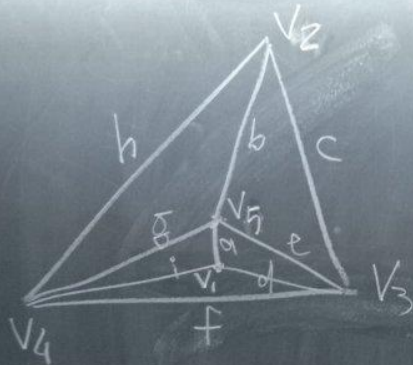




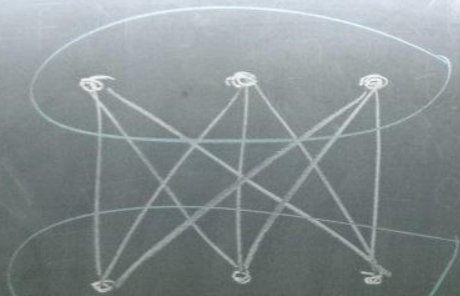
$$V(G)$$

$$E(G)$$



$$\binom{n}{m} = \frac{n!}{m!(n-m)!}$$

$$\binom{n}{2} = \frac{n \cdot (n-1) \cdot \cancel{(n-2)} \cdot \dots \cdot \cancel{2} \cdot 1}{(2-1) \cdot \cancel{(2-1)} \cdot \dots \cdot \cancel{2} \cdot 1}$$



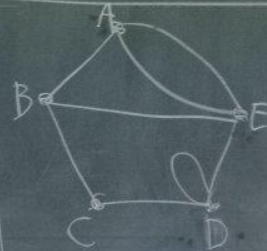
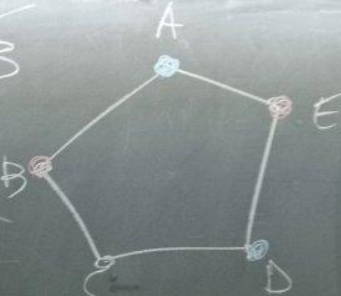
$K_{3,3}$

~~$X = A, E, F, B$~~

~~$Y = D, H, G, C$~~

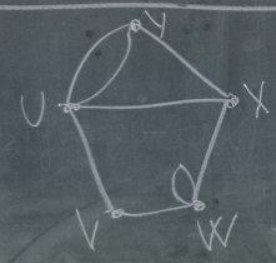
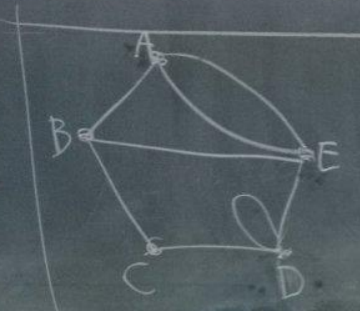
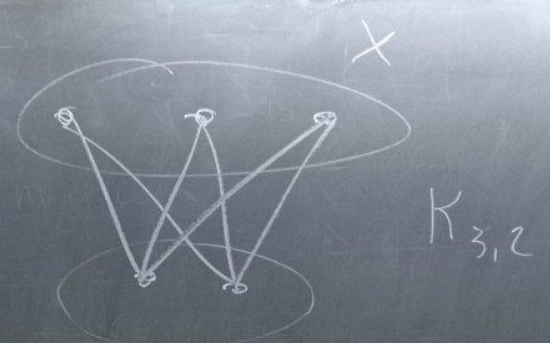
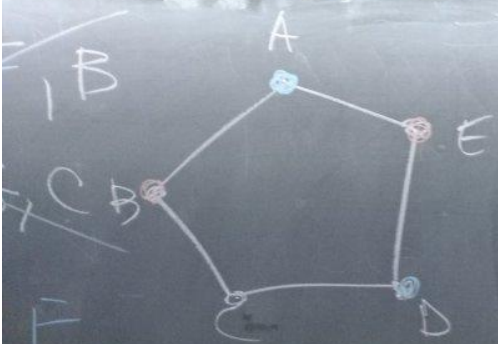
$X = A, H, C, F$

$Y = B, D, E, G$



$Z \cdot X$

$Z \cdot Y$



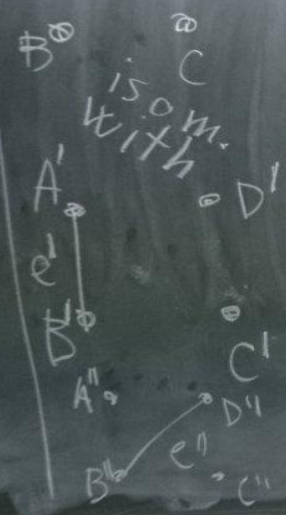
$\textcircled{1} \begin{cases} \vartheta(A) = Y \\ \vartheta(E) = U \end{cases}$ or $\textcircled{2} \begin{cases} \vartheta(A) = U \\ \vartheta(E) = Y \end{cases}$
 $\vartheta(D) = W$

0

1

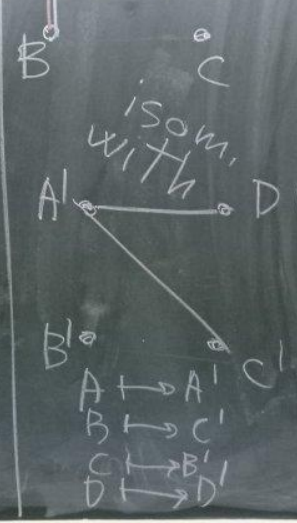
2

3



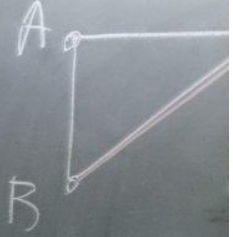
isom.
with

- $A \mapsto A'$
- $B \mapsto D'$
- $C \mapsto C'$
- $D \mapsto B'$
- $e \mapsto e'$

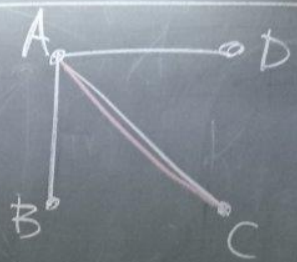
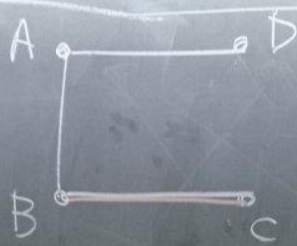
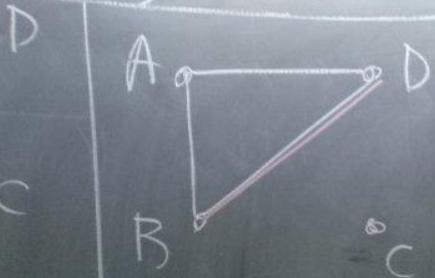


isom.
with

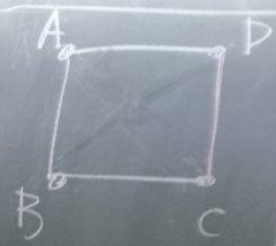
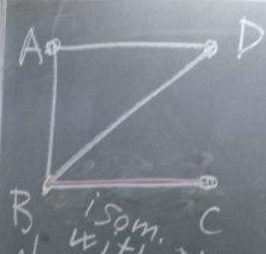
- $A \mapsto A'$
- $B \mapsto C'$
- $C \mapsto B'$
- $D \mapsto D'$



3



4

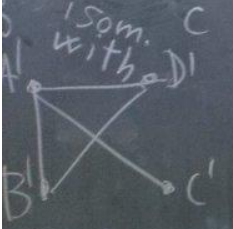
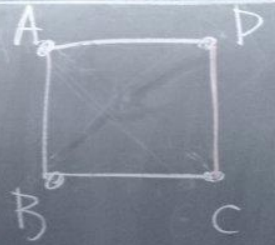
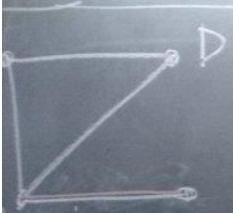


isom. with D



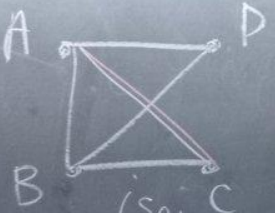
- A → B'
- B → A'
- C → C'
- D → D'

A
B

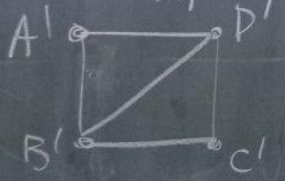


$A \mapsto B'$
 $B \mapsto A'$
 $C \mapsto C'$
 $D \mapsto D'$

5

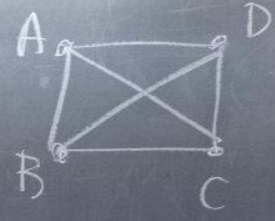


isom. with



$A' \mapsto D'$
 $B' \mapsto B'$
 $C' \mapsto C'$
 $D' \mapsto A'$

6



1-cube

2-cube



6



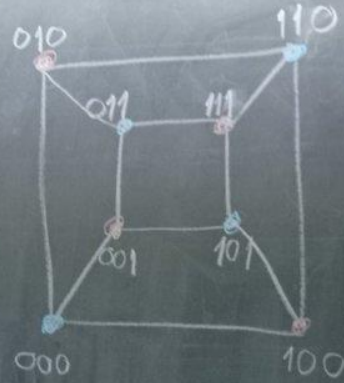
1-кубе



2-кубе



3-кубе



GENERAL
I want to prove a statement depending on a natural number

Inductive premise: prove $P(1)$

Inductive step:

Inductive hypothesis: $P(k-1)$ is true

Inductive thesis: $P(k)$ is true

I get k different permutations out of each of the previous $(k-1)!$ permutations. Total: $k \cdot (k-1)! = k!$

$p_1(1)$ $p_1(2)$... $p_1(k-2)$ $p_1(k-1)$

$p_2(1)$ $p_2(2)$... $p_2(k-2)$ $p_2(k-1)$

$p_h(1)$ $p_h(2)$... $p_h(k-2)$ $p_h(k-1)$

GENERAL
ending on a natural number n : $P(n)$

$p_1(1) \cdot p_1(2) \cdots p_1(k-2) \cdot p_1(k-1)$

$p_2(1) \cdot p_2(2) \cdots p_2(k-2) \cdot p_2(k-1)$

$p_h(1) \cdot p_h(2) \cdots p_h(k-2) \cdot p_h(k-1)$

1 2 3 ... (k-2) (k-1)

$k \cdot p_1(1) \cdot p_1(2) \cdots p_1(k-1)$
 $p_1(1) \cdot k \cdot p_1(2) \cdots p_1(k-1)$

\vdots
 $p_1(1) \cdot p_1(2) \cdots p_1(k-2) \cdot k \cdot p_1(k-1)$
 $p_1(1) \cdot p_1(2) \cdots p_1(k-1) \cdot k$

I want to

Inductive pr

Inductive hypo

Inductive thos

Proof of the indu

Set $h = (k-1)!$

I want to prove that the ^{EXAMPLE} number of permutations

Inductive premise: there is only one permutation of

$\dots (k-2) (k-1)$ Inductive hypothesis: the number of permutations of $\{1, \dots, k-1\}$

1) $p_1(2) \dots p_1(k-1)$ Inductive thesis: " " " " " " " $\{1, \dots, k\}$

k $p_1(2) \dots p_1(k-1)$ Proof of the inductive step

1) $p_1(2) \dots p_1(k-2) k p_1(k-1)$ Set $h = (k-1)!$
2) $\dots p_1(k-1) k$

EXAMPLE
The number of permutations of $\{1, 2, \dots, n\}$ is $n!$

here is only one permutation of $\{1\}$, and $1! = 1$

The number of permutations of $\{1, 2, \dots, k-1\}$ is $(k-1)! = (k-1)(k-2)\dots \cdot 2 \cdot 1$

" " " " " $\{1, 2, \dots, k-1, k\}$ is $k!$

1	21	321	231	213
	12	312	132	123