

MA 182, Honors Mathematical Analysis II, Fall '05.
Extra Homework Sheet # 5.

1. Differentiate the following functions:

(a) $f(x) := \int_0^x \tan \alpha \, d\alpha$

(b) $g(x) := \int_x^2 \tan \alpha \, d\alpha$

(c) $h(y) := \int_2^y \sqrt{1+t^2} \, dt$

(d) $k(x) := \int_{\sin x}^0 \ln(3+t^4) \, dt$

(e) $A(x) := \int_{-x}^x e^{t^2} \, dt$

[Hint: $\int_{-x}^x \cdots = \int_{-x}^0 \cdots + \int_0^x \cdots$]

(f) $G(x) := \int_{x^2}^{x^4} \log_2 t \, dt$

[Hint: Similar trick as above. It doesn't matter that 0 is not between x^2 and x^4 . Actually, one can use any $c \in \mathbb{R}$ to split the integral.]

2. Consider the function $F : \mathbb{R} \rightarrow \mathbb{R}$ defined by

$$F(x) := \int_{10}^x \frac{t}{1+t^6} \, dt$$

Find the intervals of increase and decrease of F . Determine all the relative minimum and maximum points.

[Tip: Do not attempt to solve the integral.]

3. Evaluate the following definite integrals:

(a) $\int_0^1 \cos(\pi t) \, dt$

(b) $\int_0^{\pi/2} e^{\sin x} \cos x \, dx$

(c) $\int_1^2 x\sqrt{x-1} \, dx$

(d) $\int_e^{e^4} \frac{1}{x\sqrt{\ln x}} \, dx$

4. Evaluate $\int \tan x \, dx$

[Hint: Rewrite $\tan x$ as $\frac{\sin x}{\cos x}$ and use the substitution $u = \cos x$.]