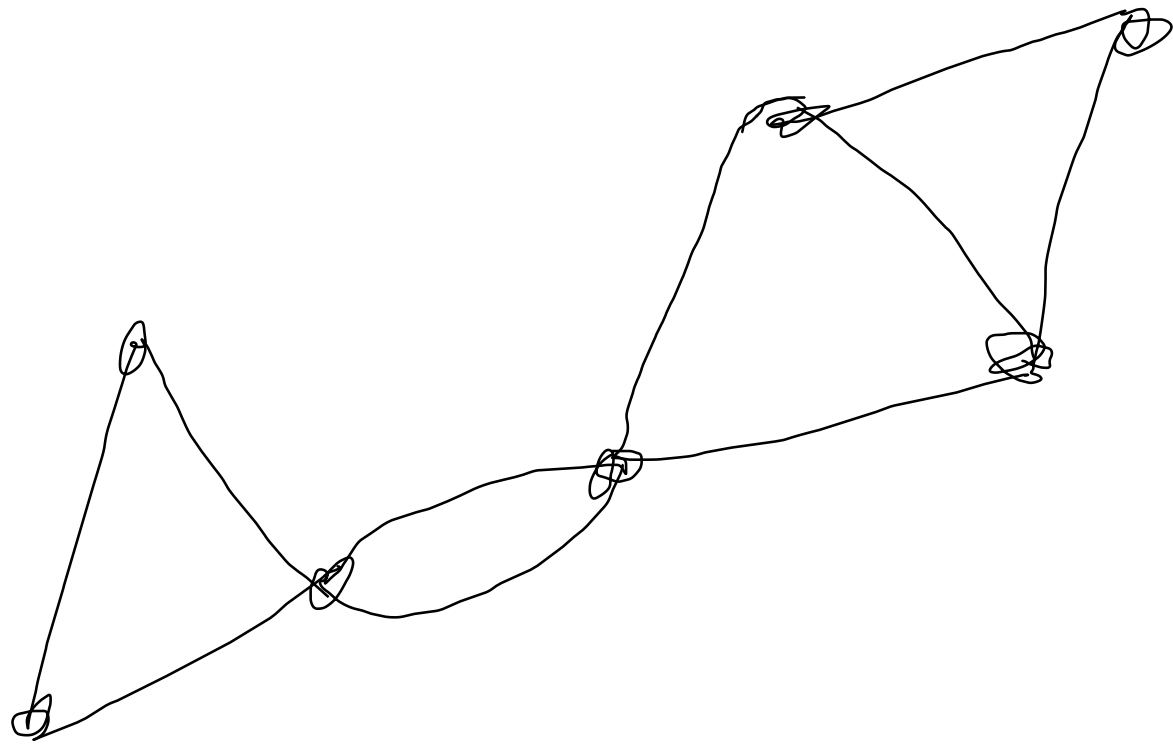
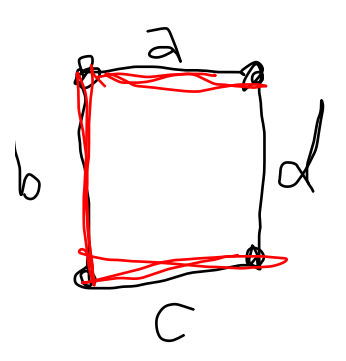
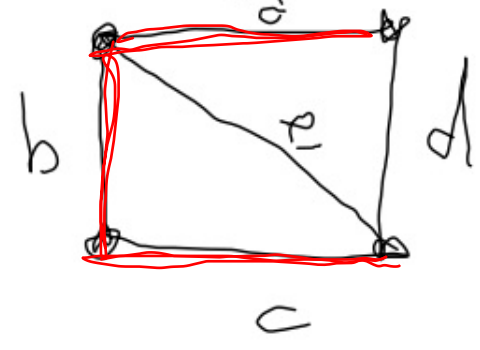
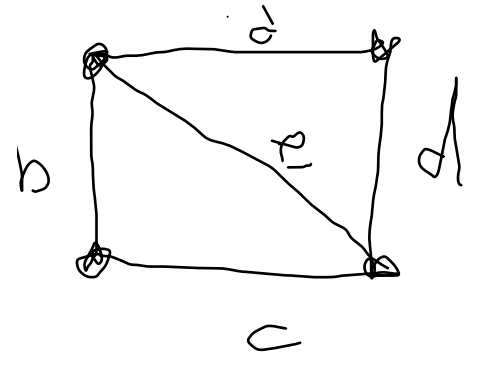
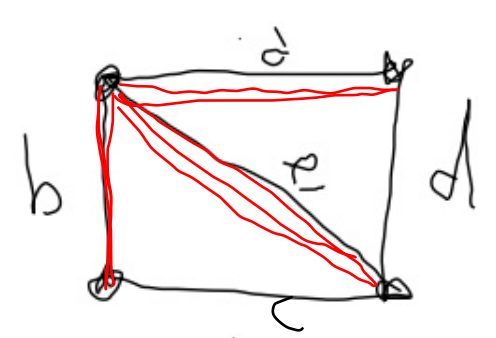
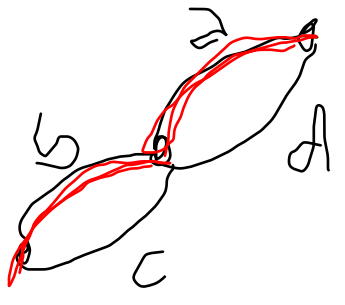


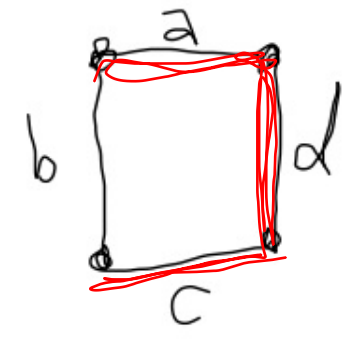
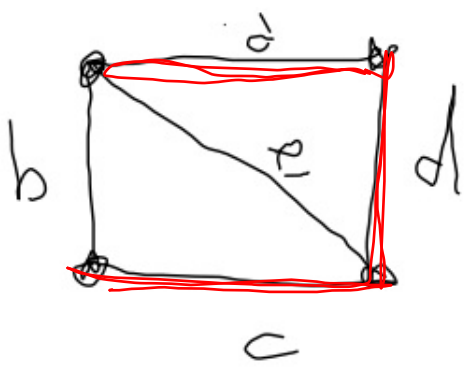
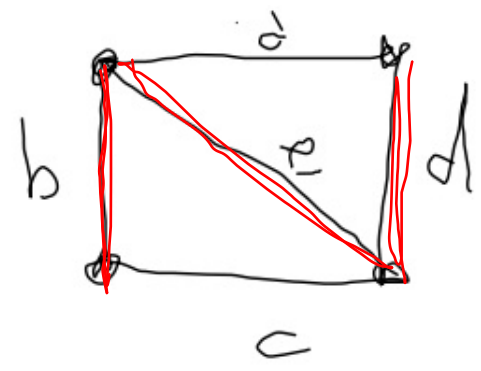
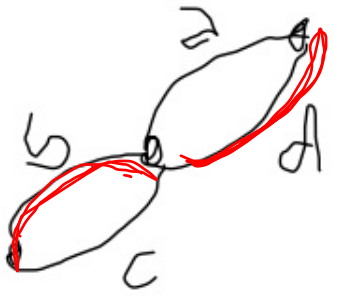
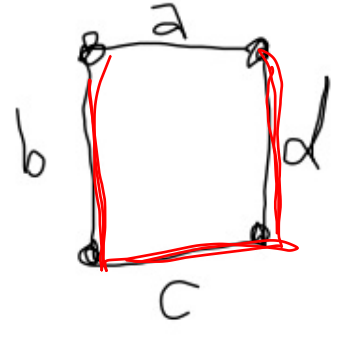
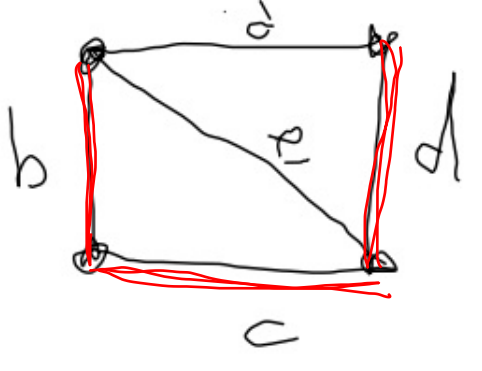
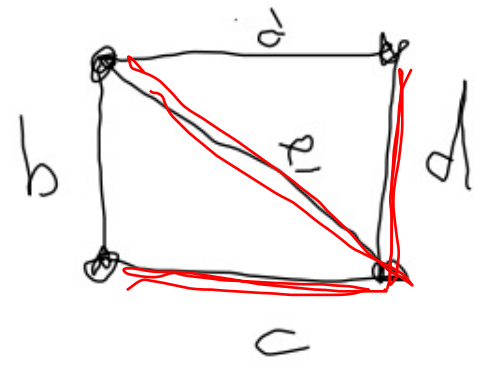
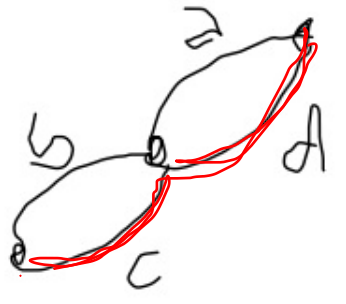
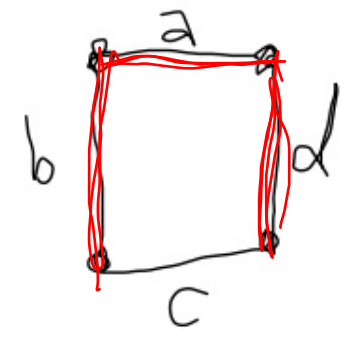
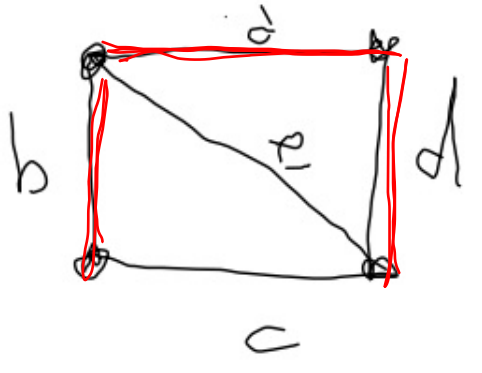
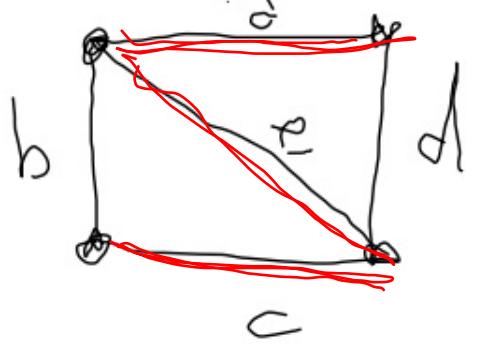
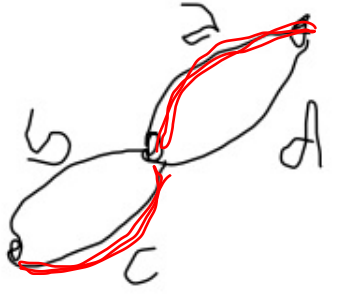
By deleting v and all incident edges I got



$G \oplus e$

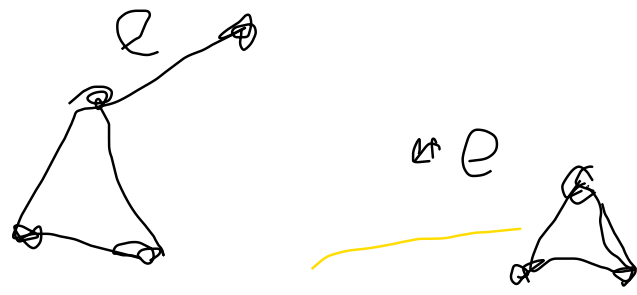


$G \oplus e$

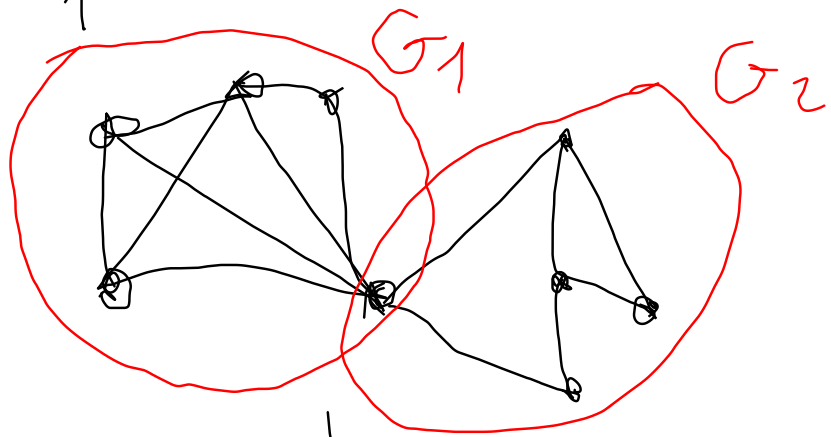
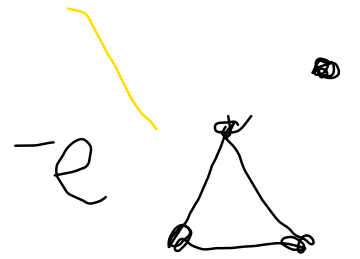


Shortcuts:

1) G disconnected $\Rightarrow \tau(G) = 0$



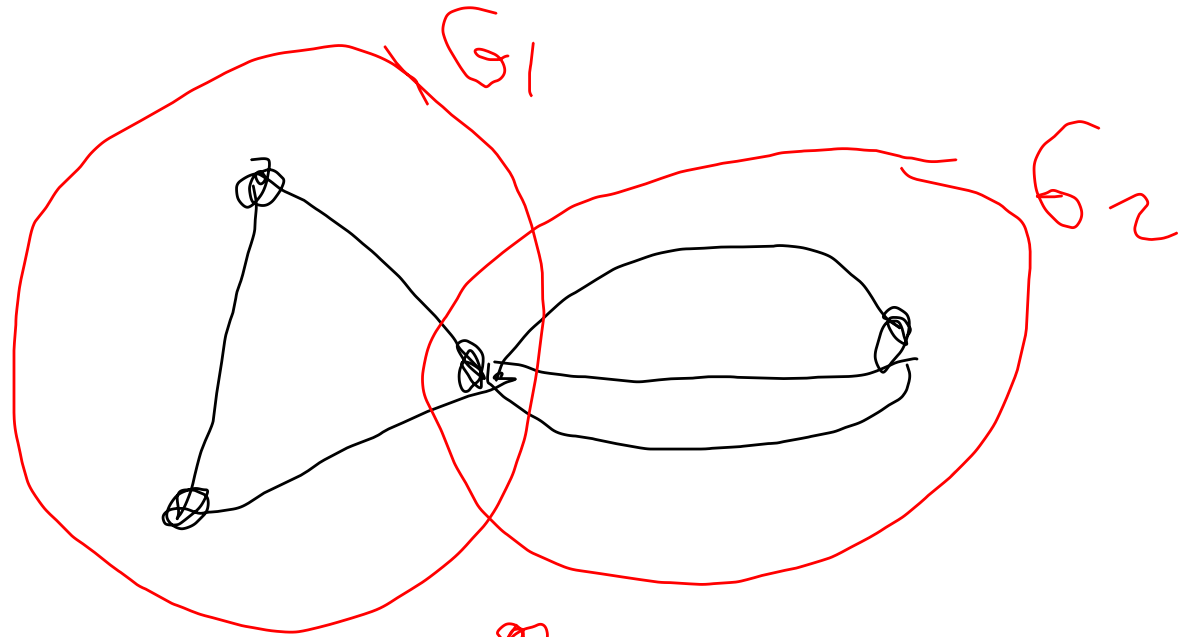
2) $G = G_1 \cup G_2$, where $G_1 \cap G_2$ is a vertex



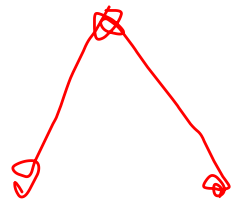
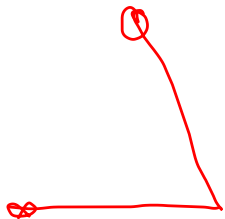
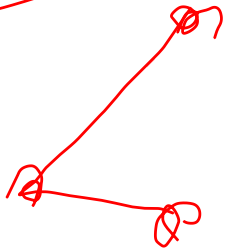
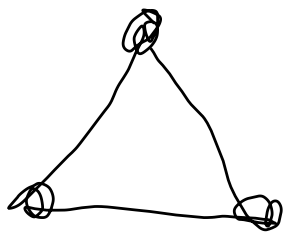
$$\tau(G) = \tau(G_1) \cdot \tau(G_2)$$

3) If you have multiple edges, each gives a different spanning tree

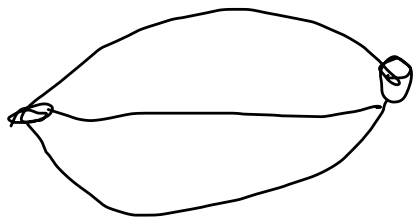
4) If G is a k -cycle, then $\tau(G) = k$



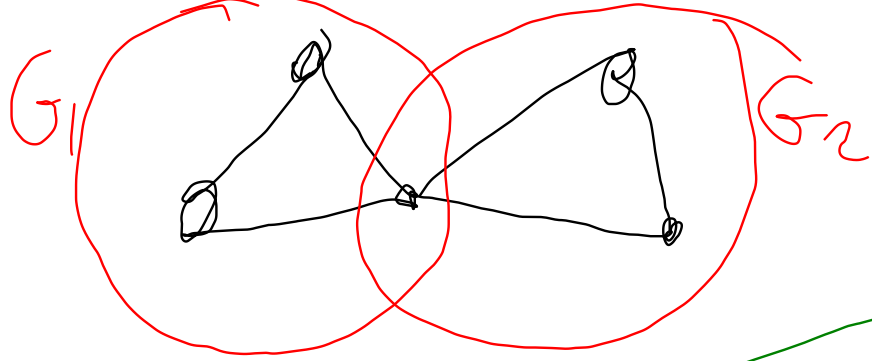
$$\chi(G_1) = 3$$



$$\chi(G_2) = 3$$



$$\chi(G) = 3 \cdot 3 = 9$$



$$\chi(G) = \chi(G_1) \cdot \chi(G_2) = 3 \cdot 3 = 9$$

