 2\Delta$$

$$S \leq \frac{2\varepsilon}{\Delta} \leq \Delta$$



A a B g D < C

A B D C

A a B b C

A a B e C

DEF - A relation R on a set X is said to be an equivalence relation if these three conditions hold.

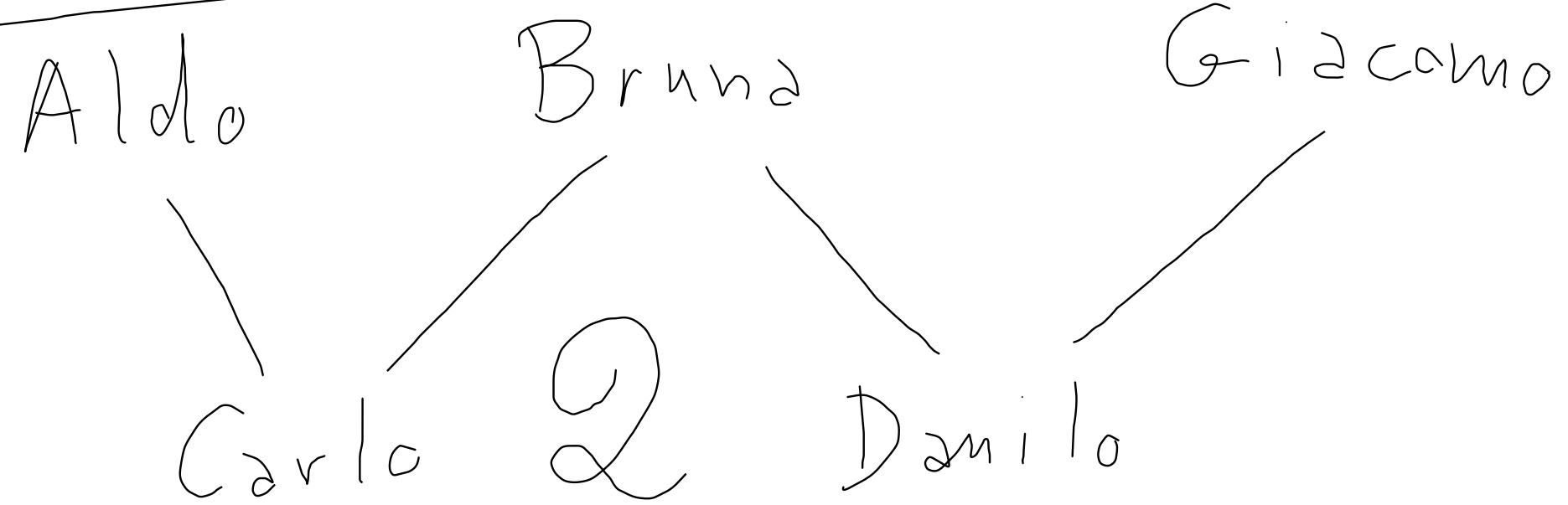
1) $\forall x \in X \quad x R x$ (reflexivity)

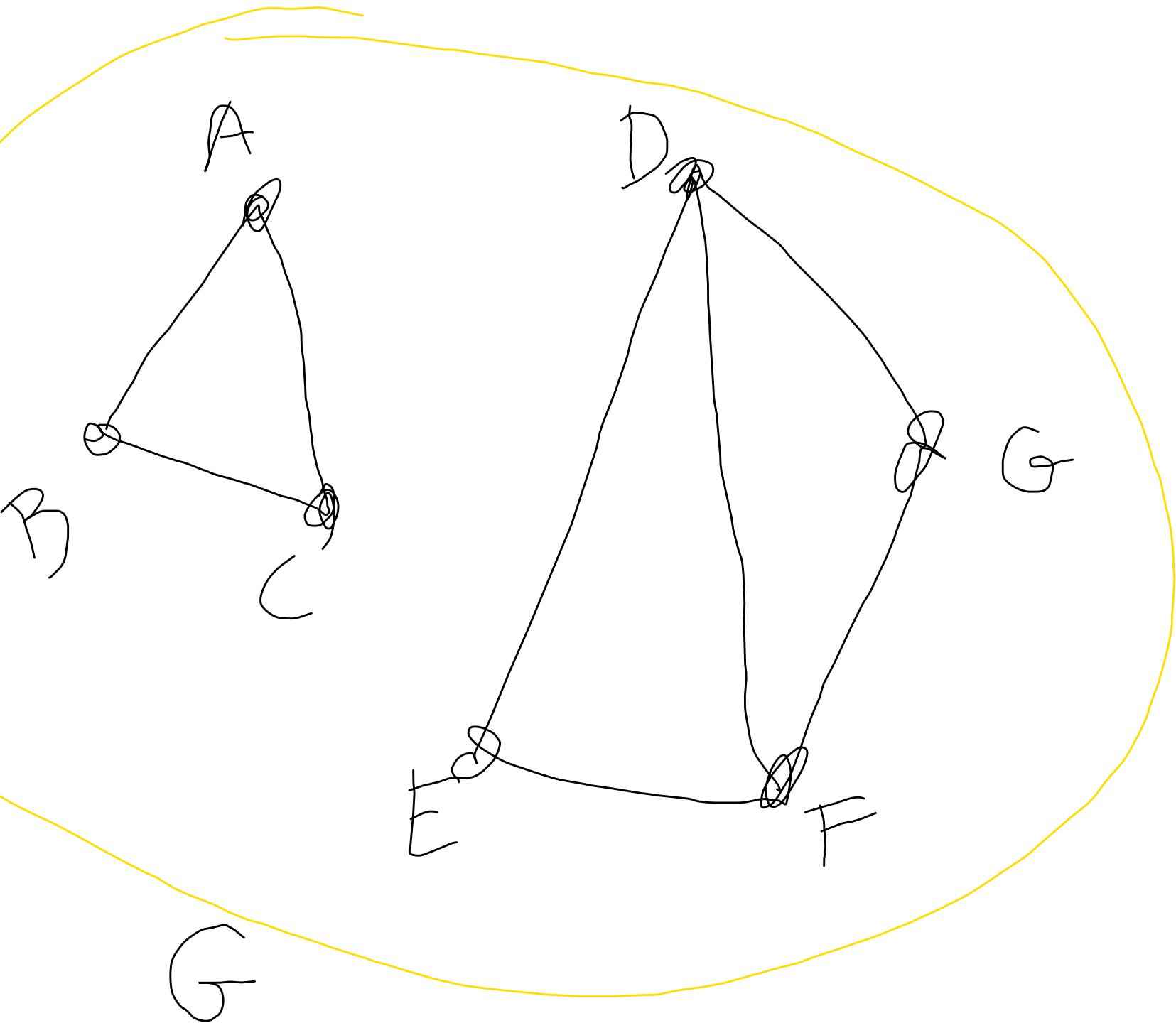
2) $\forall x, y \in X \quad x R y \iff y R x$ (symmetry)

3) $\forall x, y, z \in X \quad (x R y) \wedge (y R z) \Rightarrow (x R z)$ (transitivity)

DEF - A partition of a set X is a family S of subsets of X , $S = \{X_1, X_2, \dots, X_h\}$ such that 1) $X_1 \cup X_2 \cup \dots \cup X_h = X$ and 2) $i \neq j \Rightarrow X_i \cap X_j = \emptyset$

THM - Given an equivalence relation R on a set X ,
calling **equivalence class** every subset of X of elements
 y such that for the same x we have $y R x$,
the family of equivalence classes is a partition of X





} A, B, C

} D, E, F, G