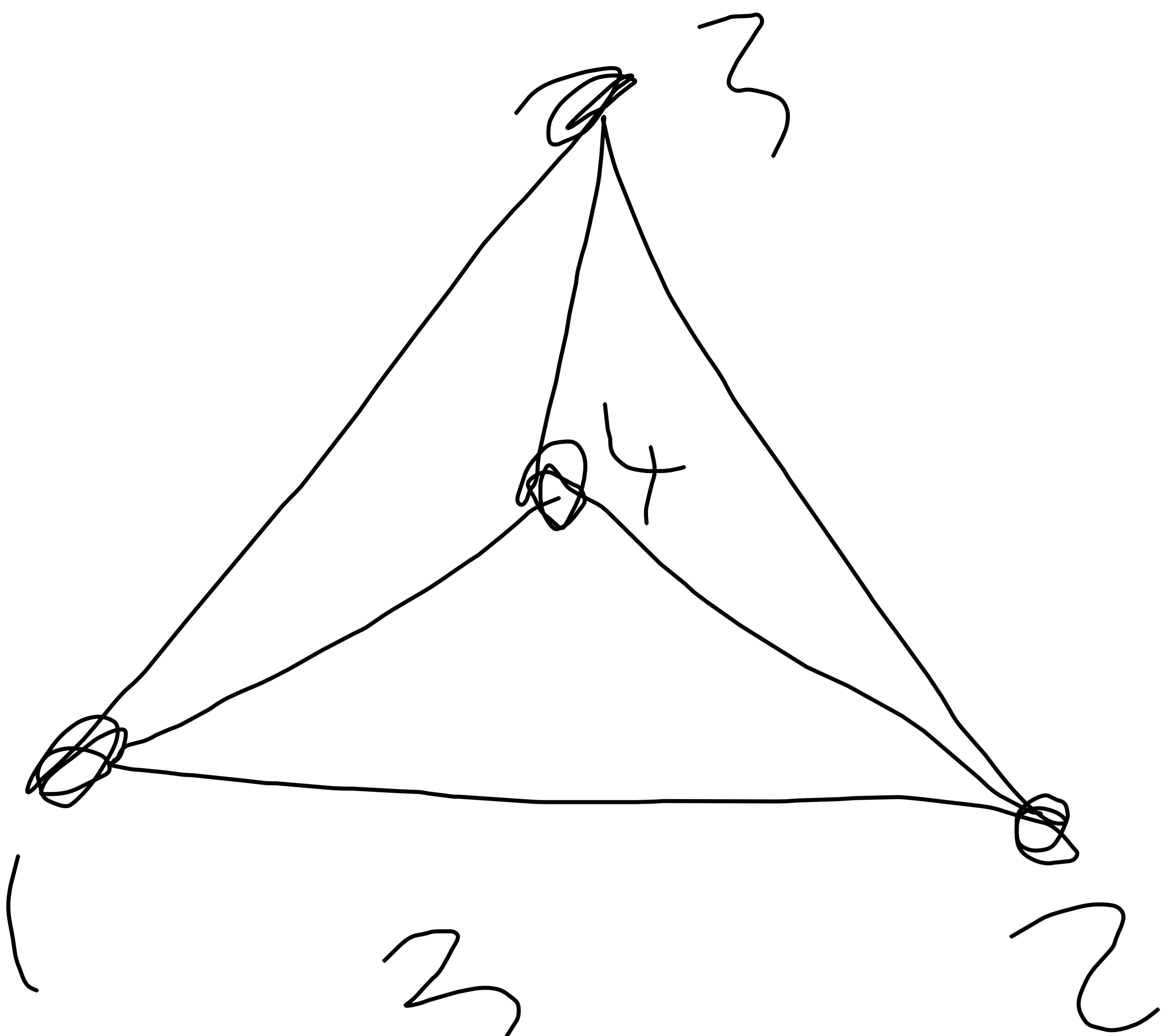
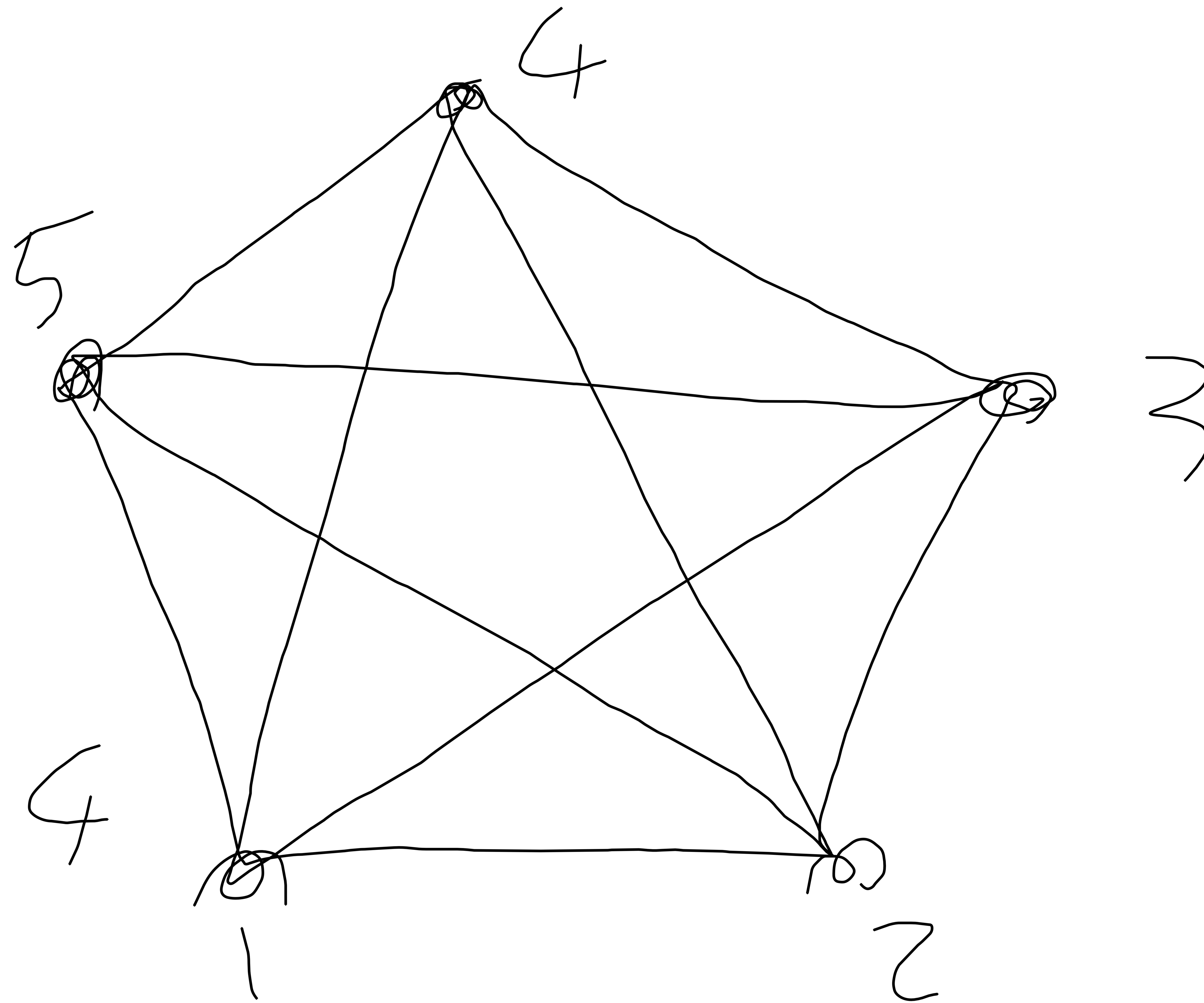


$$\Delta \geq k-1 \quad k \leq \Delta+1$$

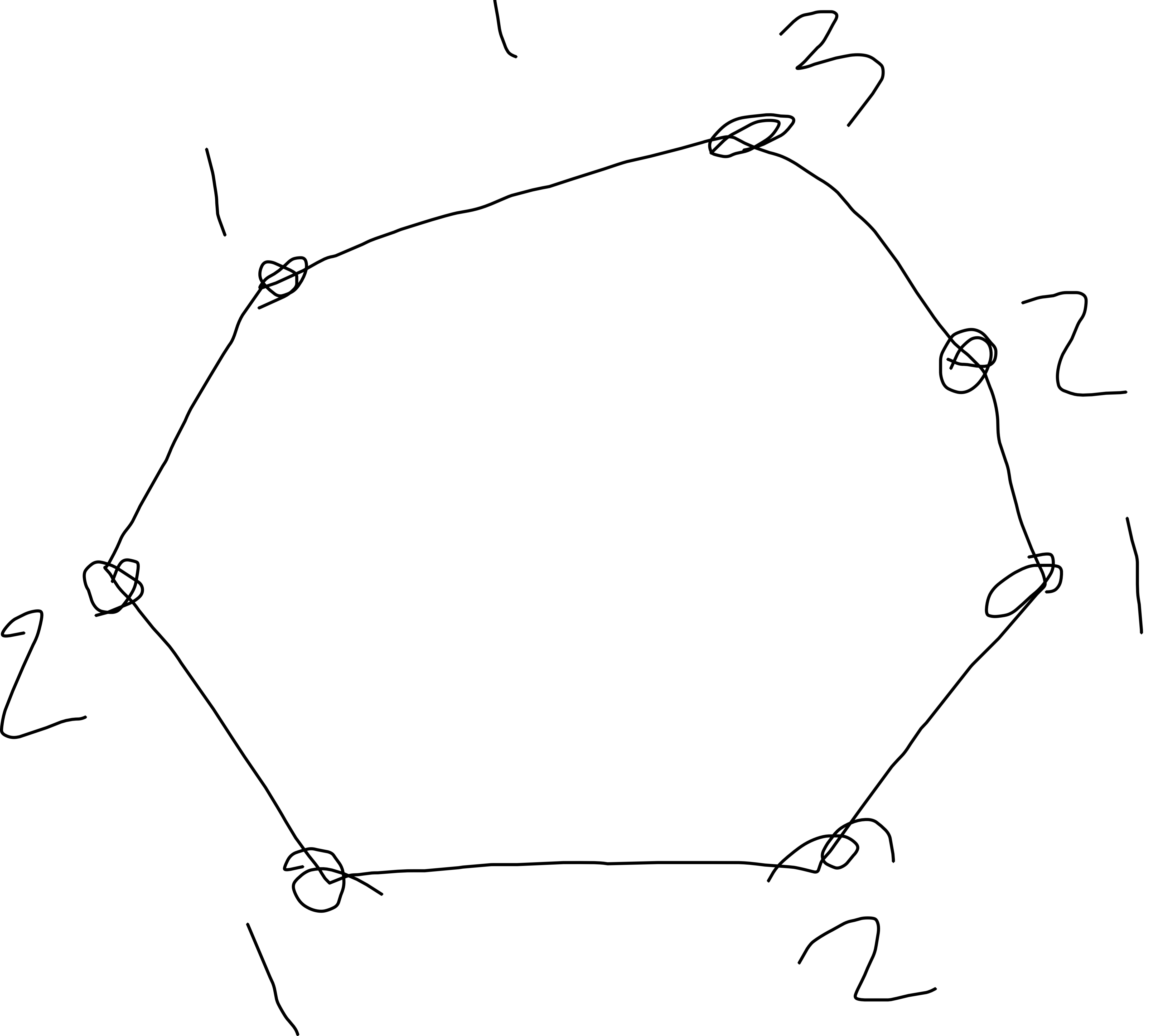
$K_4$

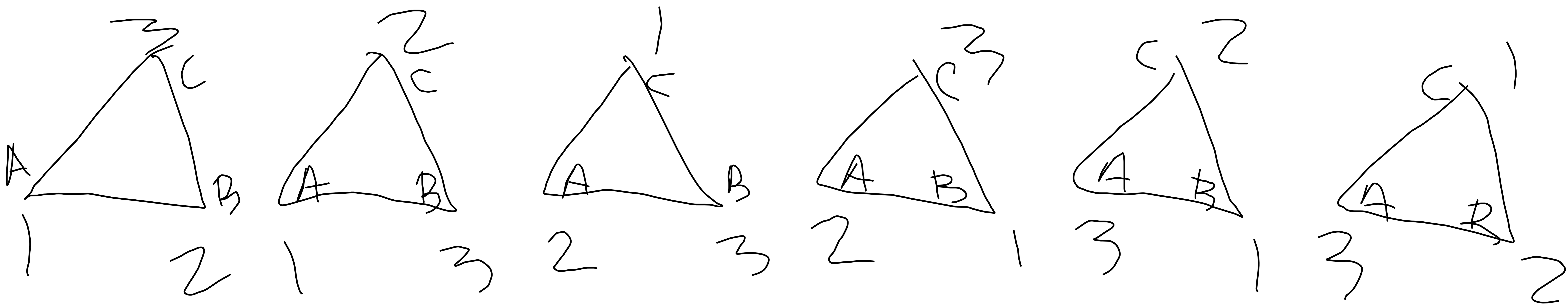


$\Delta = 3$

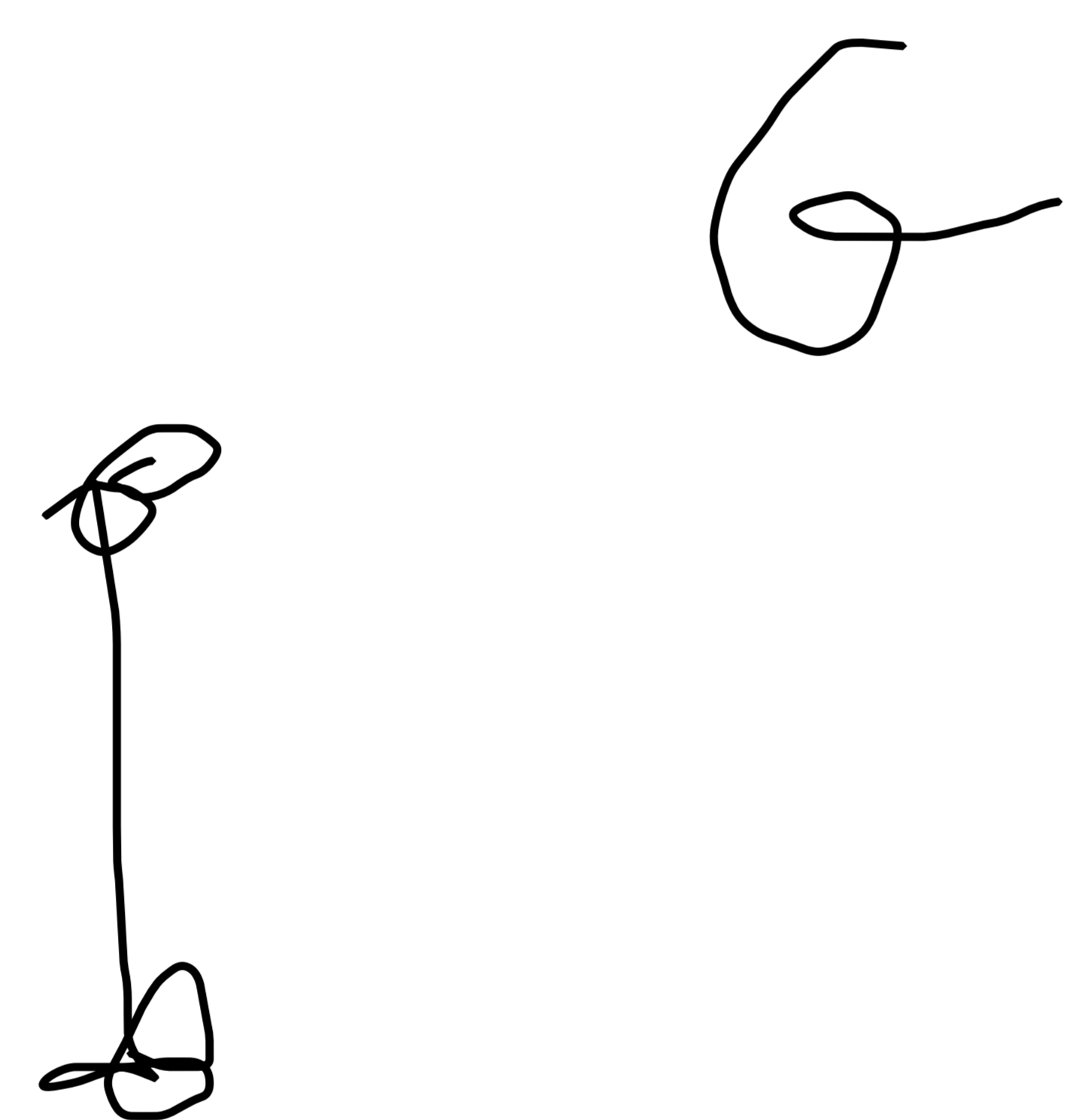


$\Delta = 4$





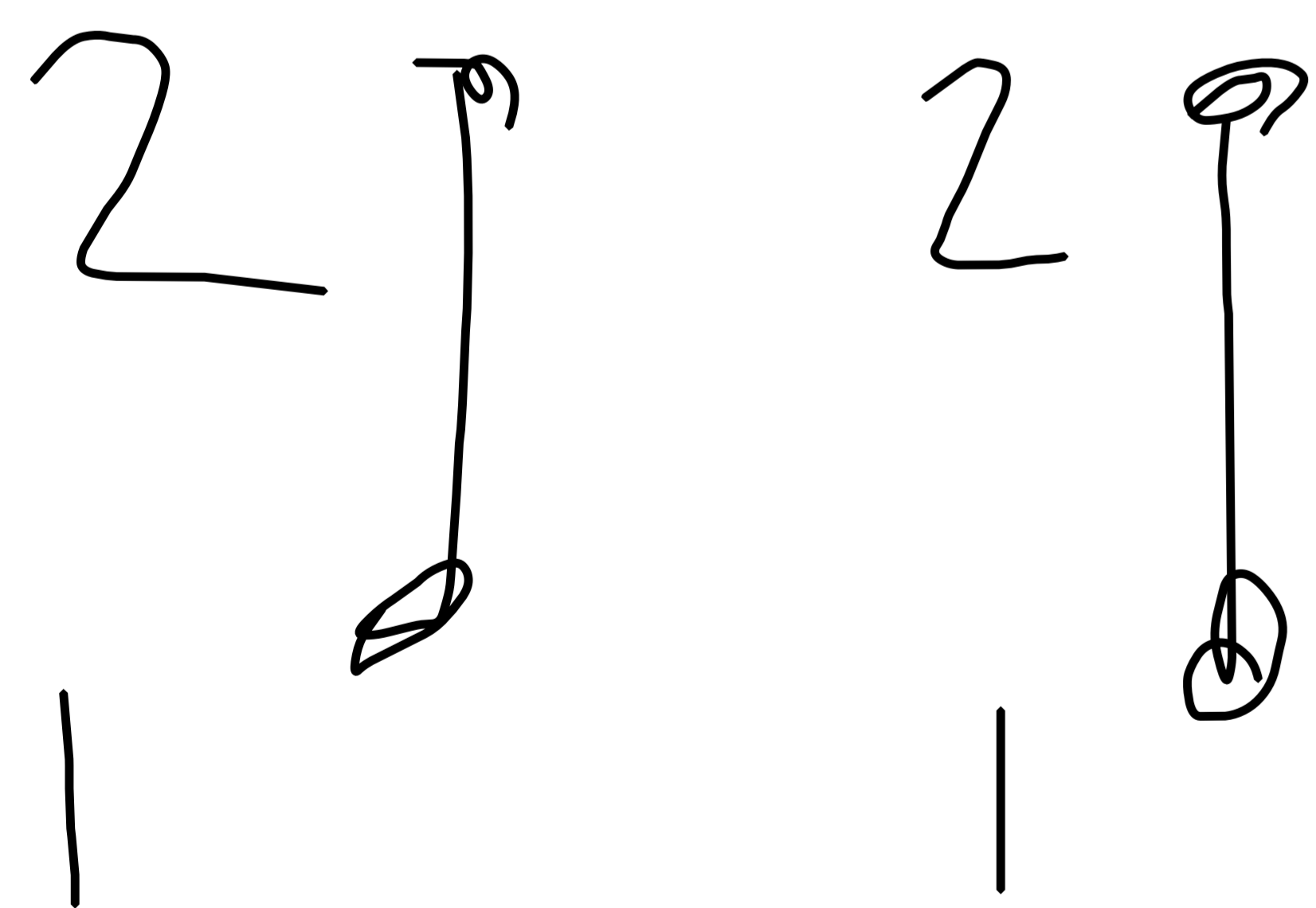
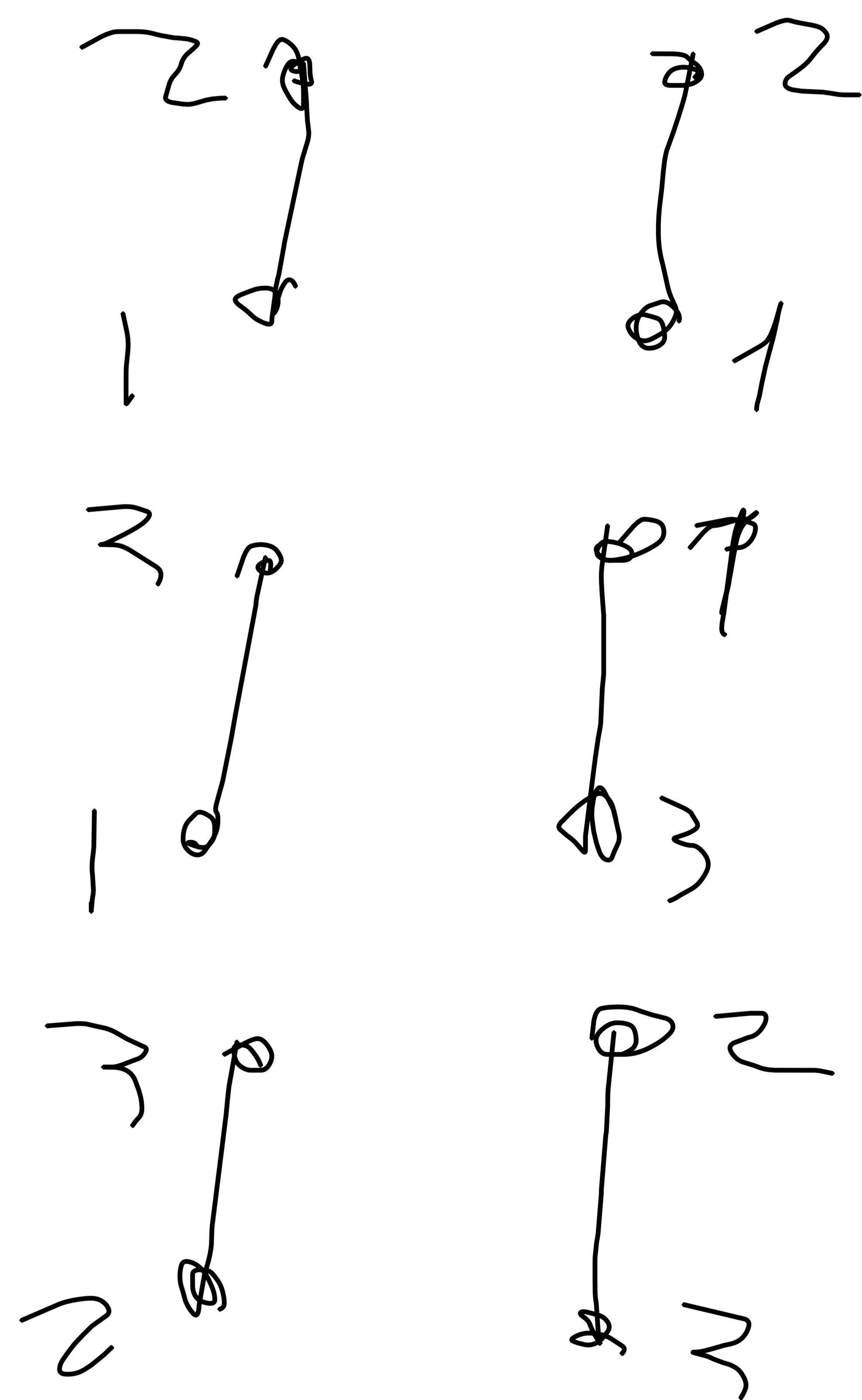
$$\pi_3(G) = 6$$

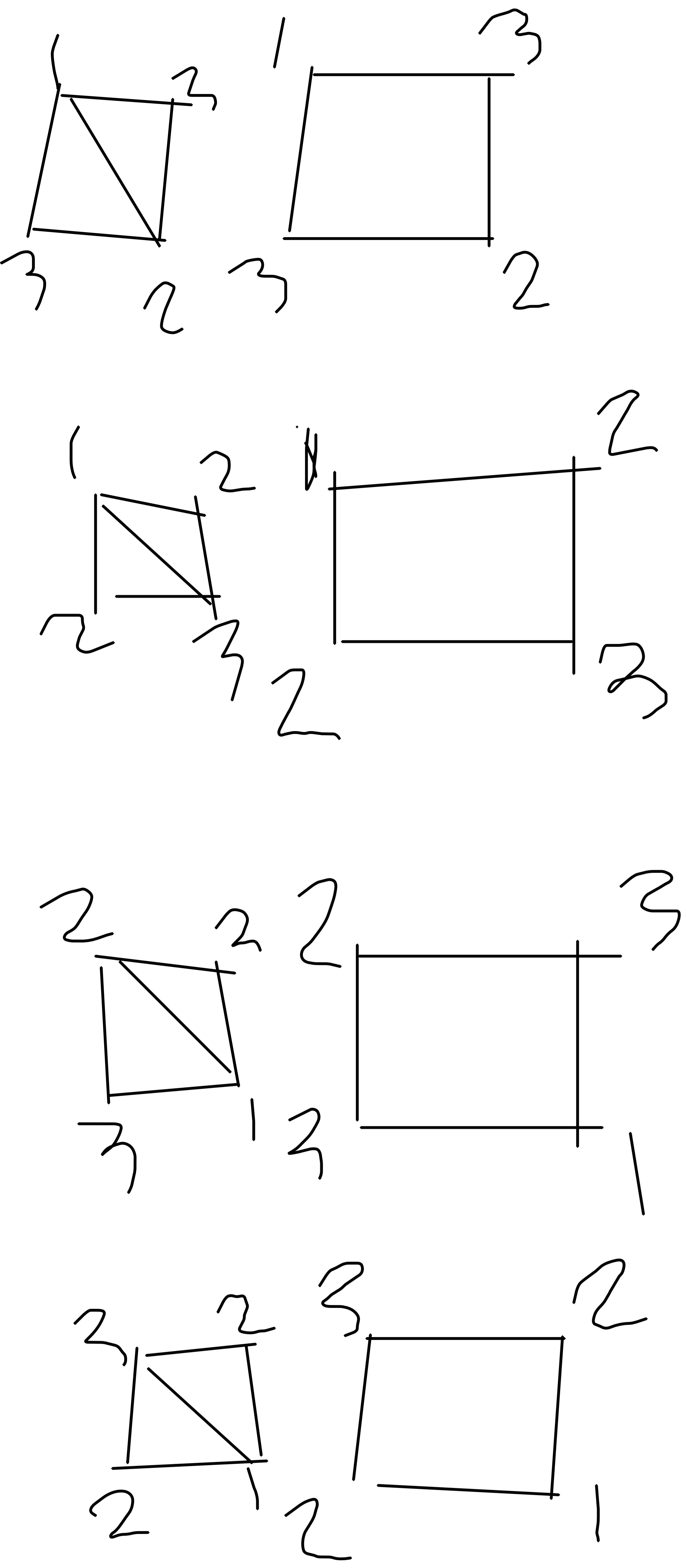


$$\pi_1(G) = 0$$

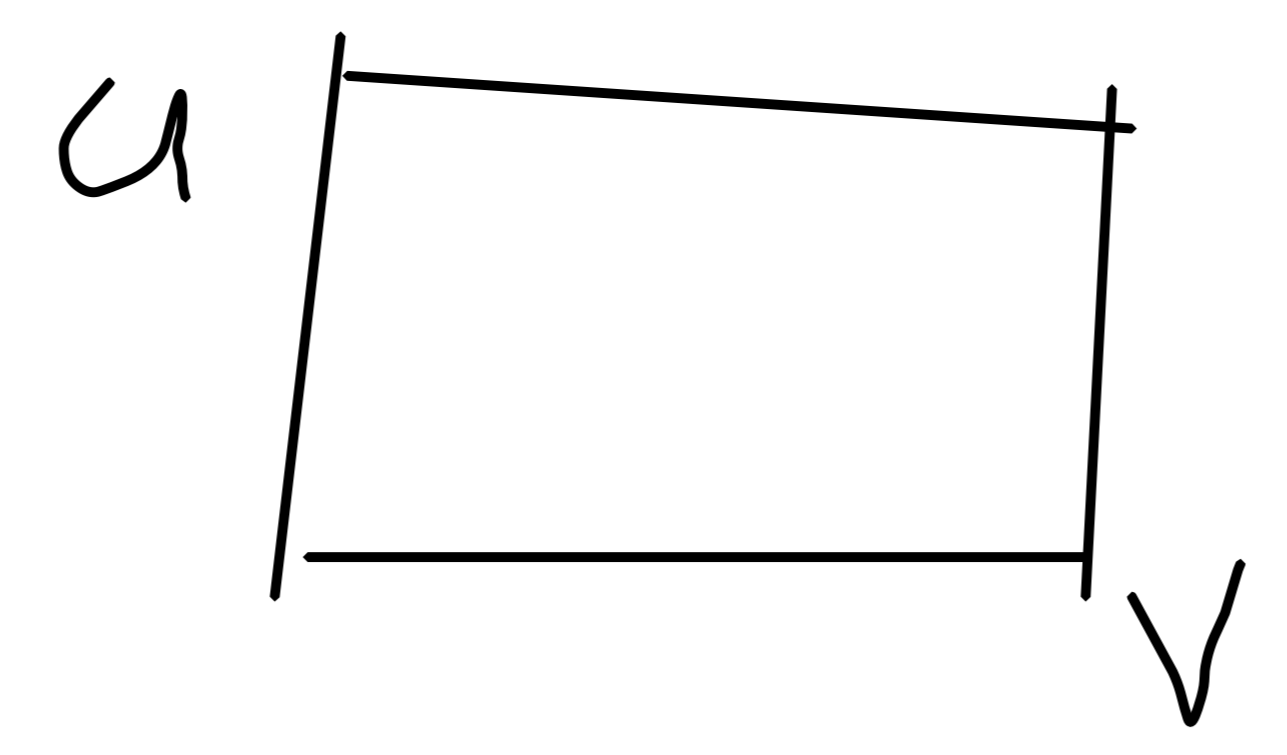
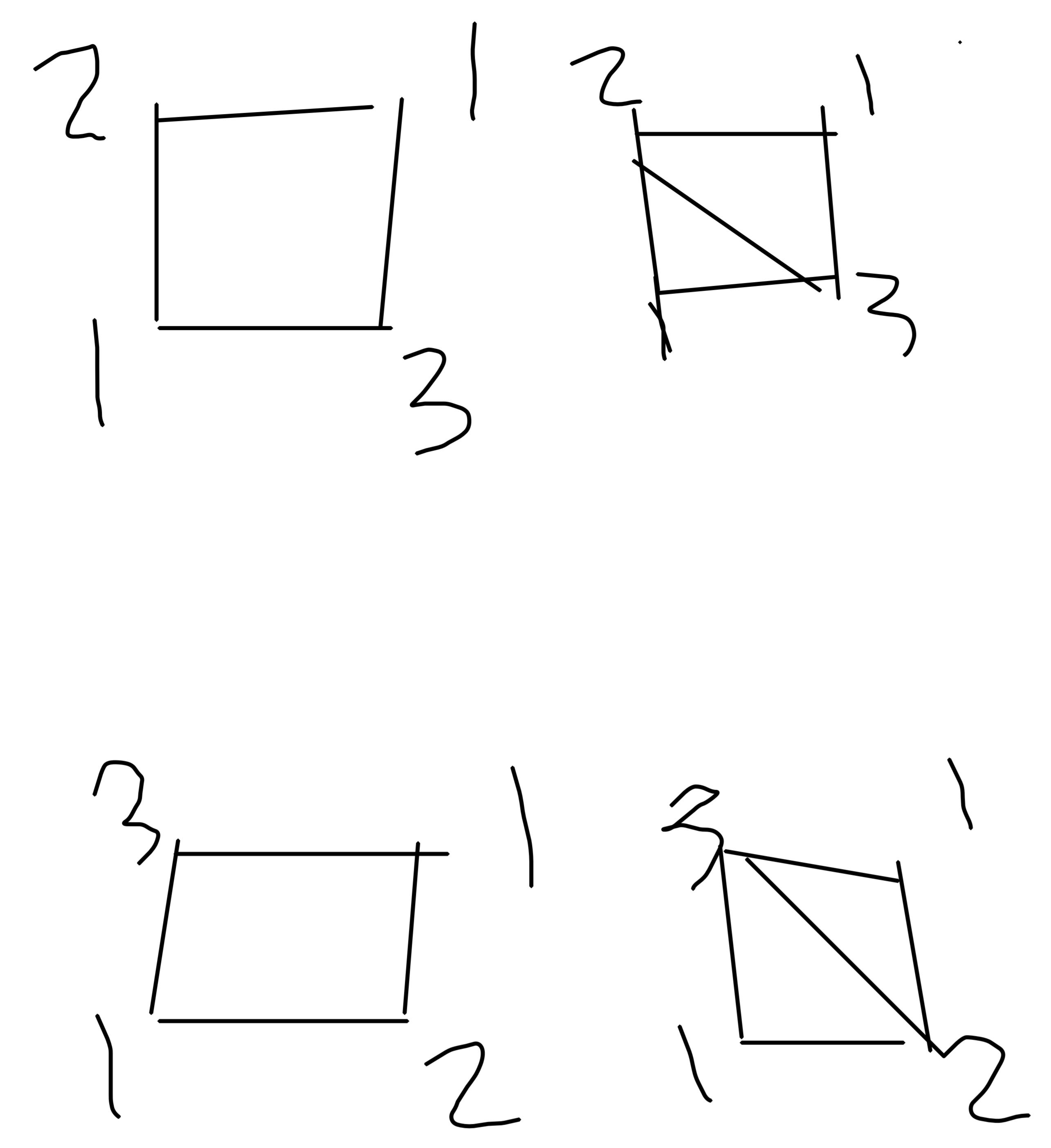
$$\pi_2(G) = 2$$

$$\pi_3(G) = 6$$

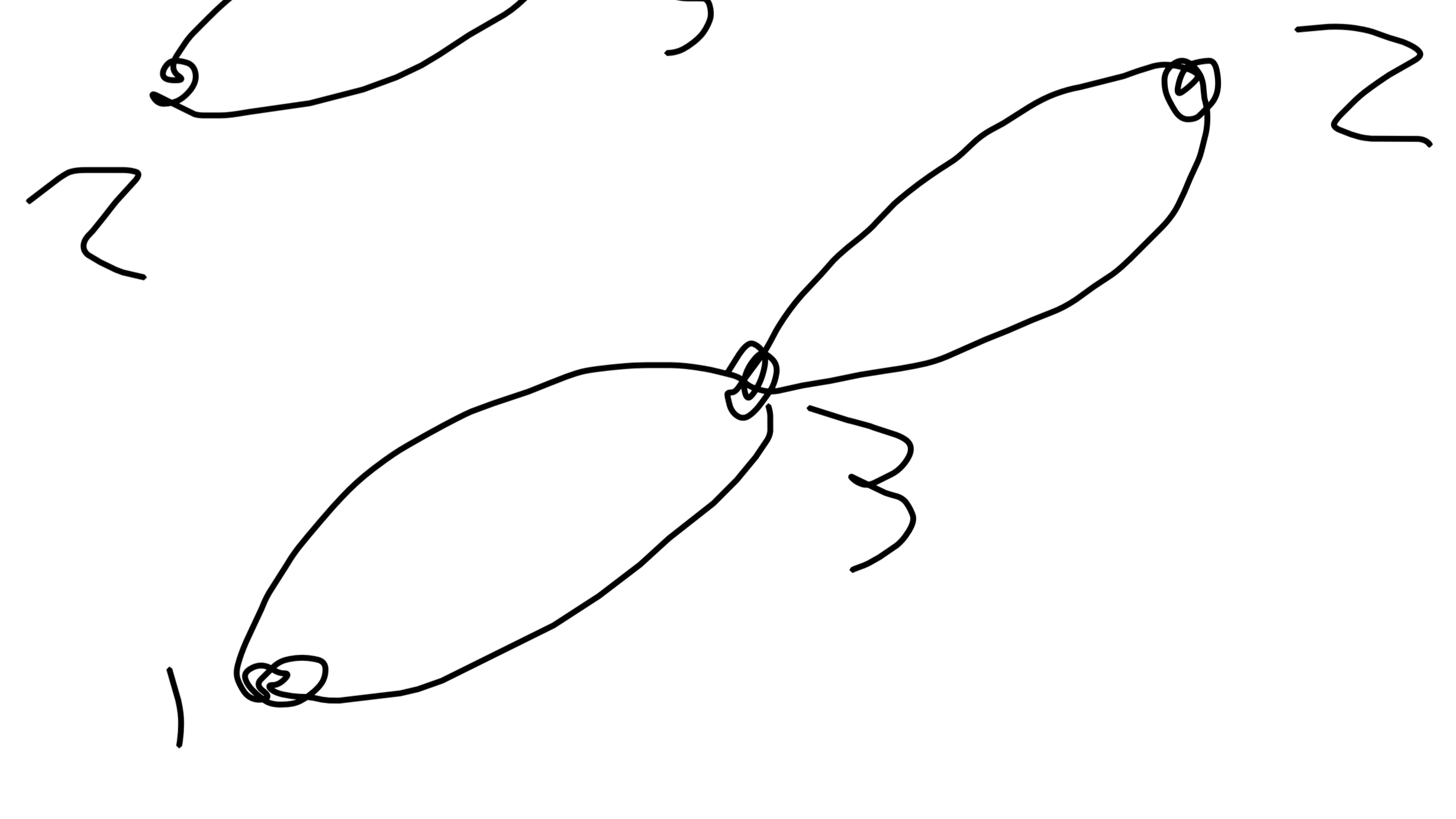
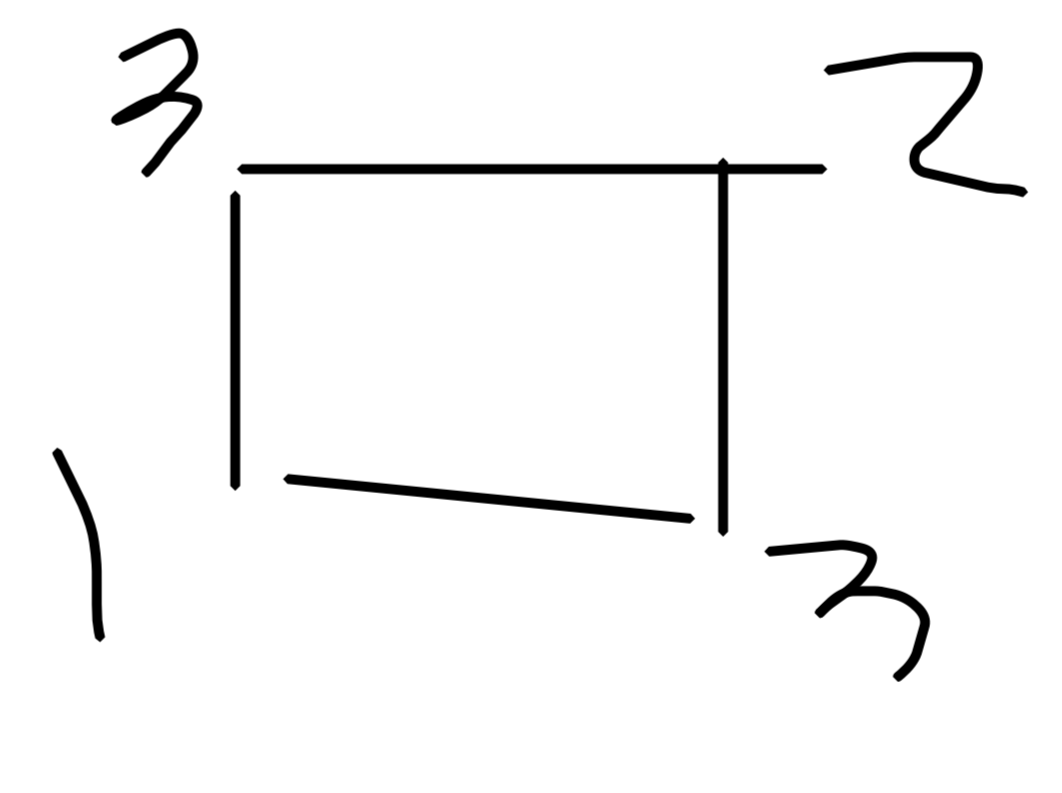
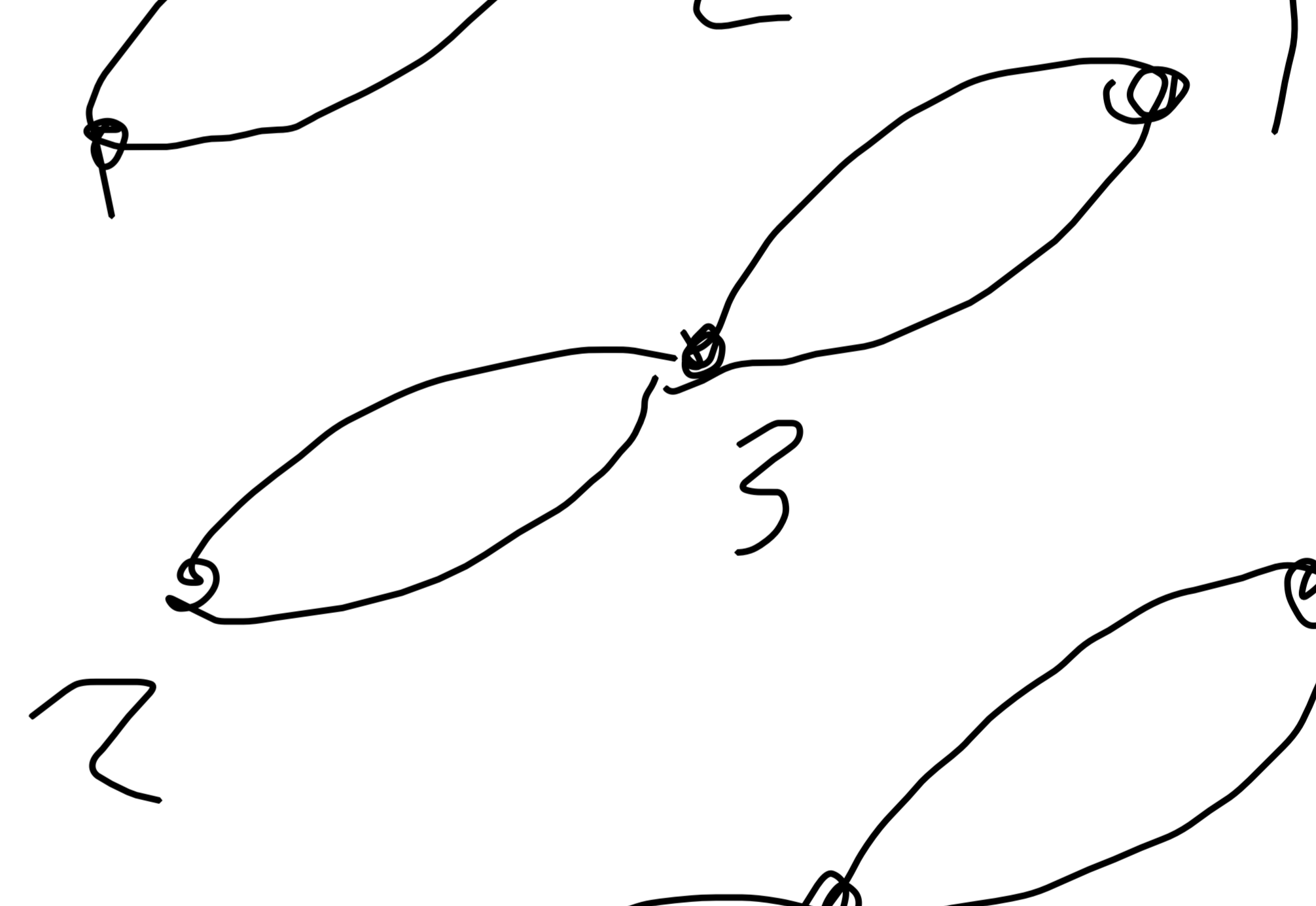
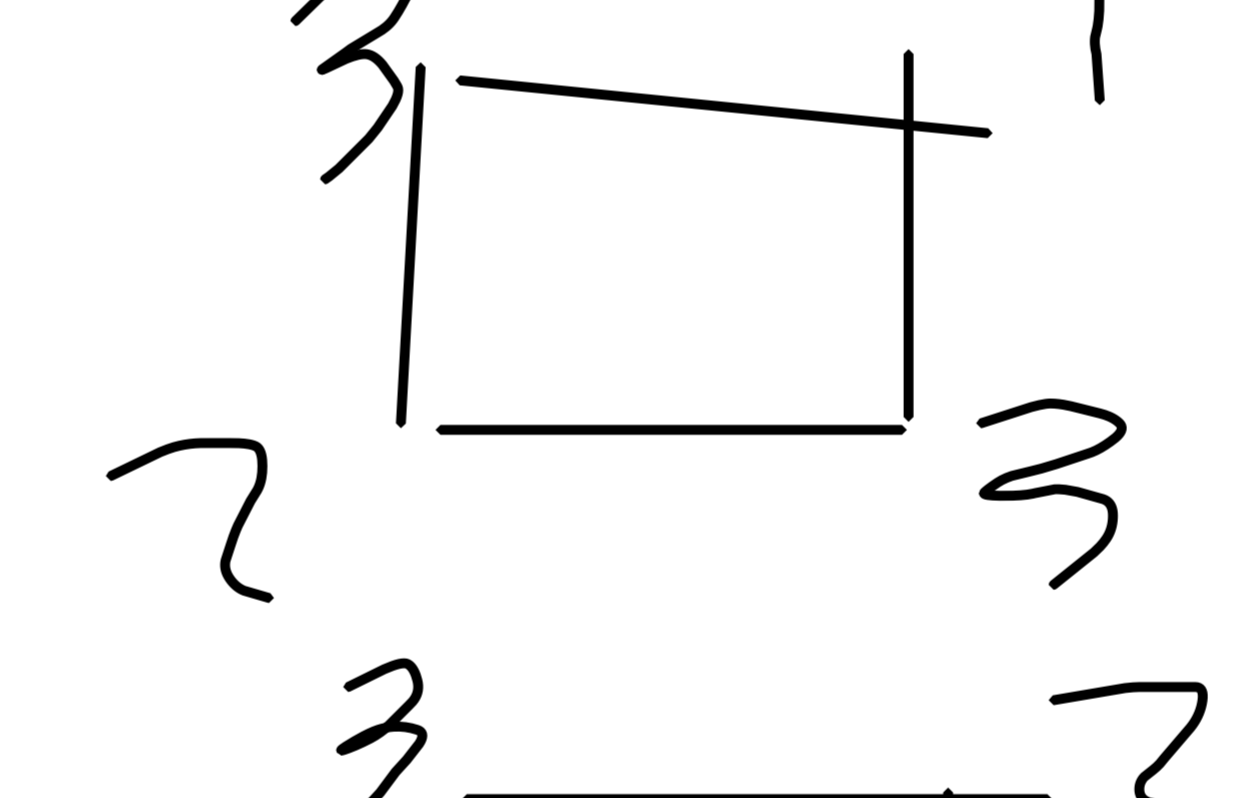
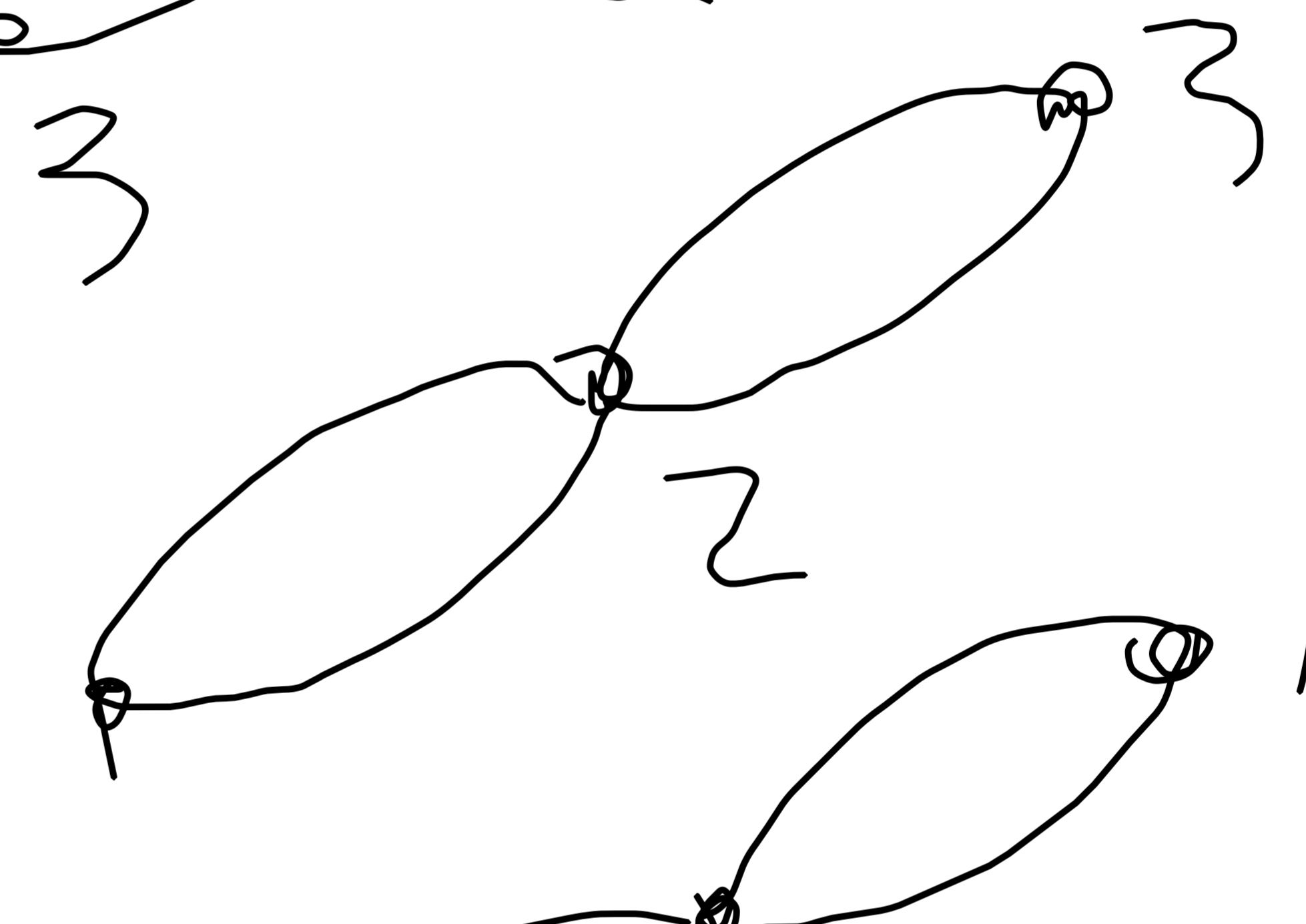
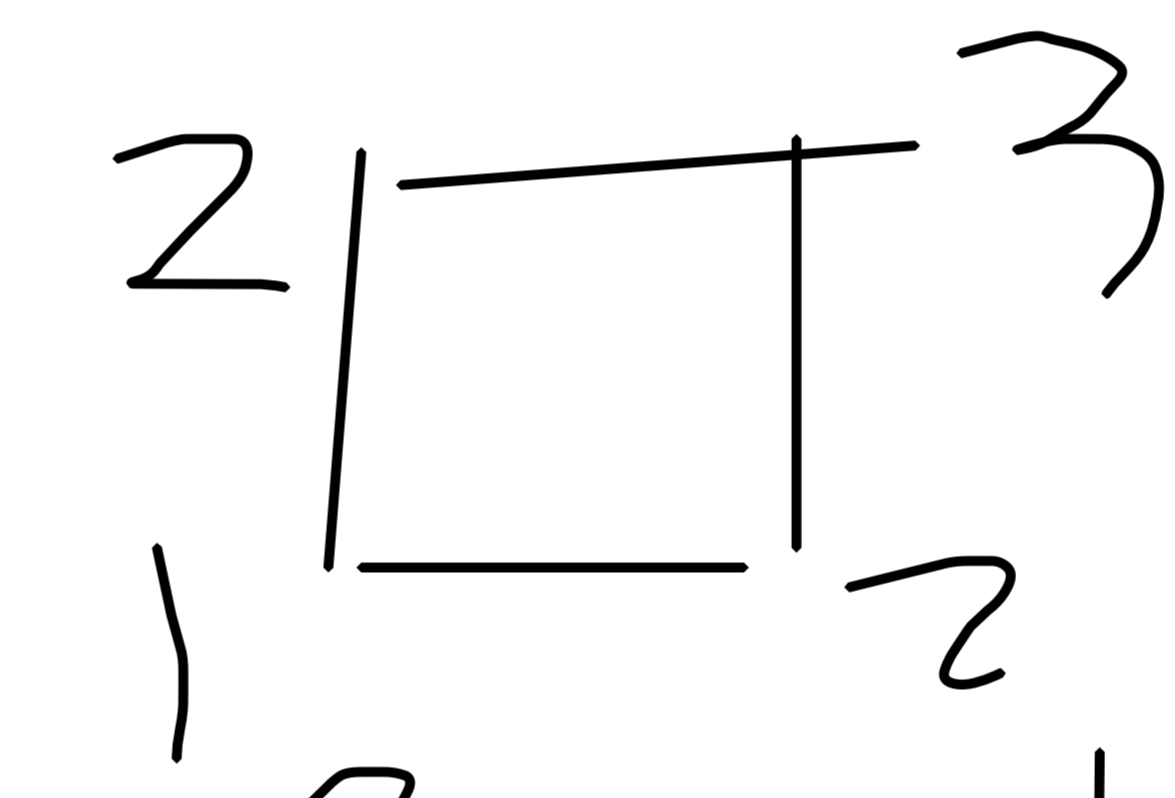
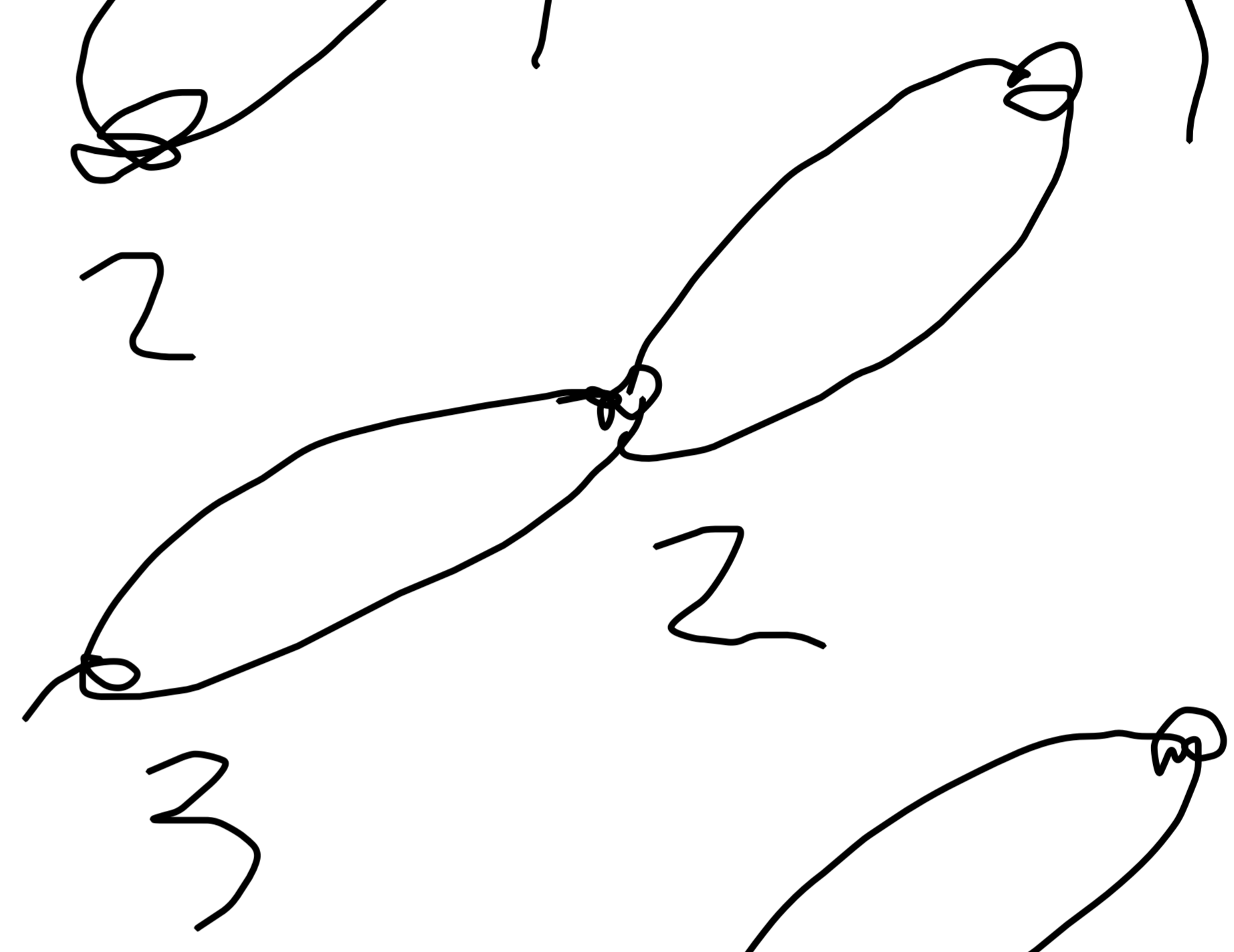
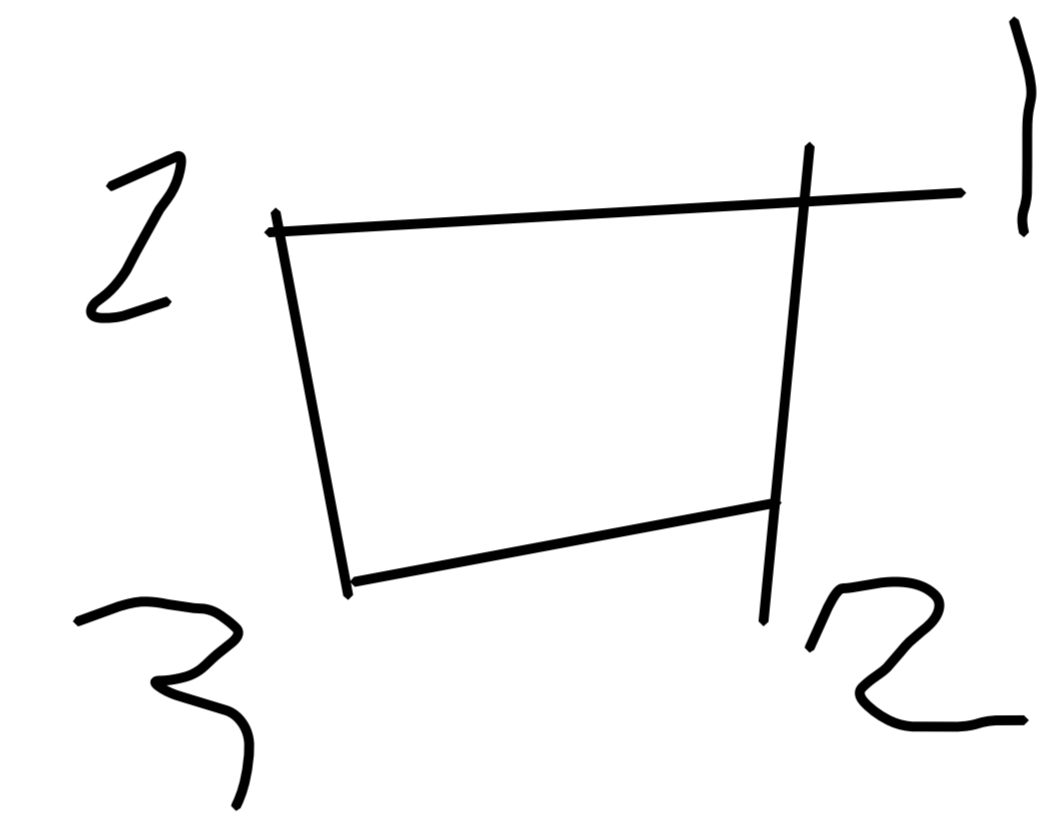
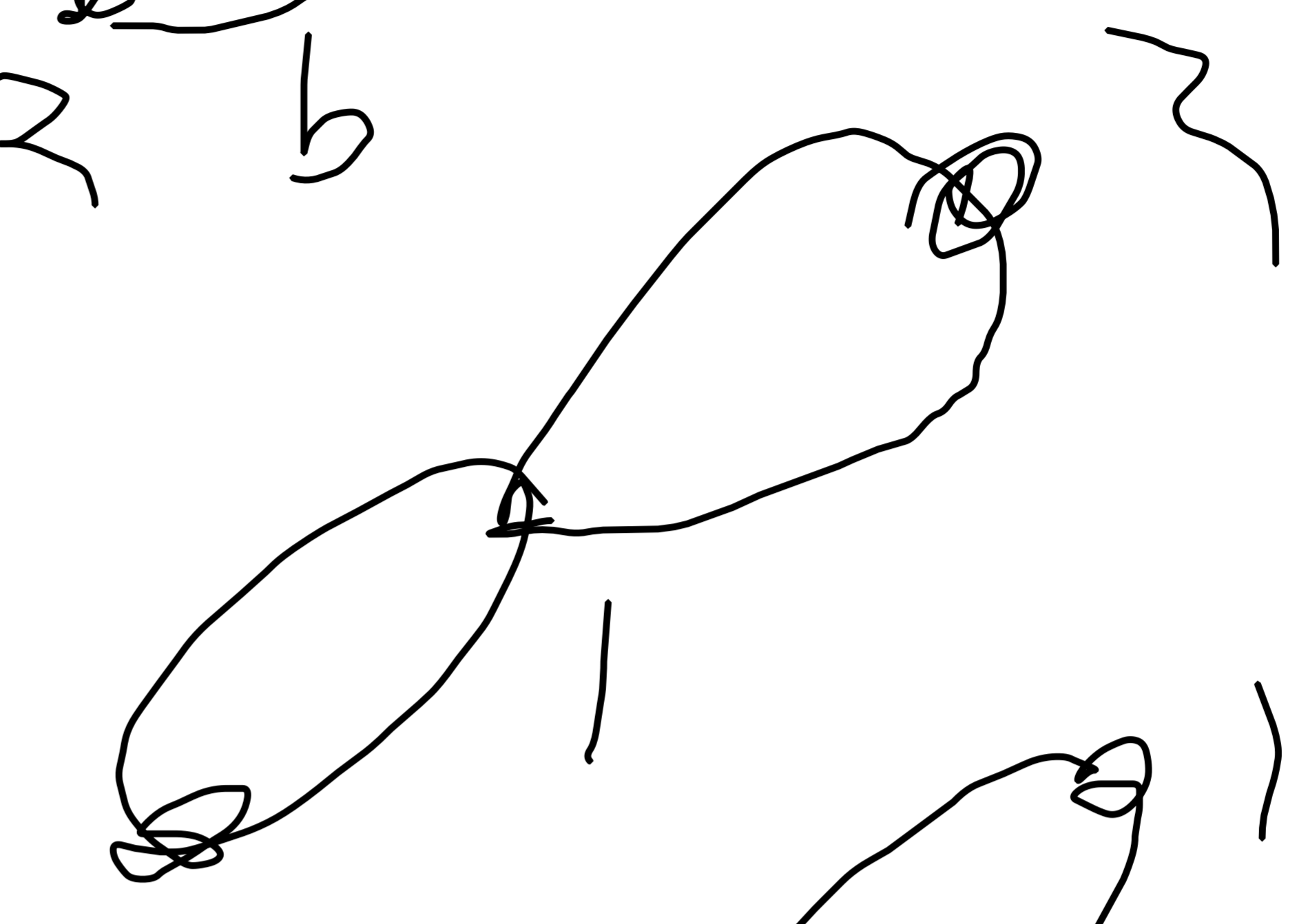
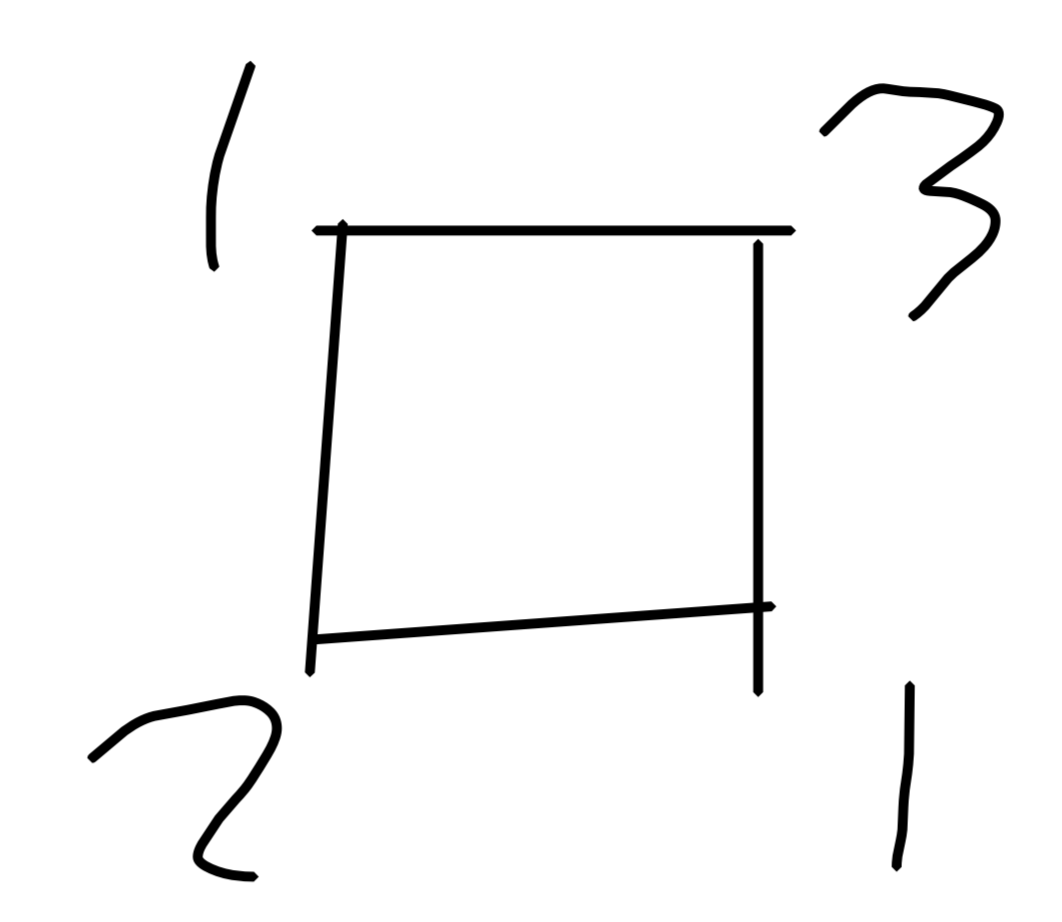
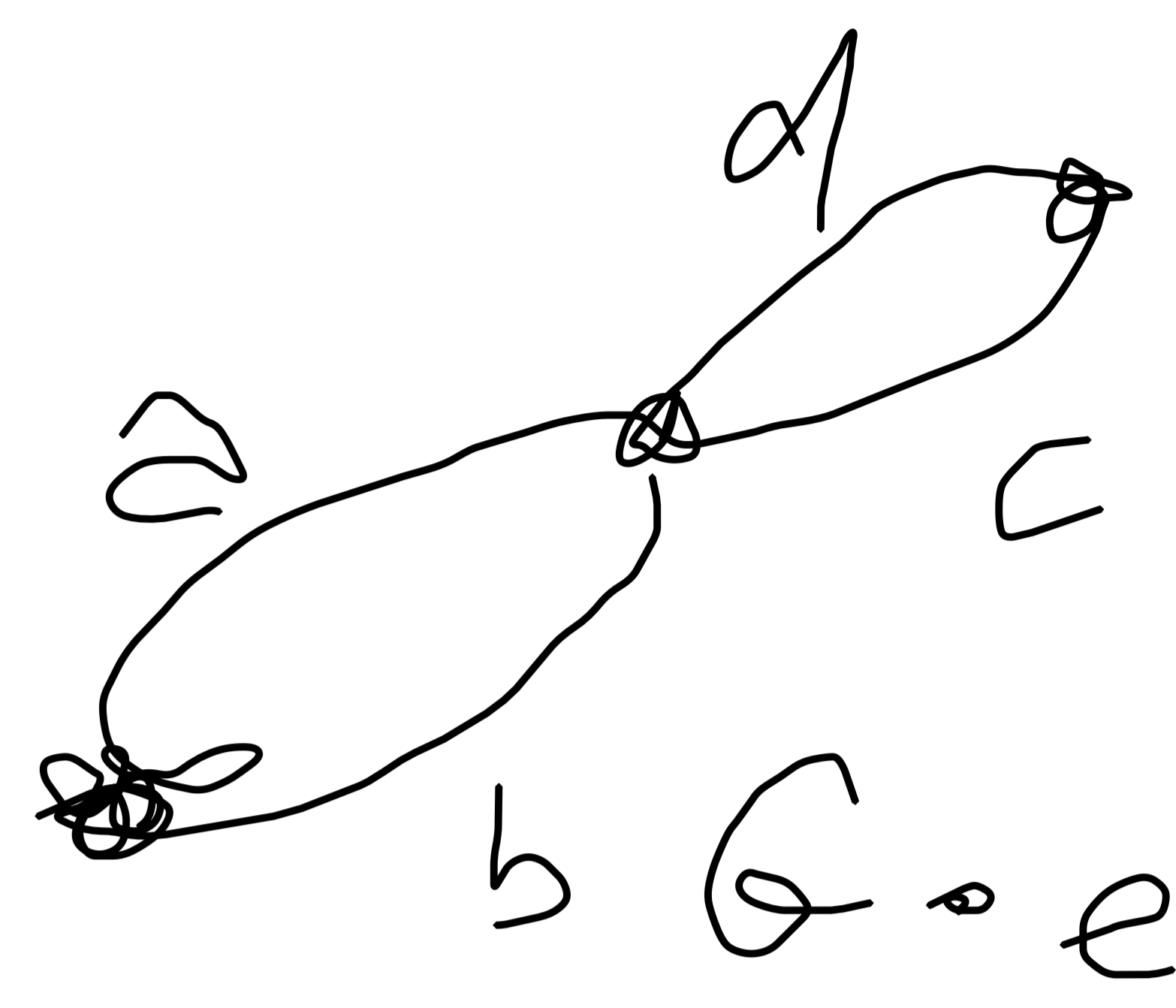
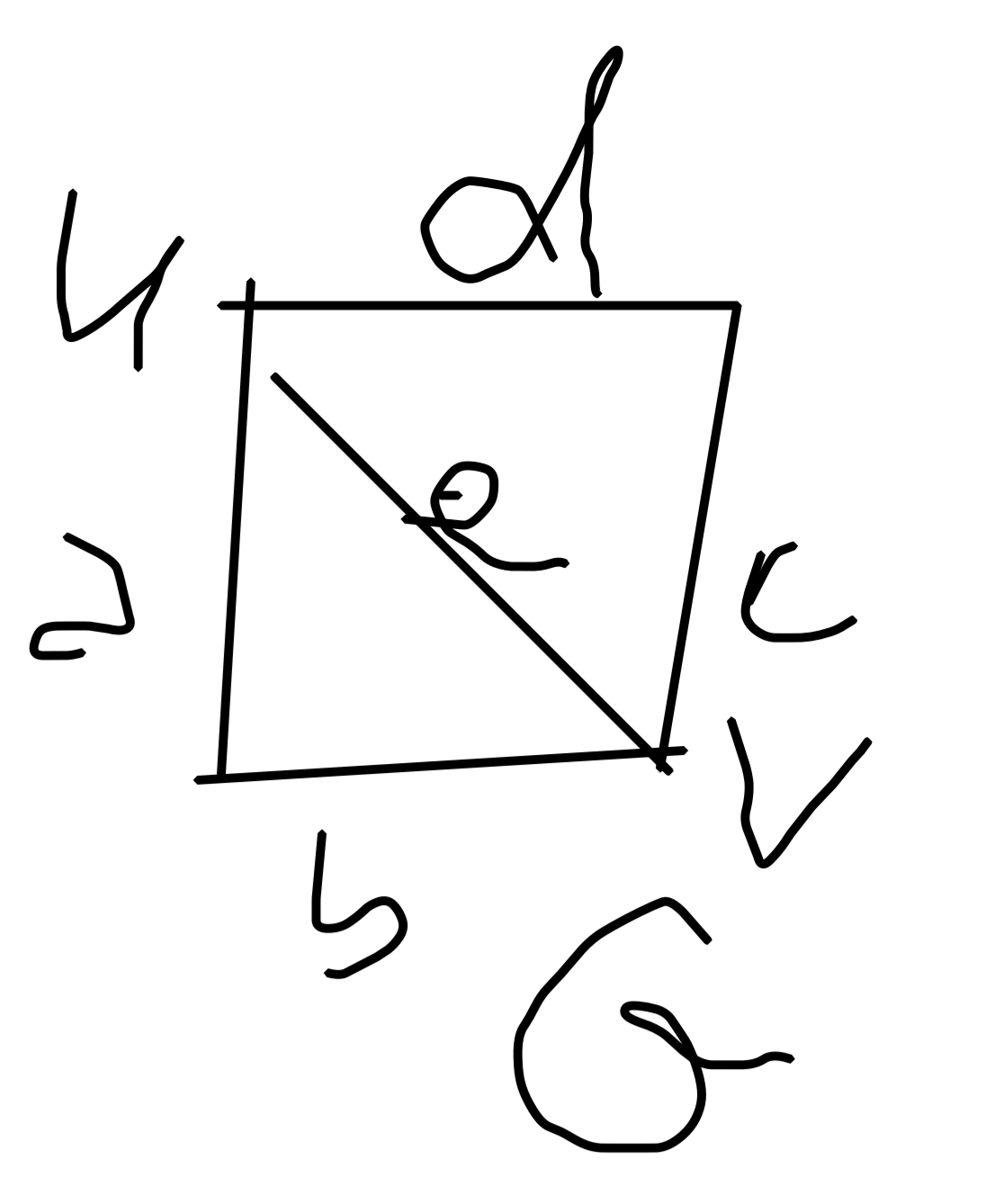
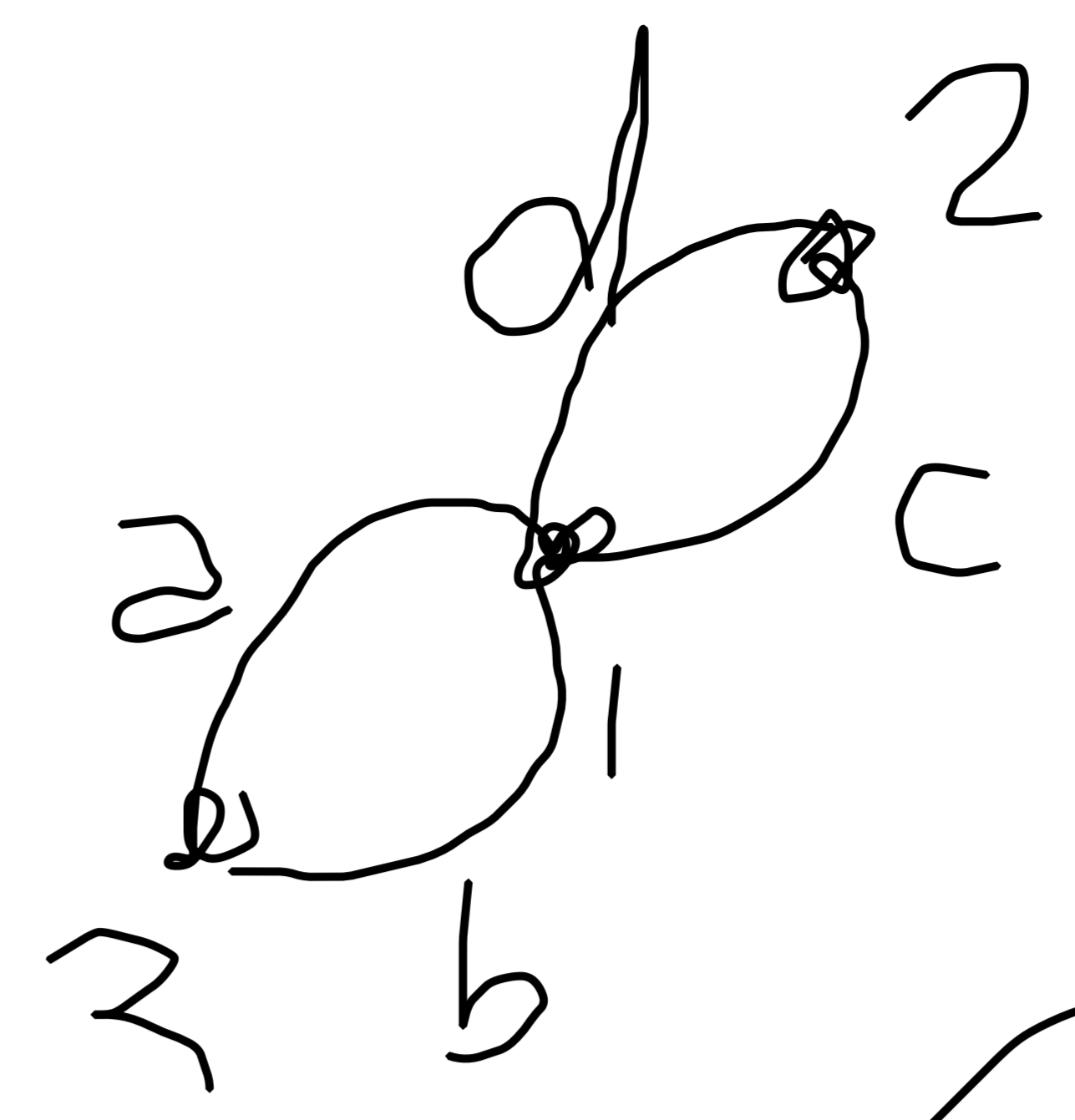
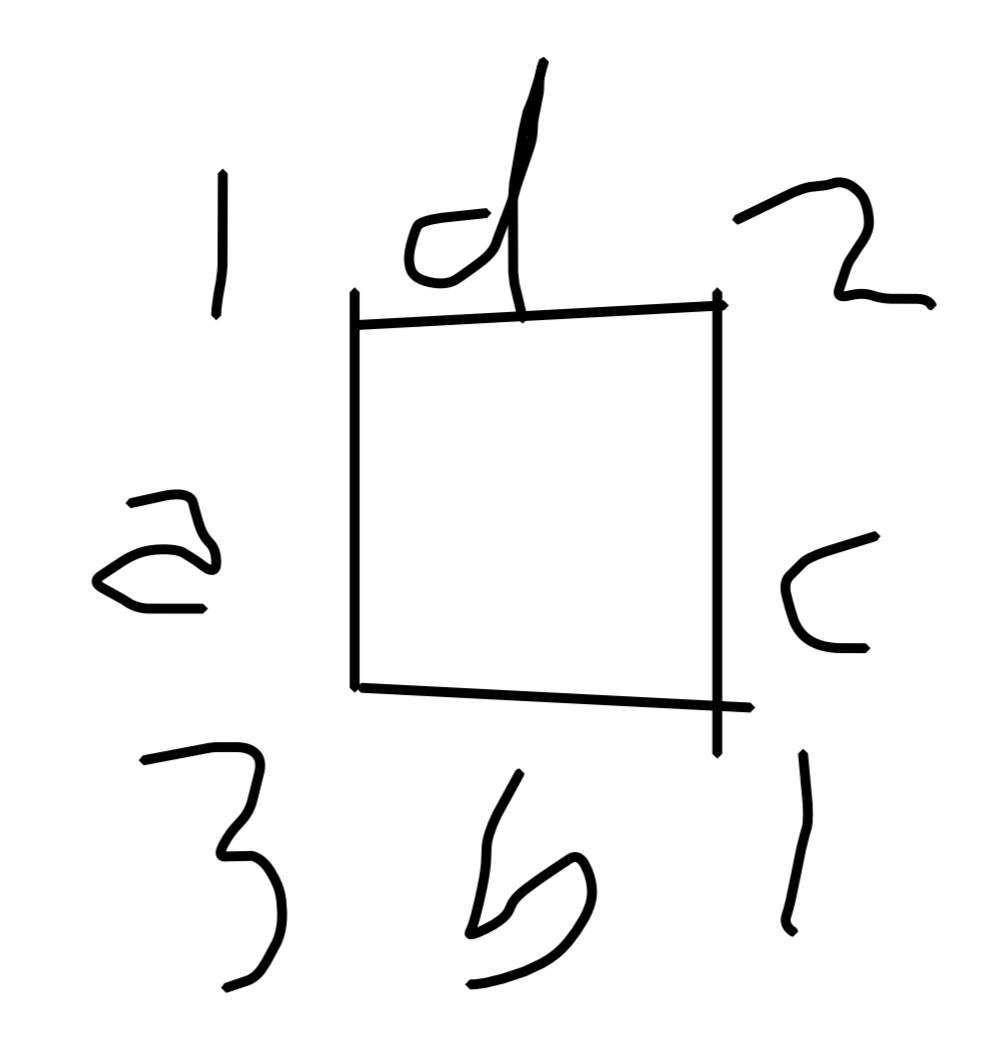




$$\pi_k(G-e) = \pi_k(G) + \pi_k(G \cdot e)$$

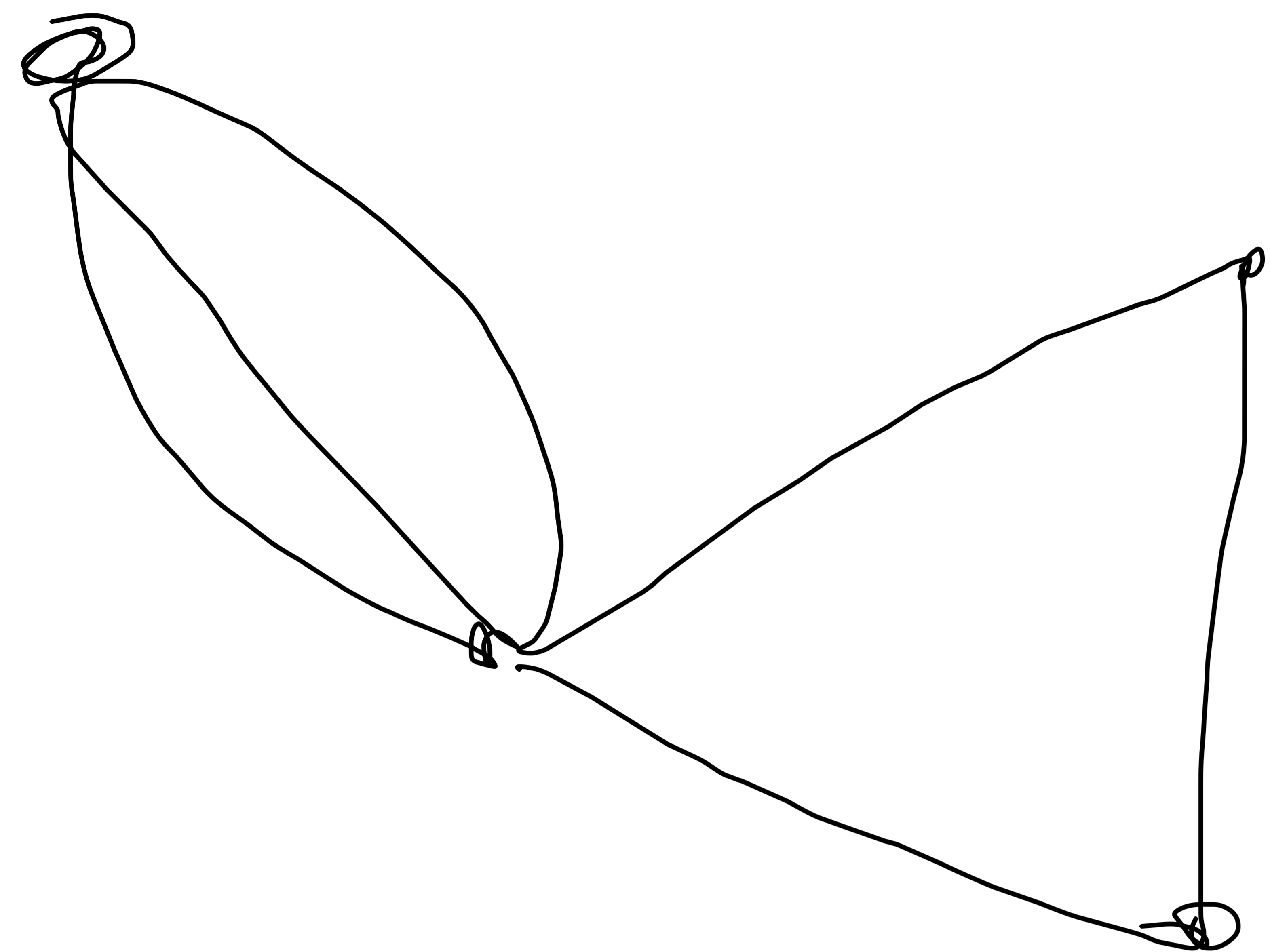


$G-e$

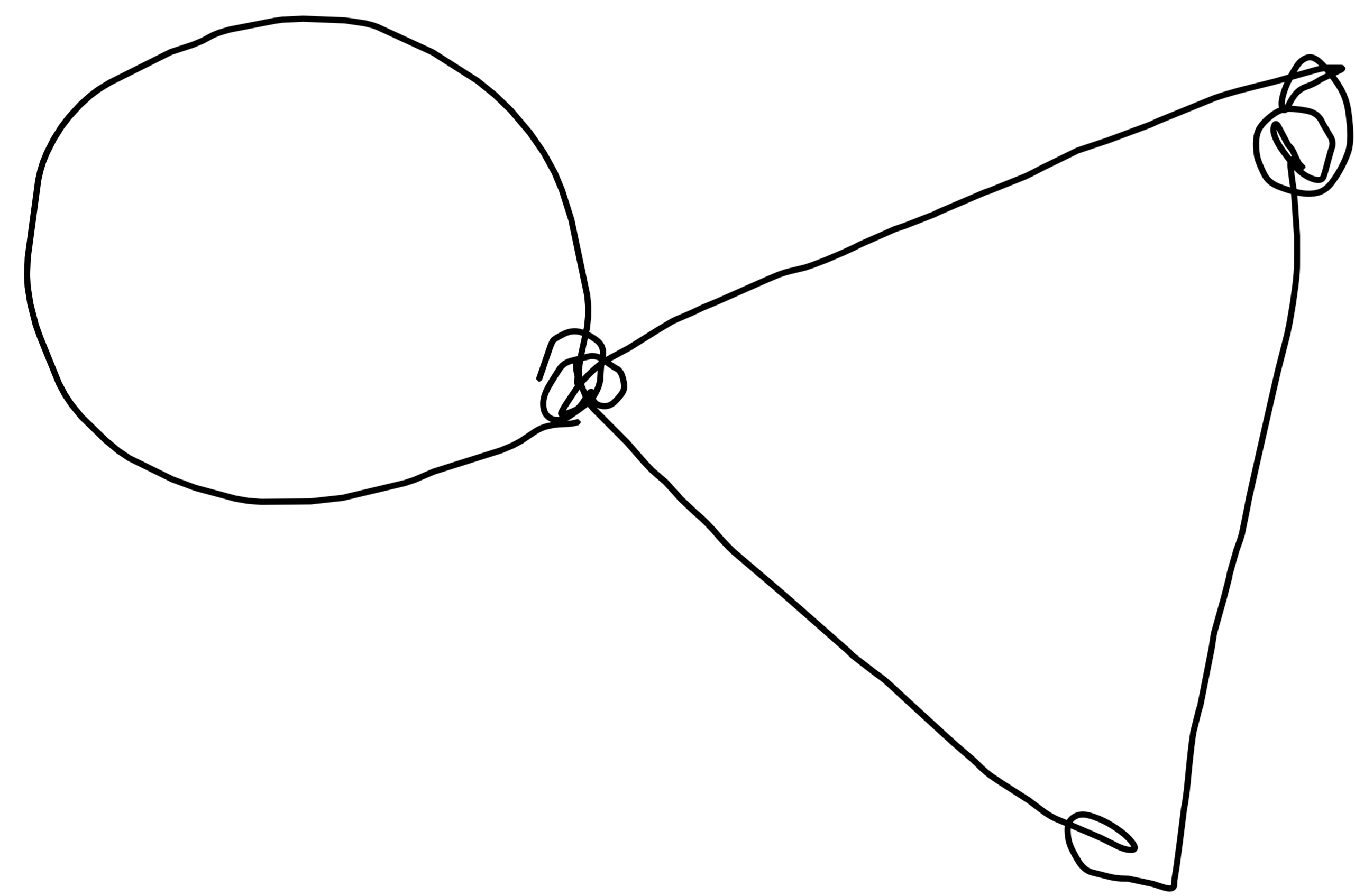
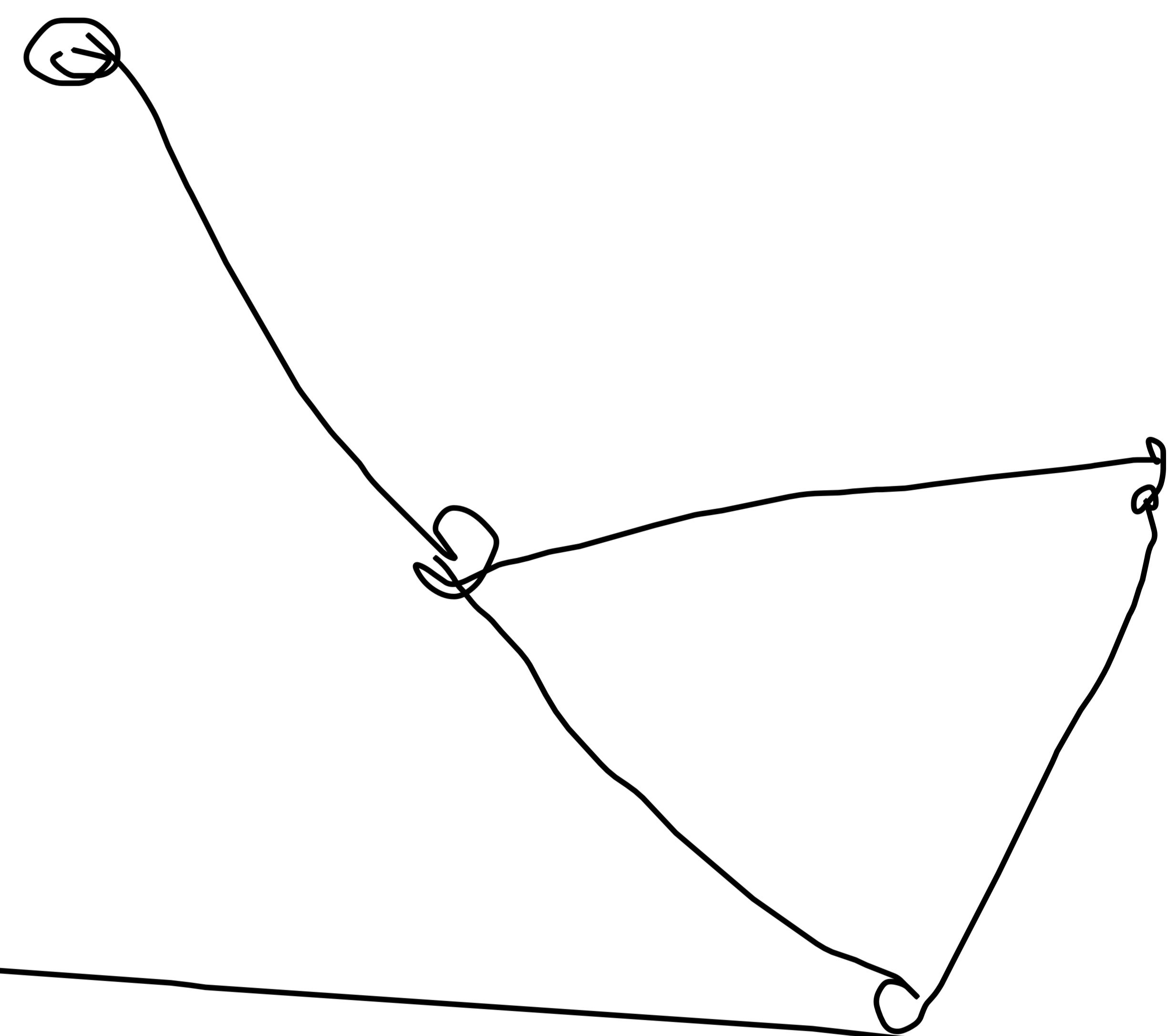




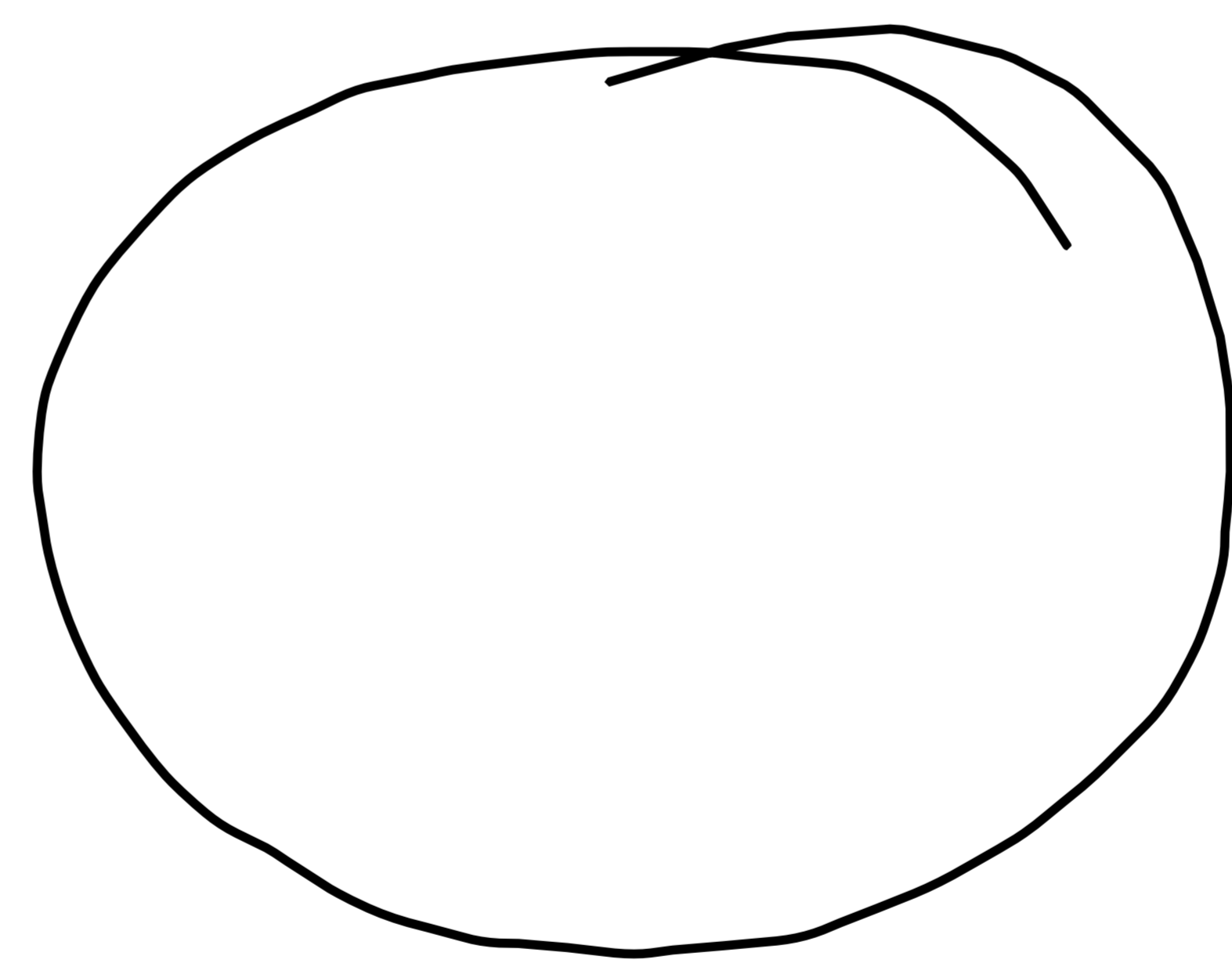
# Tricks



has same  $\pi_1$   
as



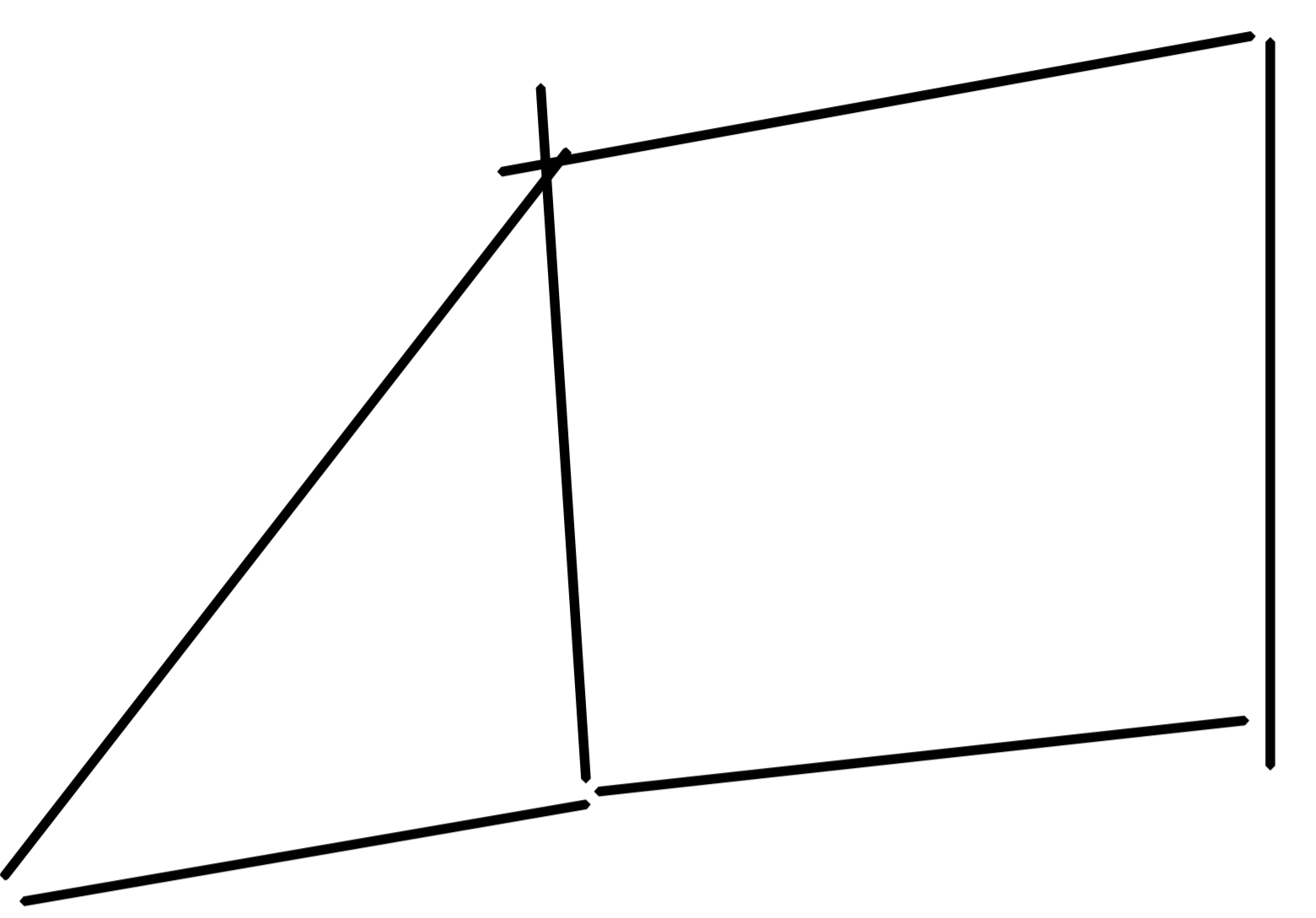
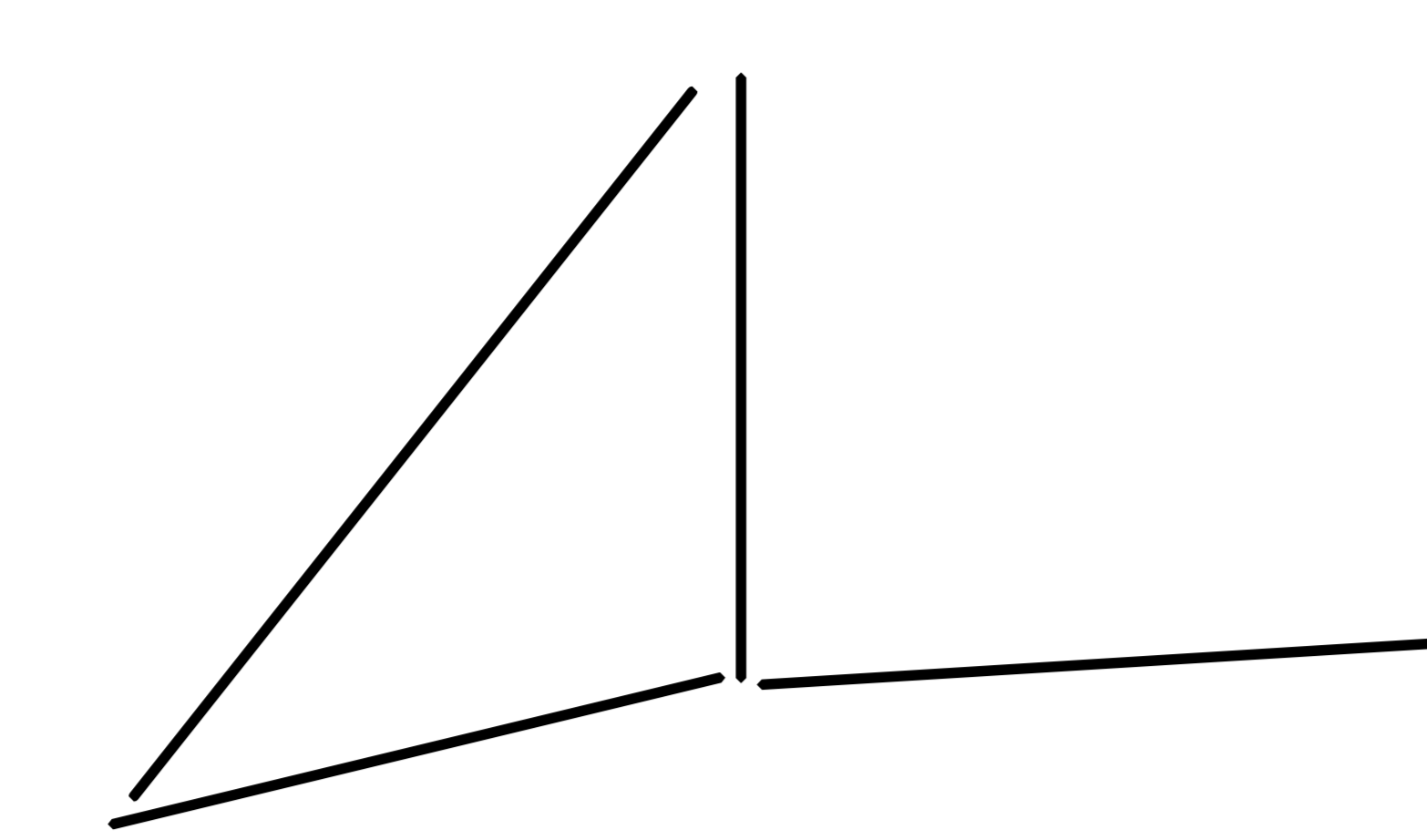
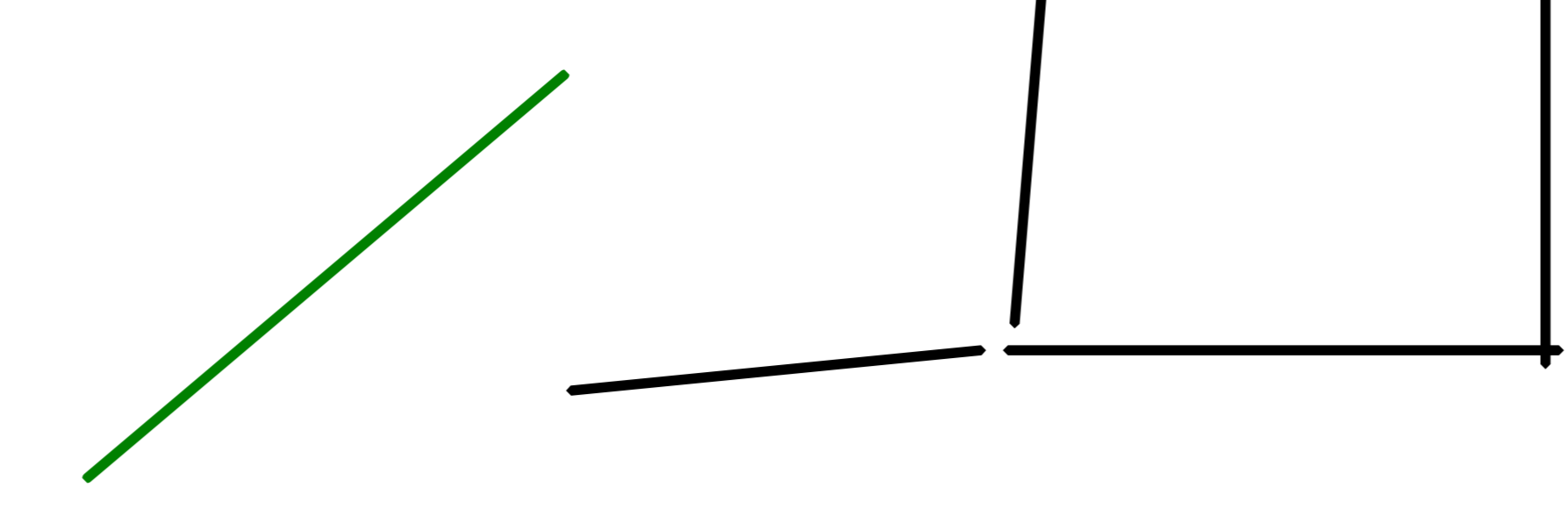
$=$

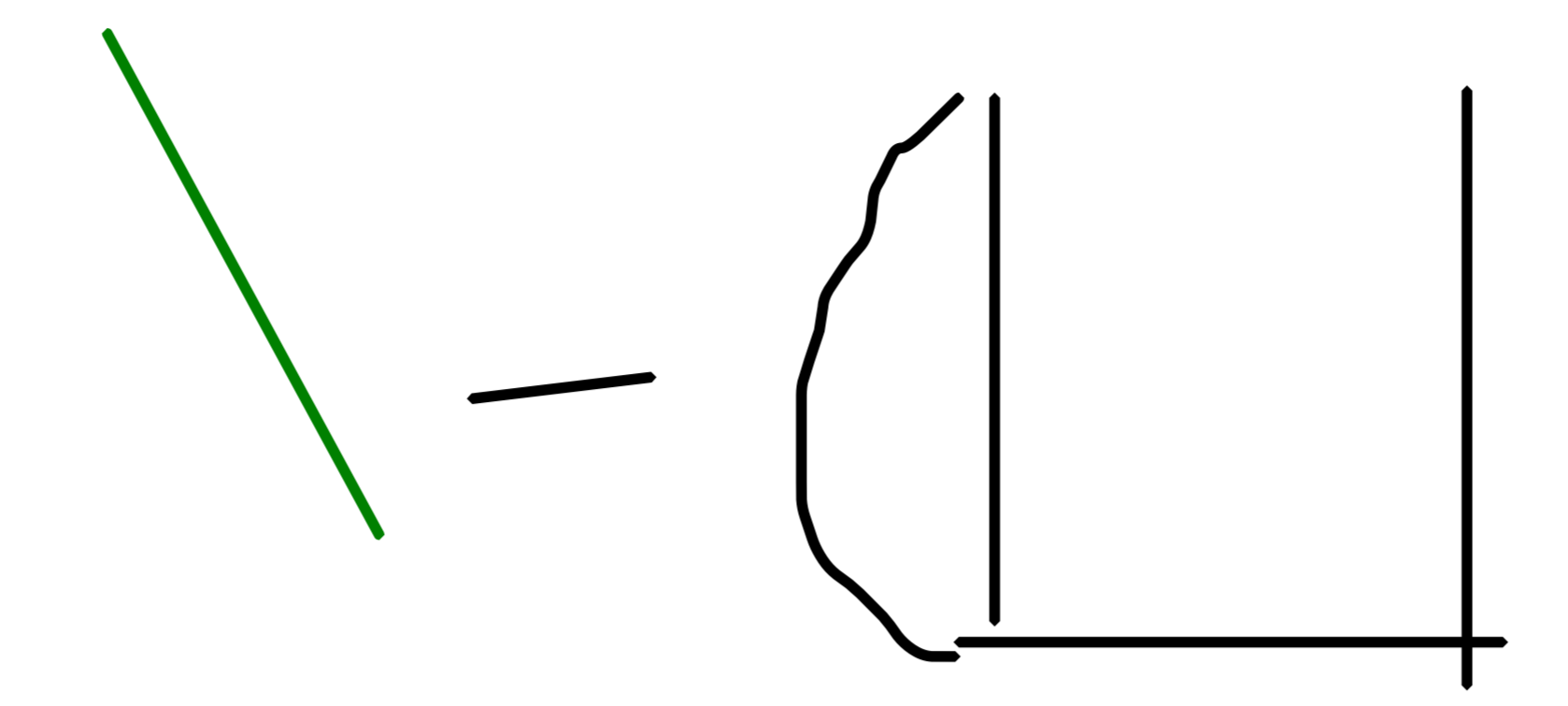
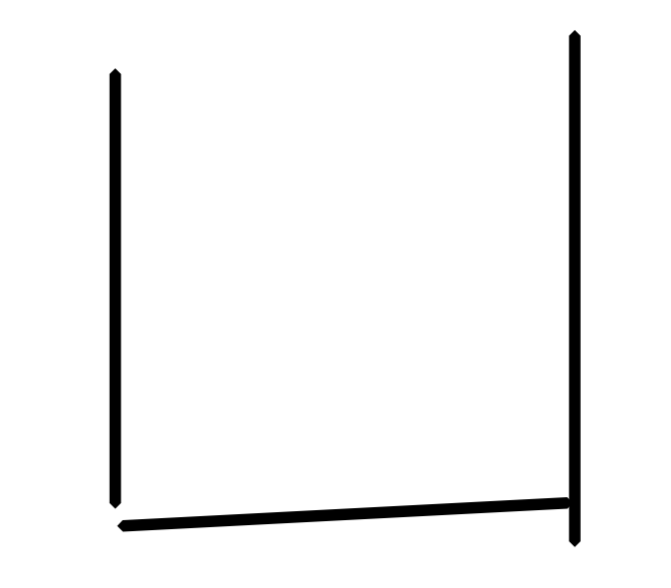


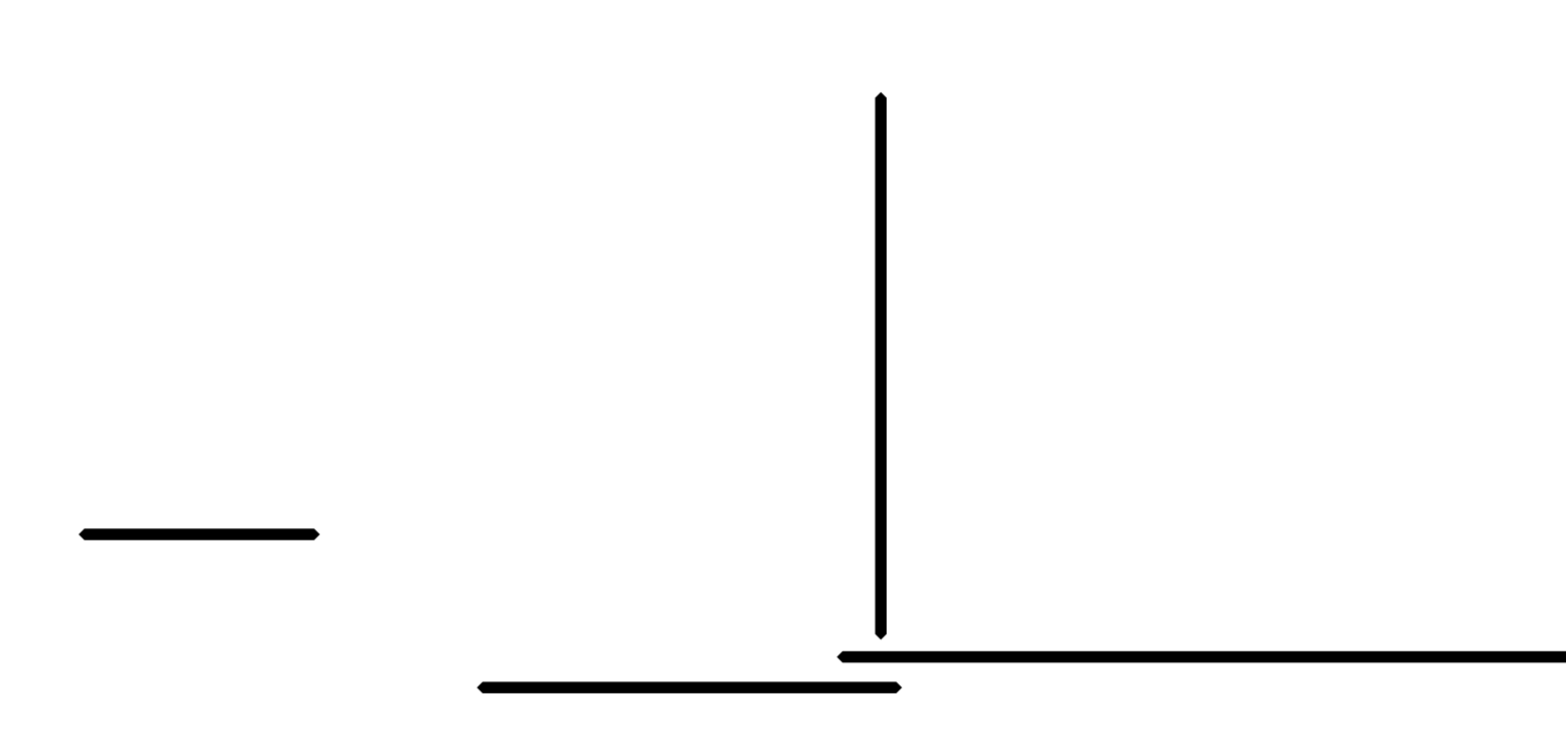
$$\pi_k \left( \text{triangle} \cup \text{square} \right) = \pi_k \left( \text{triangle} \right) \otimes \pi_k \left( \text{square} \right)$$

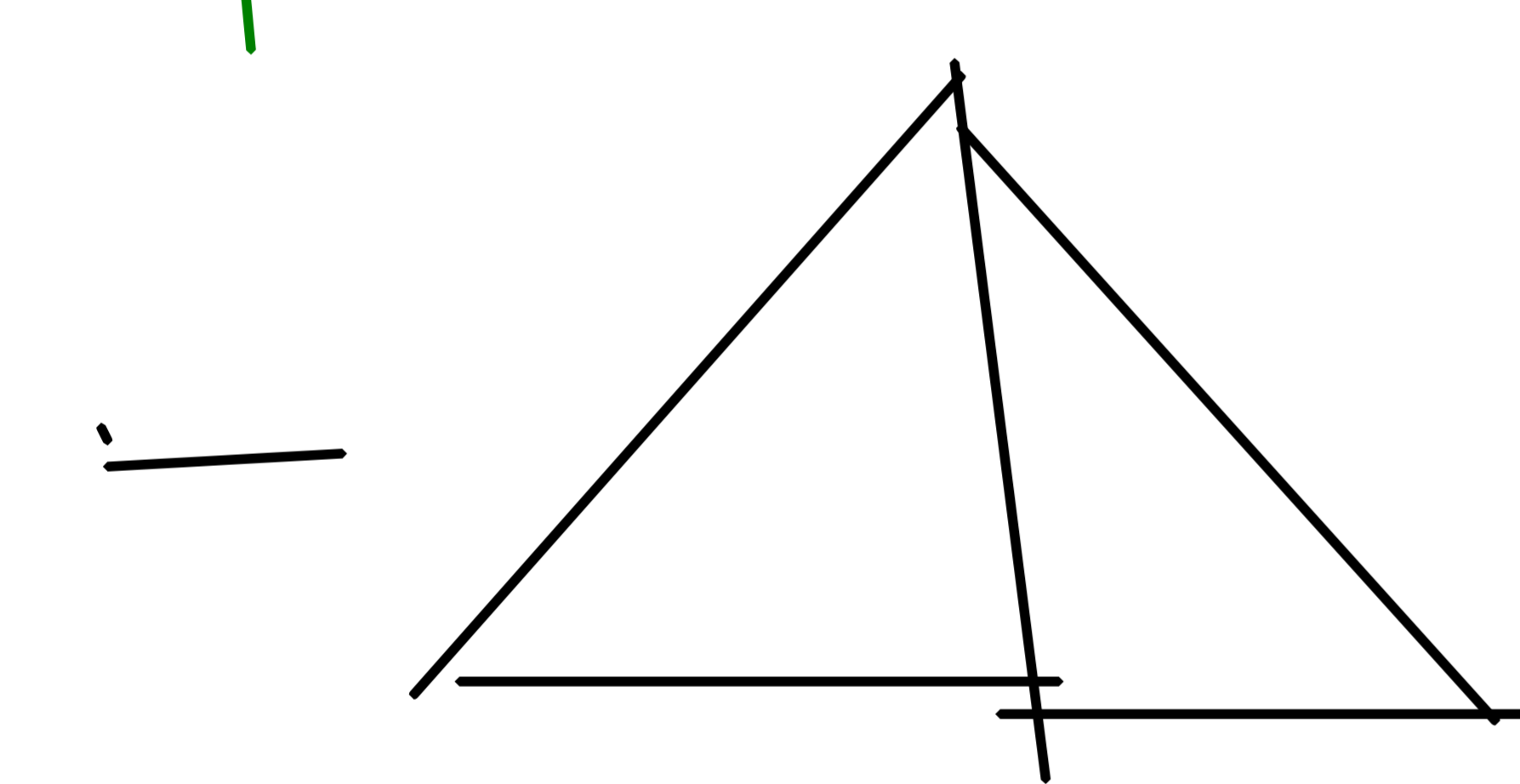
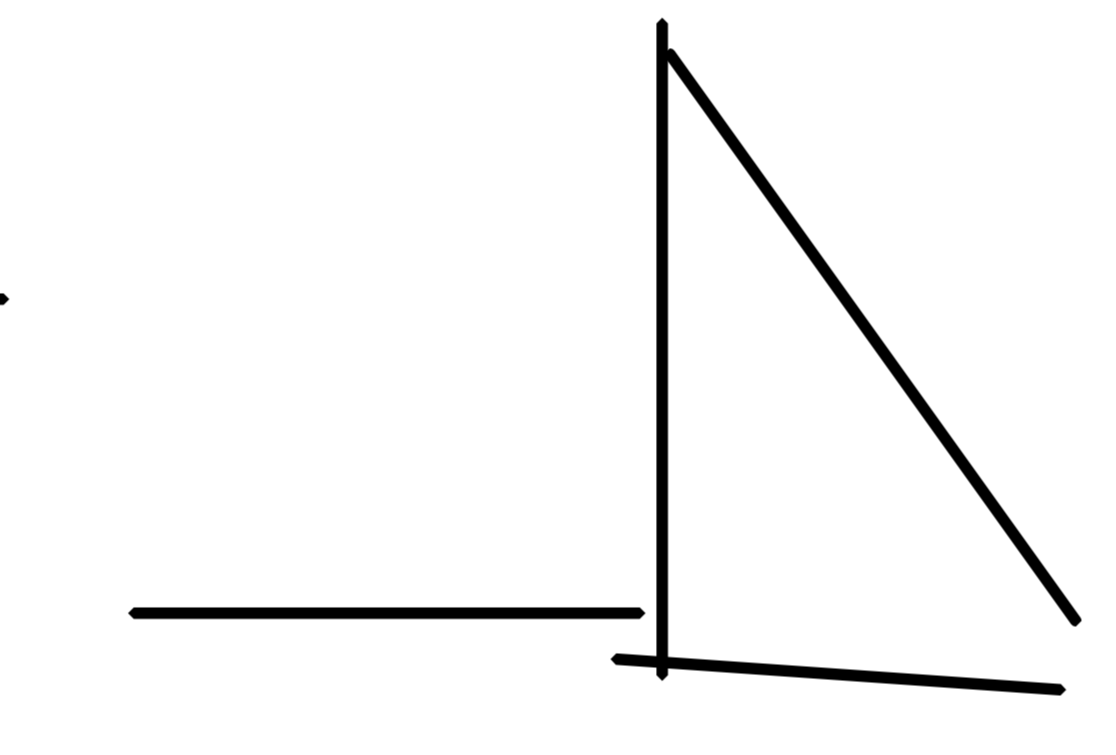
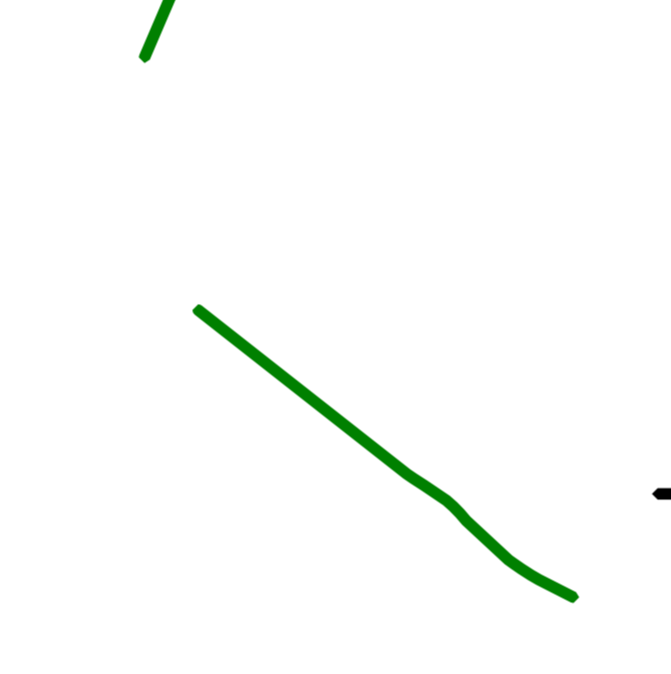
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$$\pi_k \left( \text{triangle} \cup \text{square} \right) = \frac{\pi_k \left( \text{triangle} \right) \otimes \pi_k \left( \text{square} \right)}{k}$$

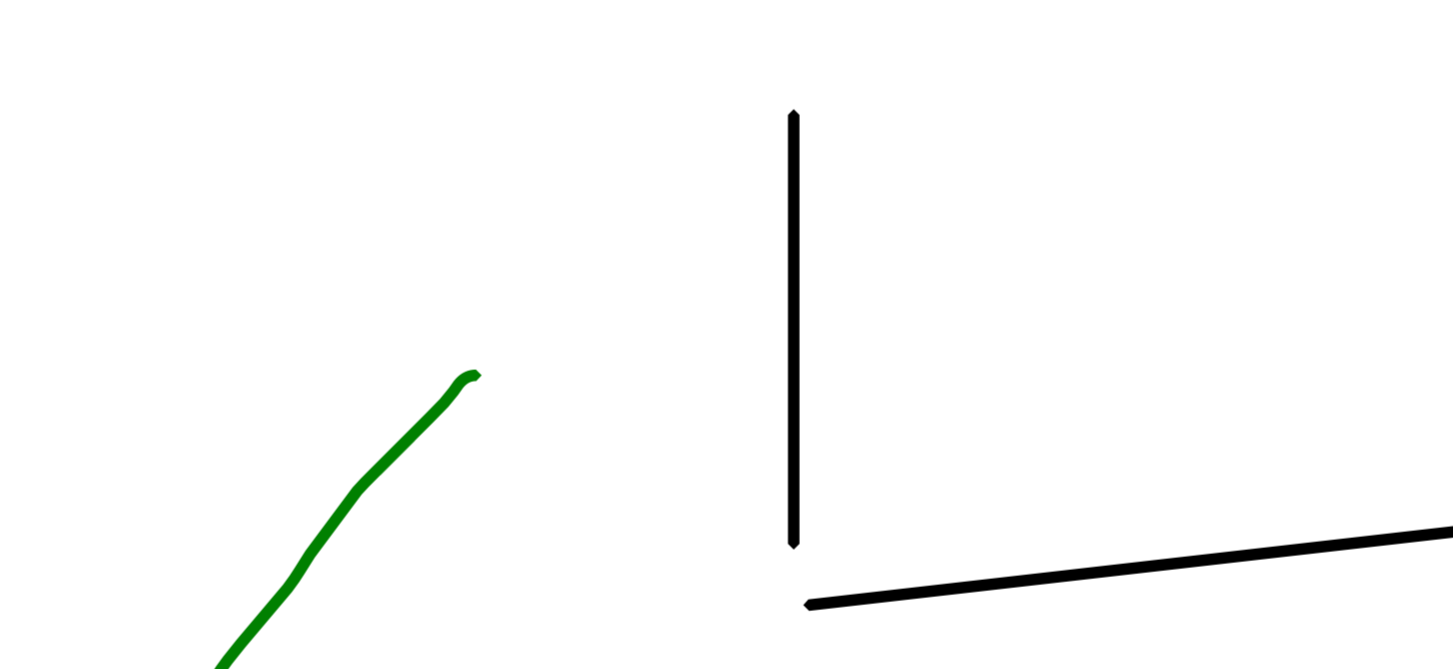



 $= k(k-1)^4$

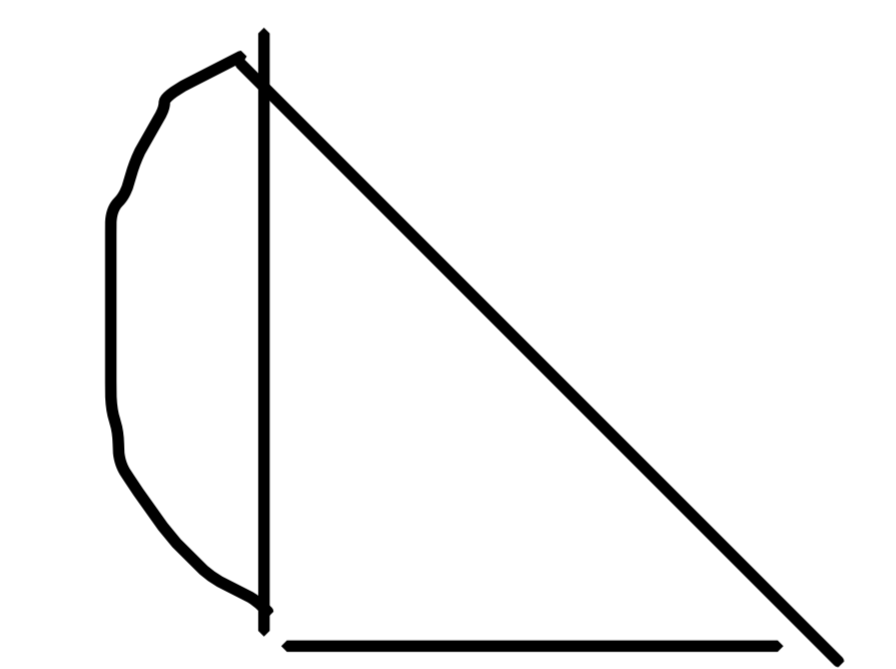
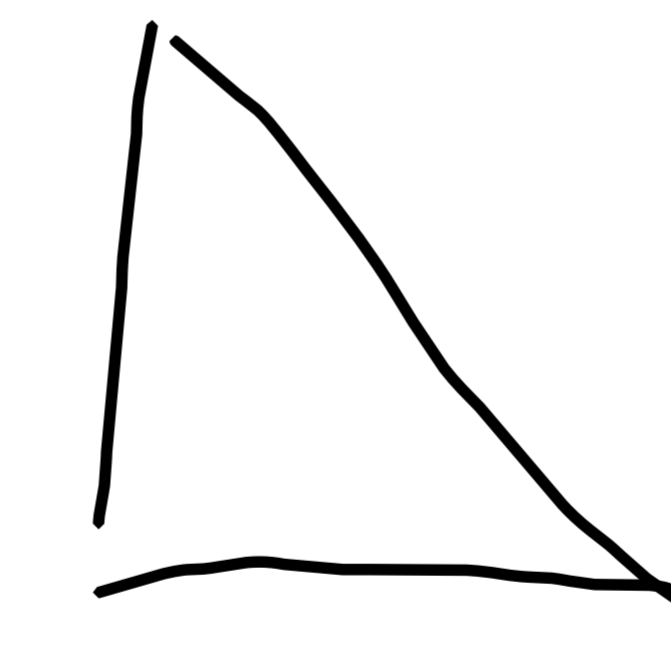

 $-$ 

 $= -k(k-1)^3$


 $= -k(k-1)^3$


 $-$ 

 $-$ 

 $+ \text{---}$ 
 $= k(k-1)^2$


 $+ \text{---}$ 
 $= k(k-1)^2$

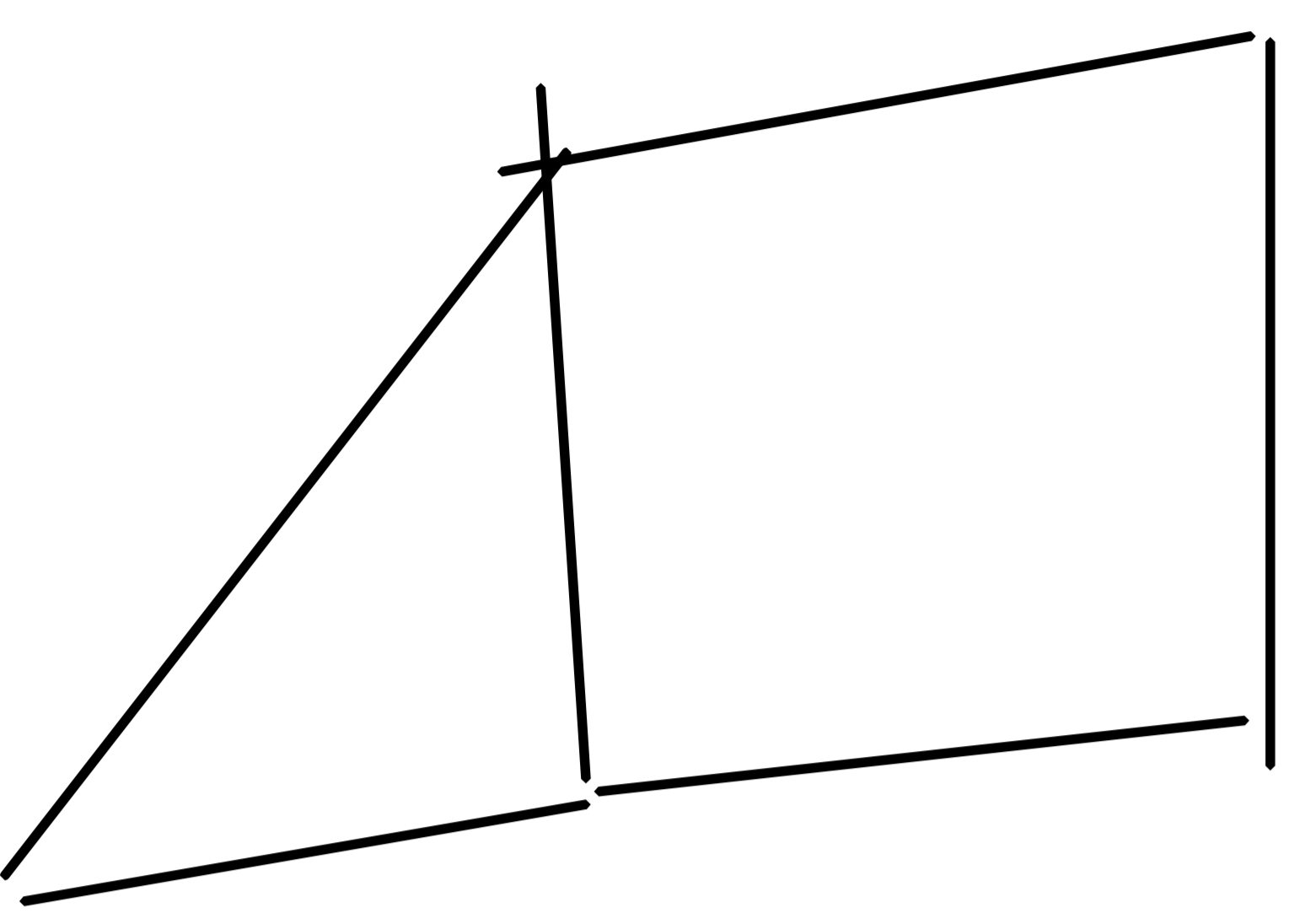
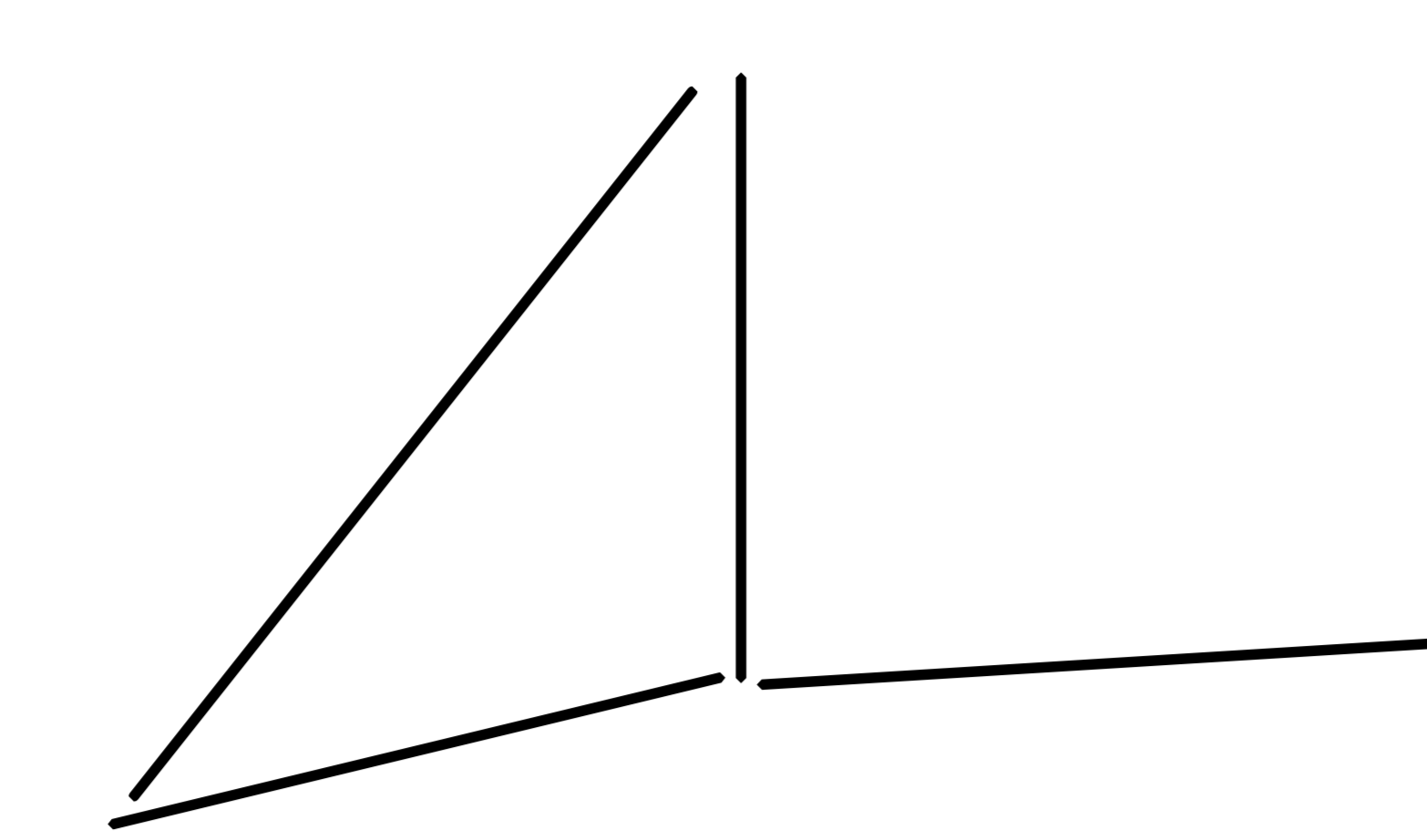
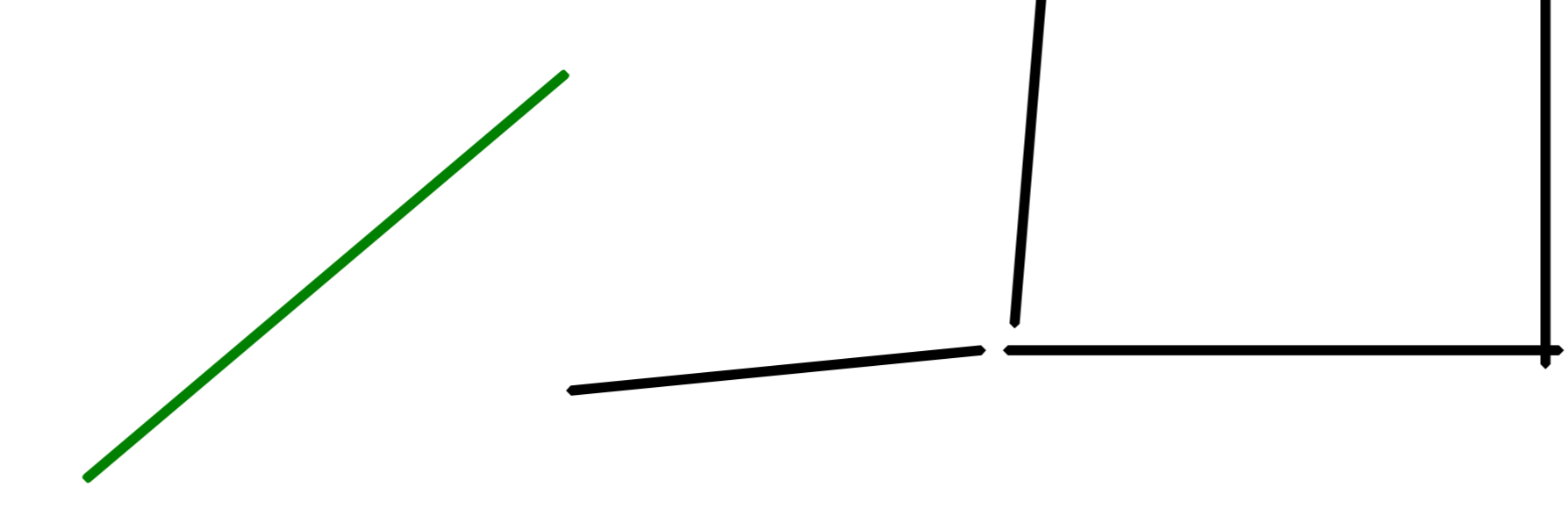

 $= k(k-1)^2$

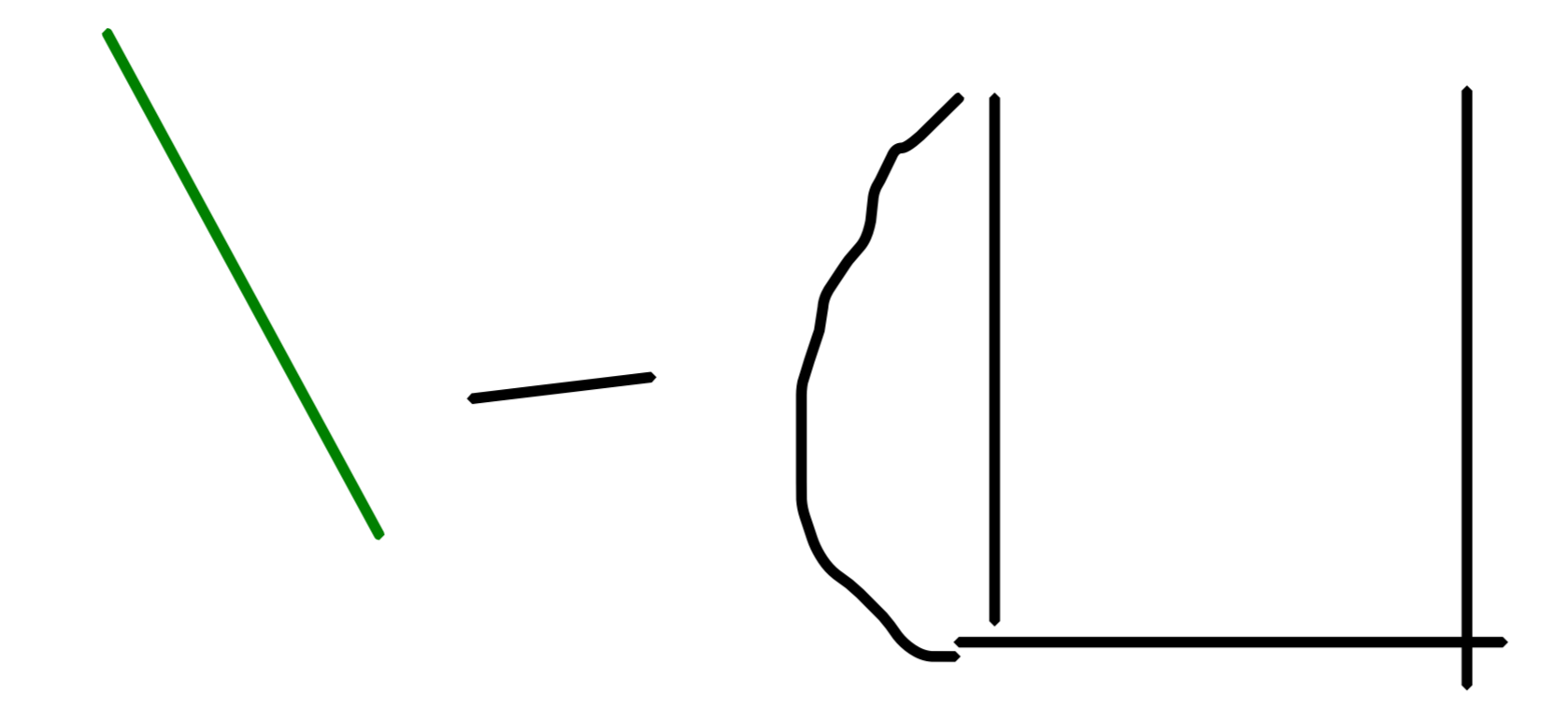
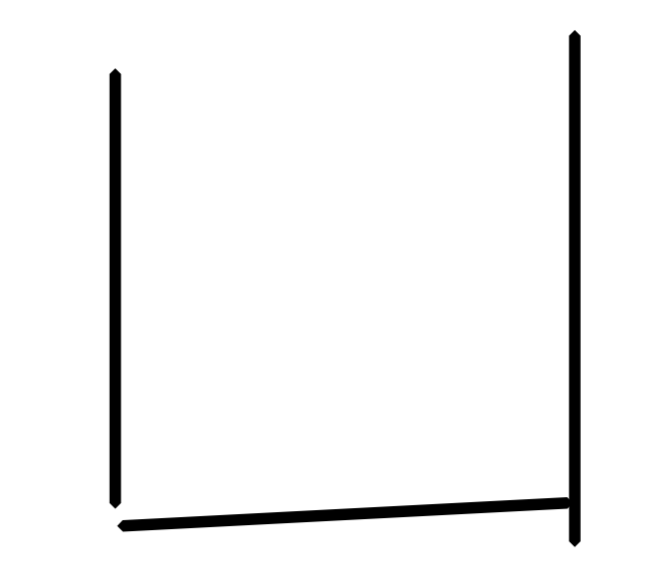

 $=$ 

 $- \text{---}$ 
 $= -k(k-1)$

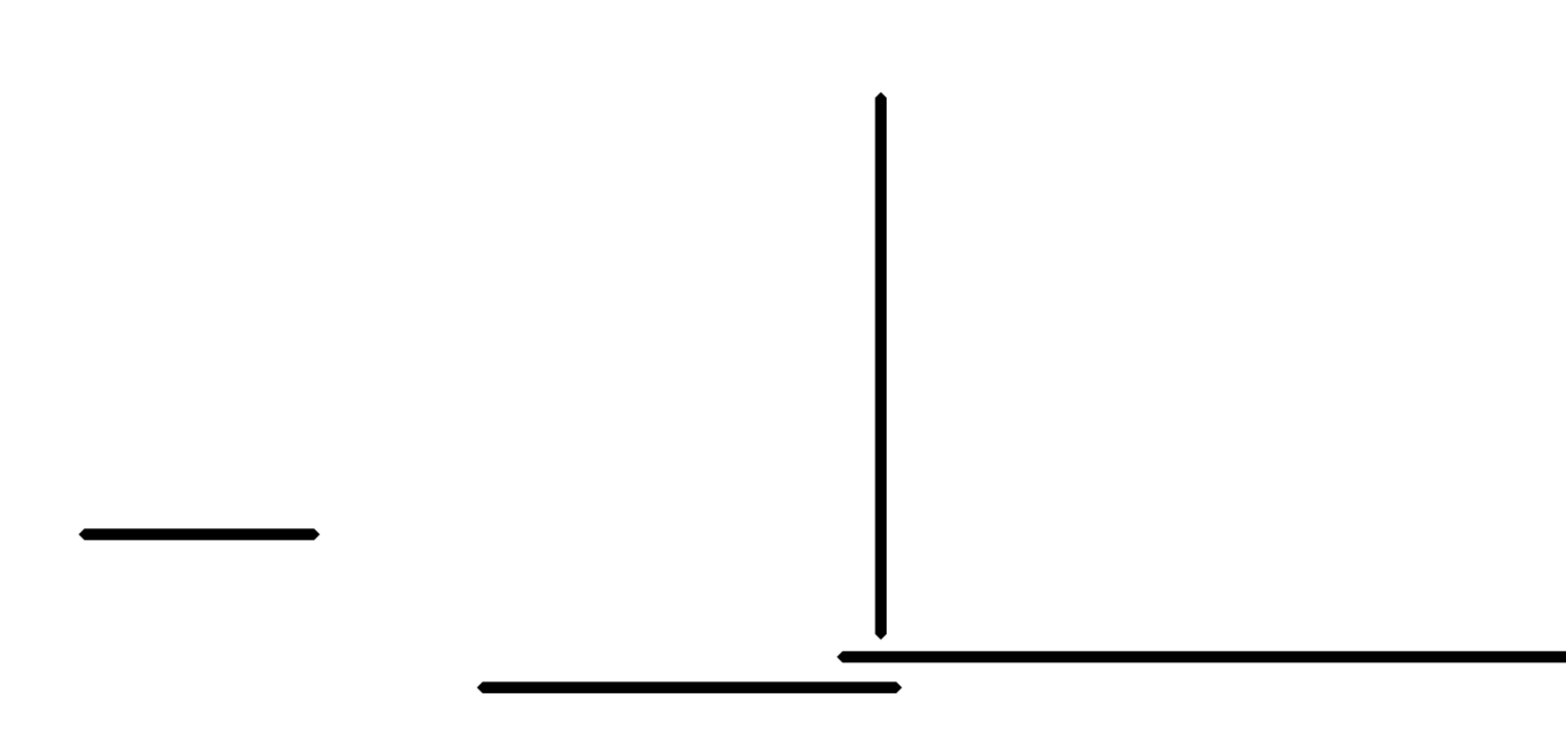
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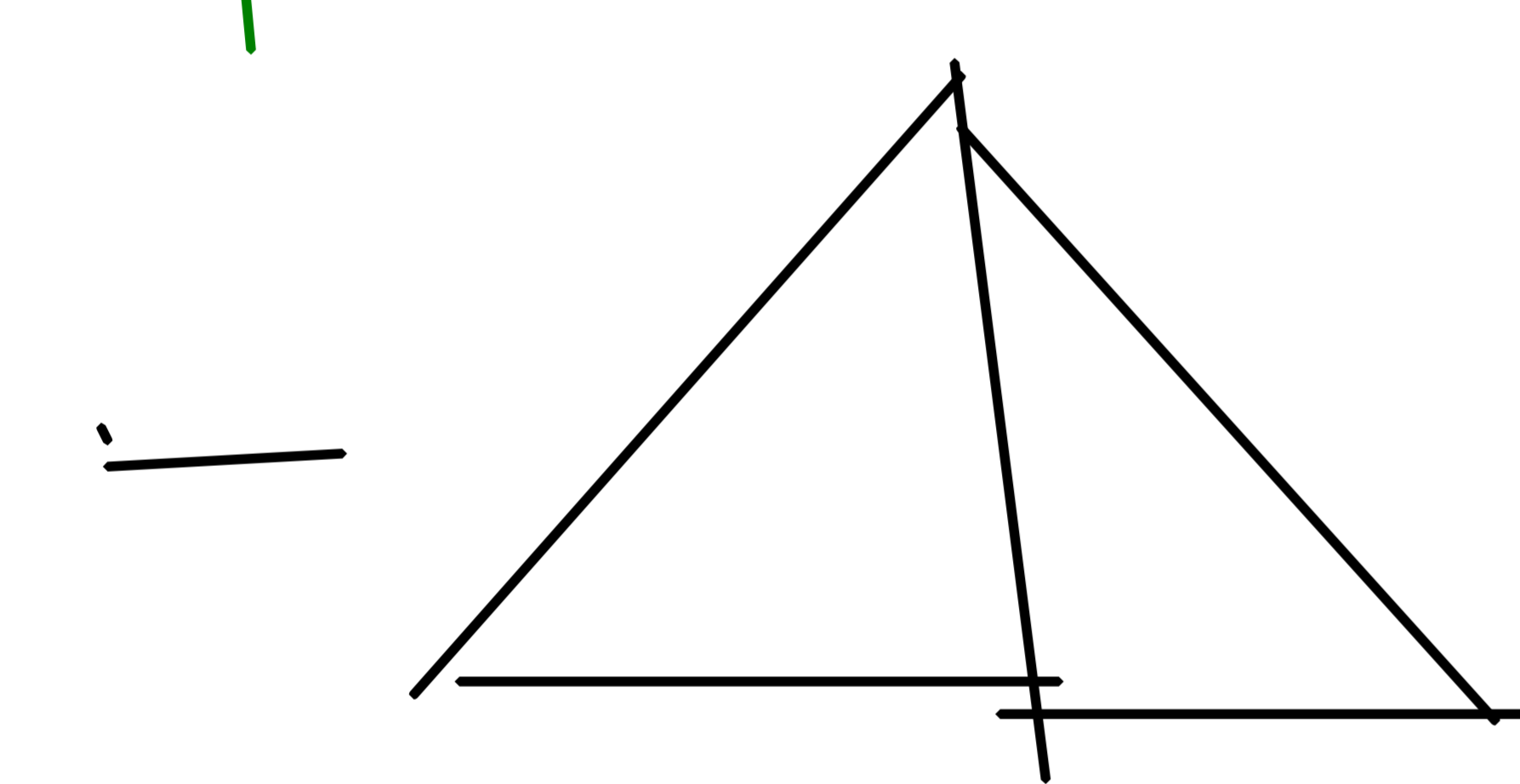
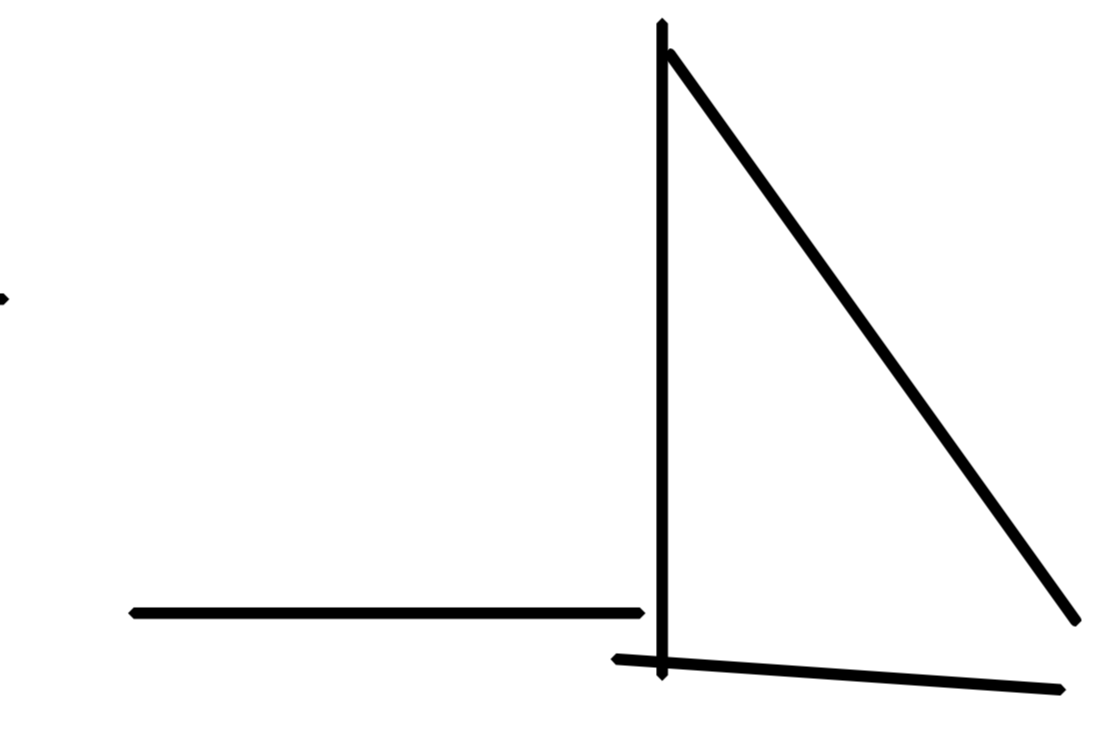
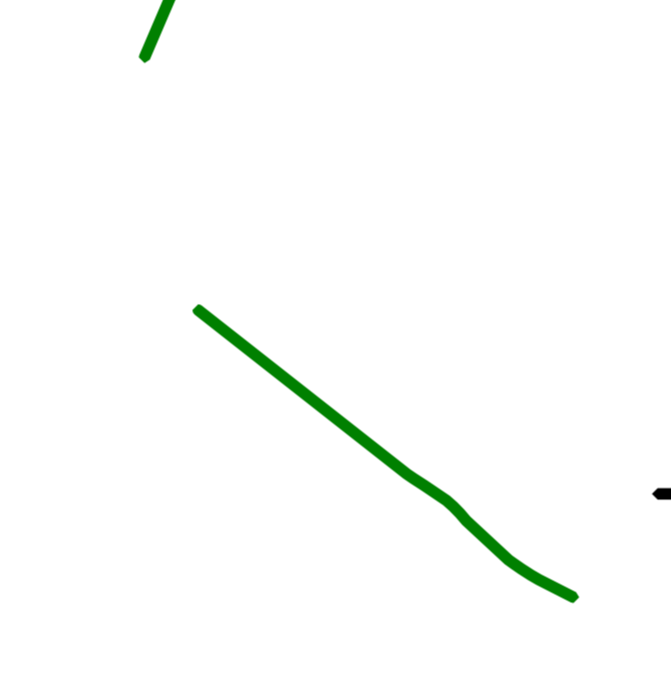
$k(k-1)^4 - 2k(k-1)^3 + 2k(k-1)^2 - k(k-1)$

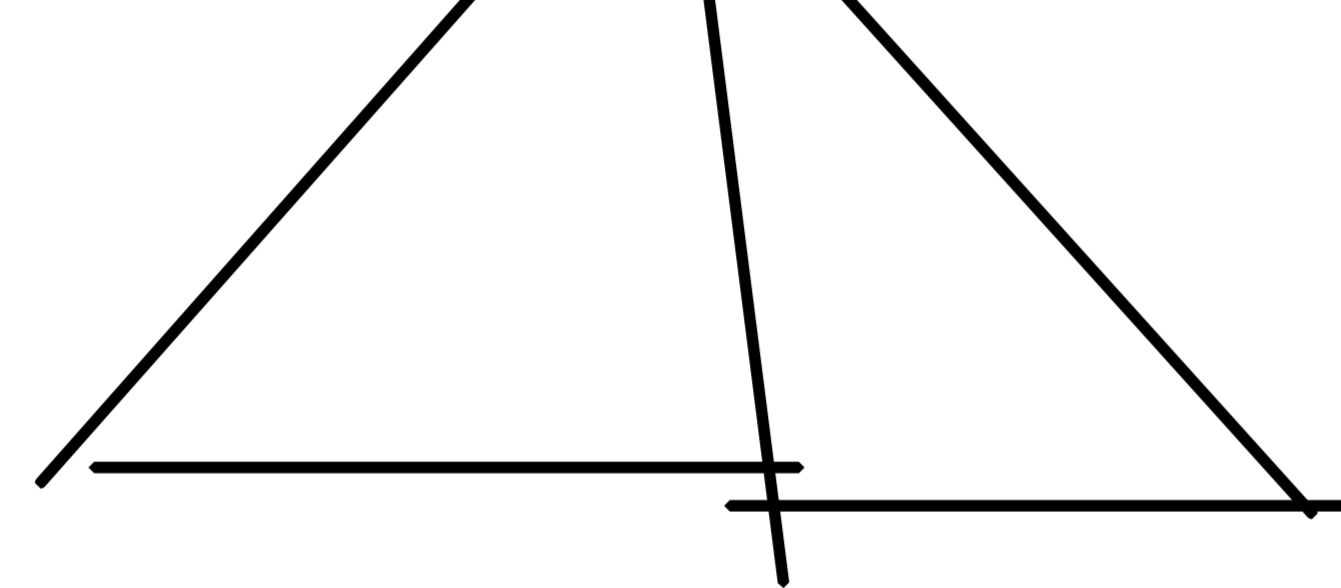
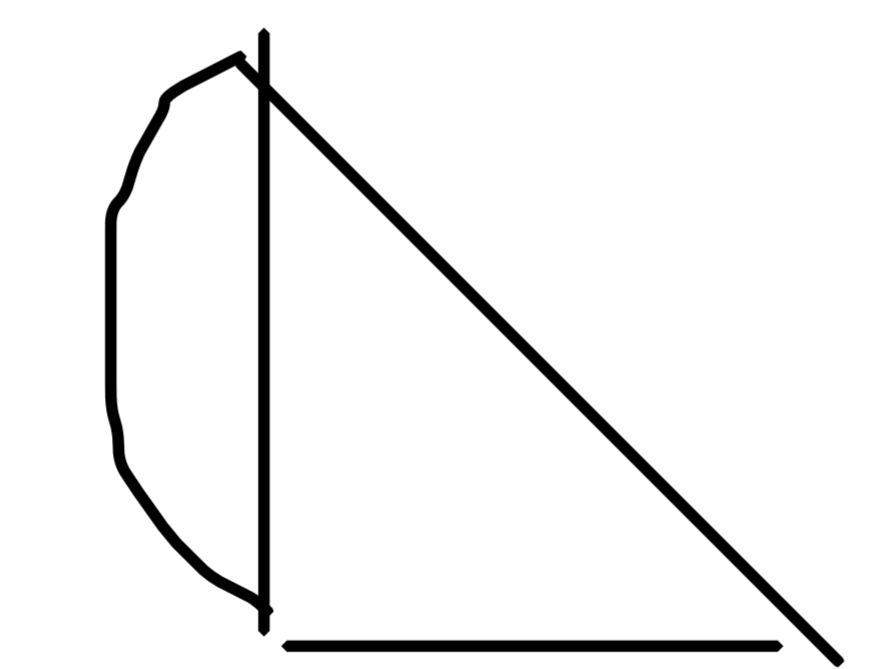
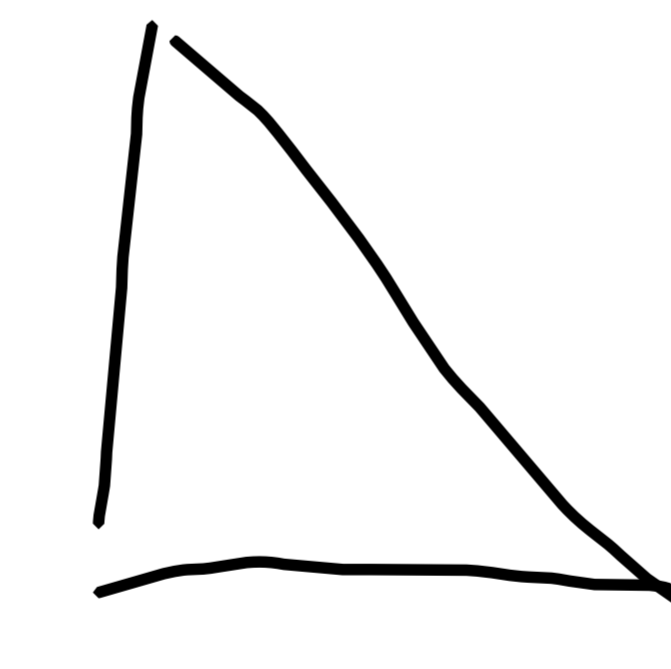


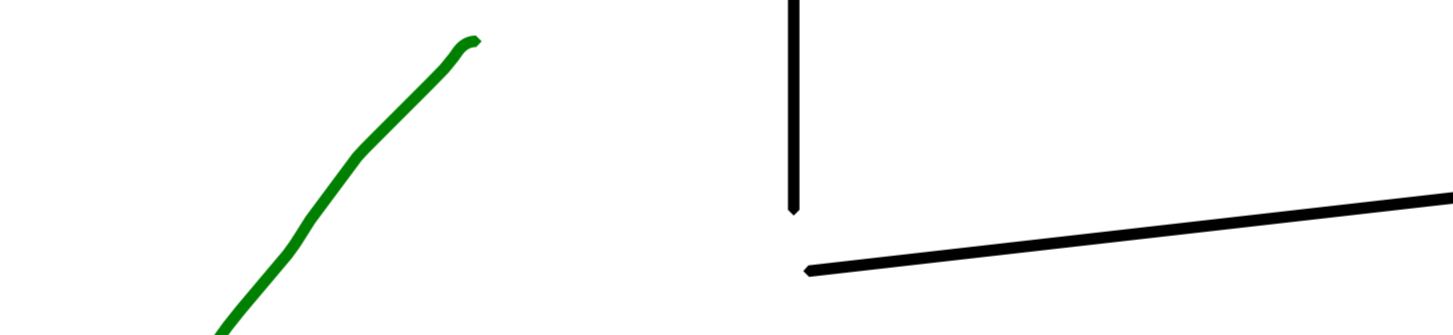
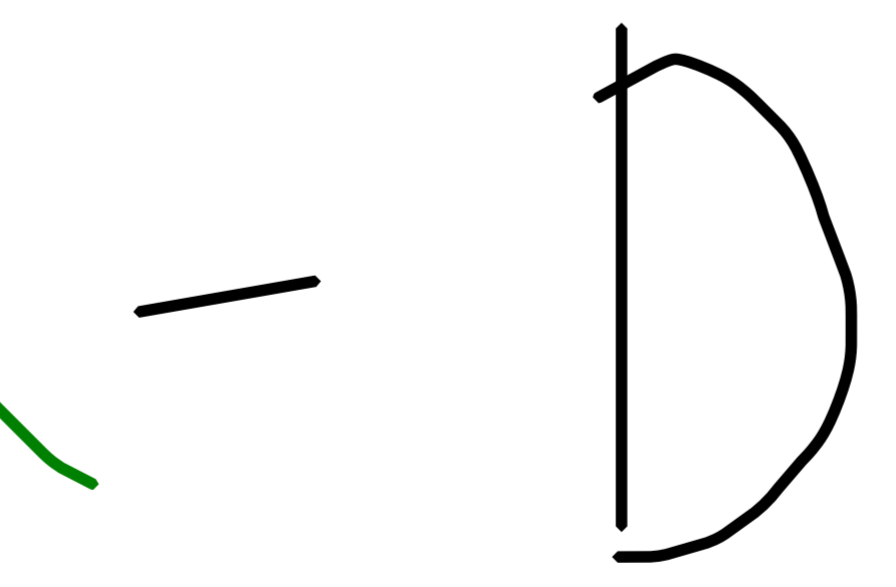



 $= k(k-1)^4$


 $-$ 

 $= -k(k-1)^3$


 $= -k(k-1)^3$



 $-$ 

 $= +k(k-1)^2$



 $=$ 

 $= k(k-1)^2$


 $-$ 

 $= -k(k-1)$

---

$k(k-1)^4 - 2k(k-1)^3 + 2k(k-1)^2 - k(k-1)$



1 1  
 1 2 1  
 1 3 3 1  
 1 4 6 4 1

$$\frac{k(k-1)^4 - 2k(k-1)^3 + 2k(k-1)^2 - k(k-1)}{k^5 - 4k^4 + 6k^3 - 4k^2 + k}$$

$$k^5 - 4k^4 + 6k^3 - 4k^2 + k$$

$$- 2k^4 + 6k^3 - 6k^2 + 2k$$

$$+ 2k^3 - 4k^2 + 2k$$

$$- k^2 + k$$

---


$$k^5 - 6k^4 + 14k^3 - 15k^2 + 6k$$

$$u \vee v = u \vee v$$

$$u + uv = u$$

| $u$ | $v$ | $uv$ | $u + uv$<br>or<br>$u \vee (u \wedge v)$ |
|-----|-----|------|---|
| T   | T   | T    | T                                       |
| T   | F   | F    | T                                       |
| F   | T   | F    | F                                       |
| F   | F   | F    | F                                       |

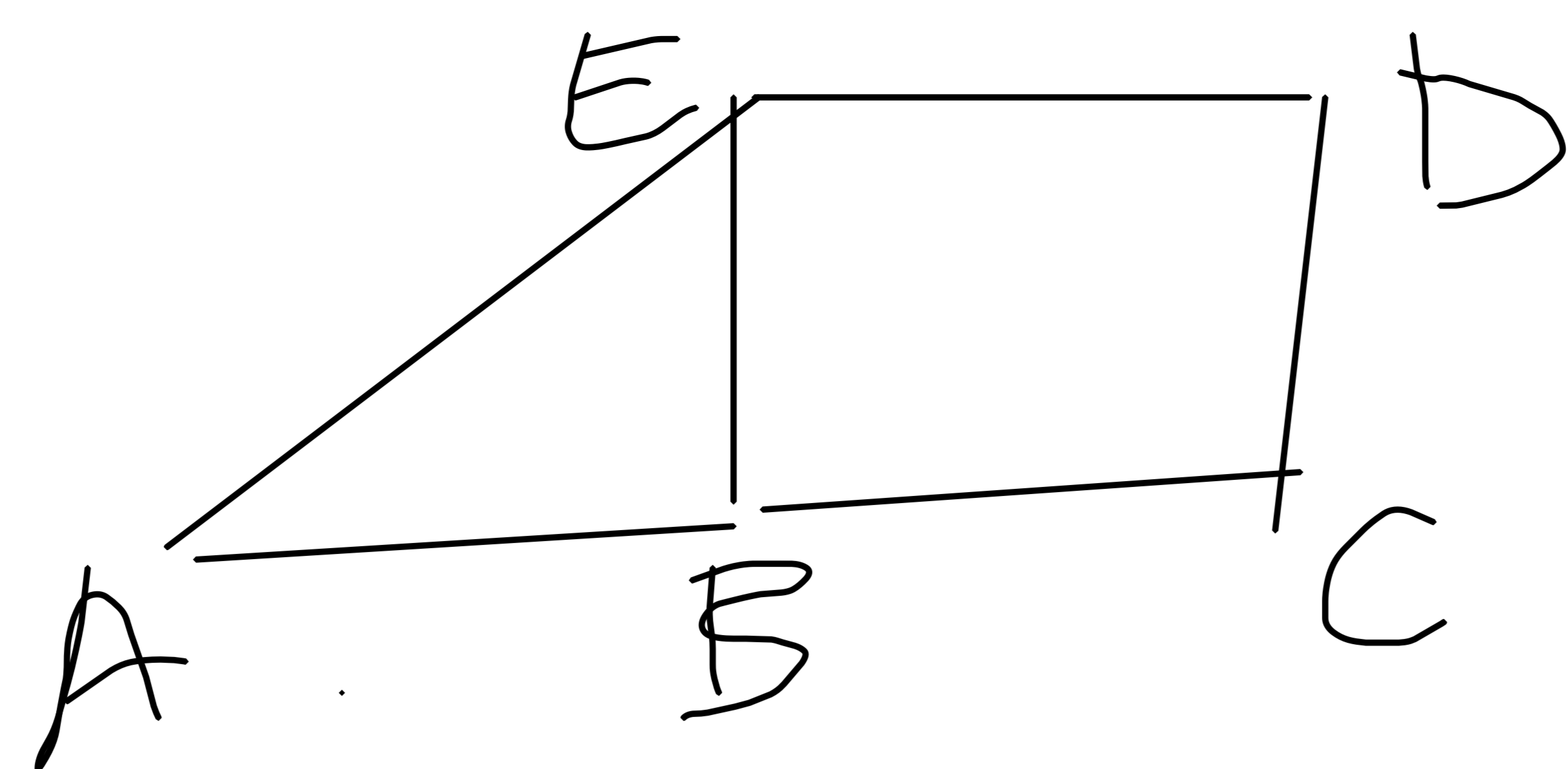
$$v \vee v = v$$

| $v$ | $v$ |
|-----|-----|
| T   | T   |
| F   | F   |

and

| $v \wedge v$ |
|--------------|
| T            |
| F            |





$$(A + BE)(B + ACE)(C + BD)(D + CE)(E + ABD) =$$

$$(AB + \cancel{AACE} + \cancel{BEB} + \cancel{BEACE})(\quad) = (AB + ACE + BE)(C + BD)(\quad) =$$

$$= (ABC + \cancel{ABBD} + \cancel{ACEC} + \cancel{ACEBD} + BEC + \cancel{BEDD})(\quad) =$$

$$= (ABC + ABD + ACE + BEC + BED)(D + CE)(\quad) =$$

$$= (\cancel{ABCD} + \cancel{ABCE} + \cancel{ABDD} + \cancel{ABDCE} + \cancel{ACED} + \cancel{ACECE} + \cancel{BECCE} + \cancel{BEDD} + \cancel{BEDCE})(\quad) =$$

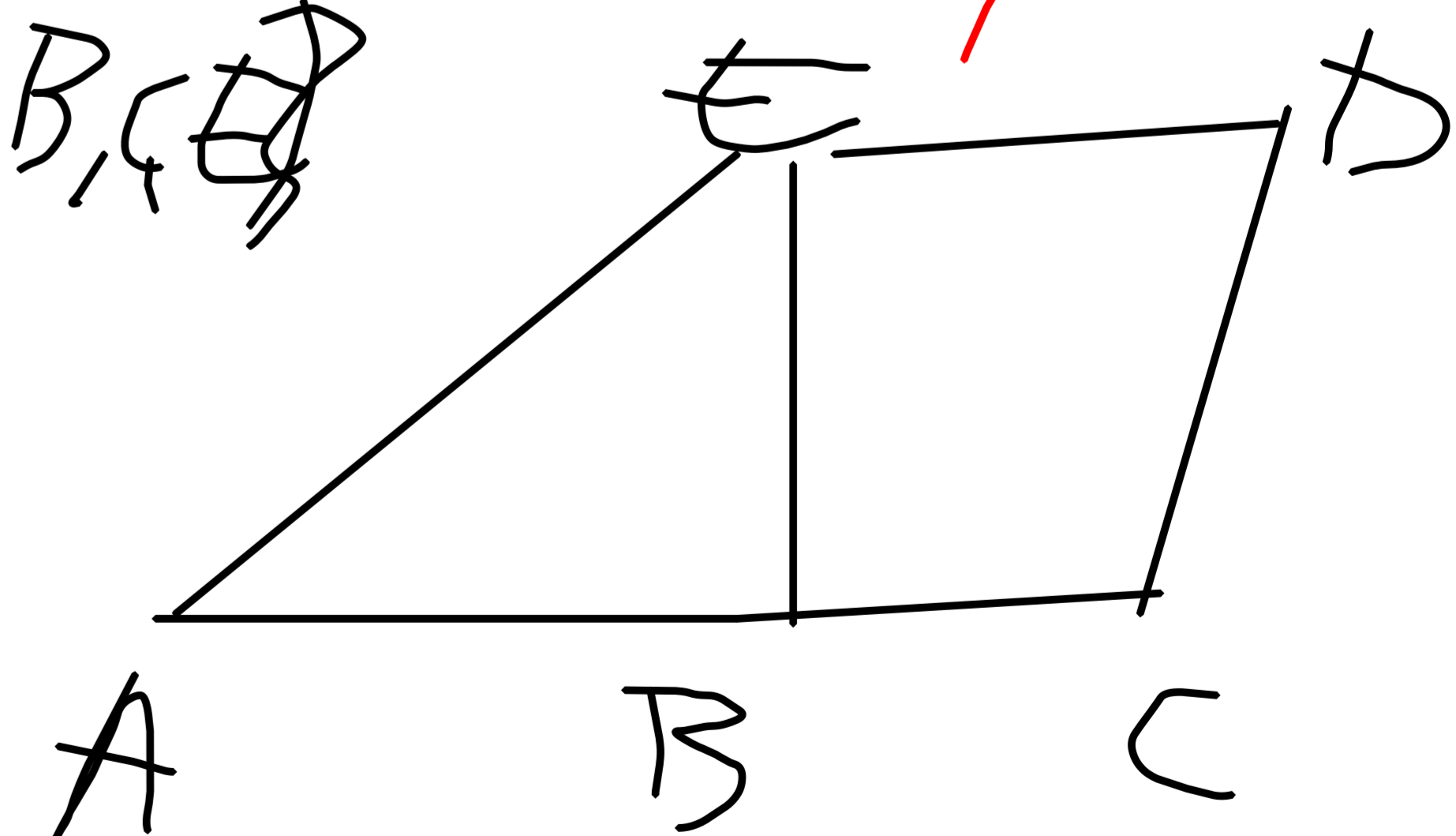
$$= (ABD + ACE + BEC + BED)(E + ABD) =$$

$$= \cancel{ABDE} + \cancel{ABDABD} + \cancel{ACEE} + \cancel{ACEABD} + BECE + \cancel{BECABD} + \cancel{BEDDE} + \cancel{BEDDABD} =$$

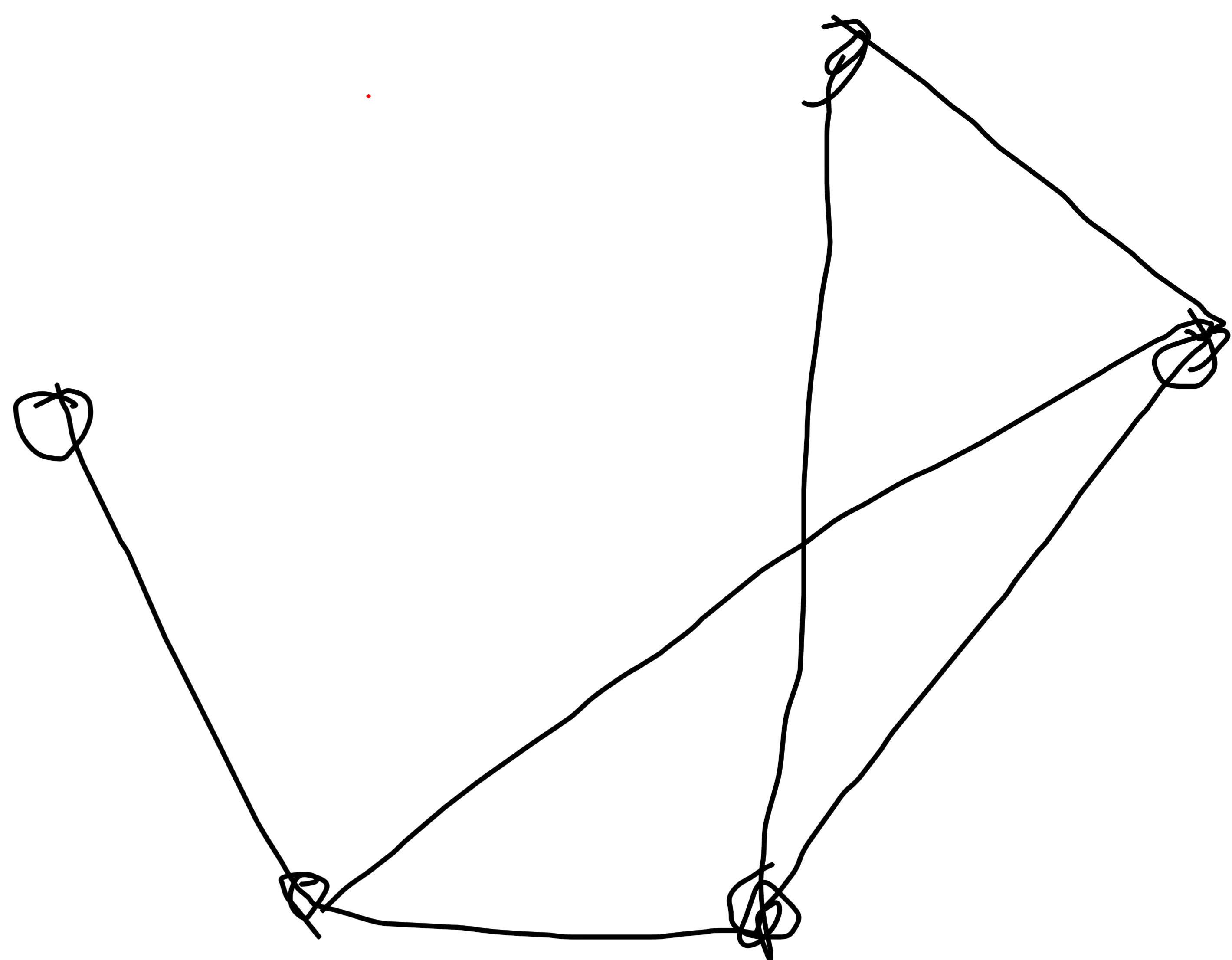
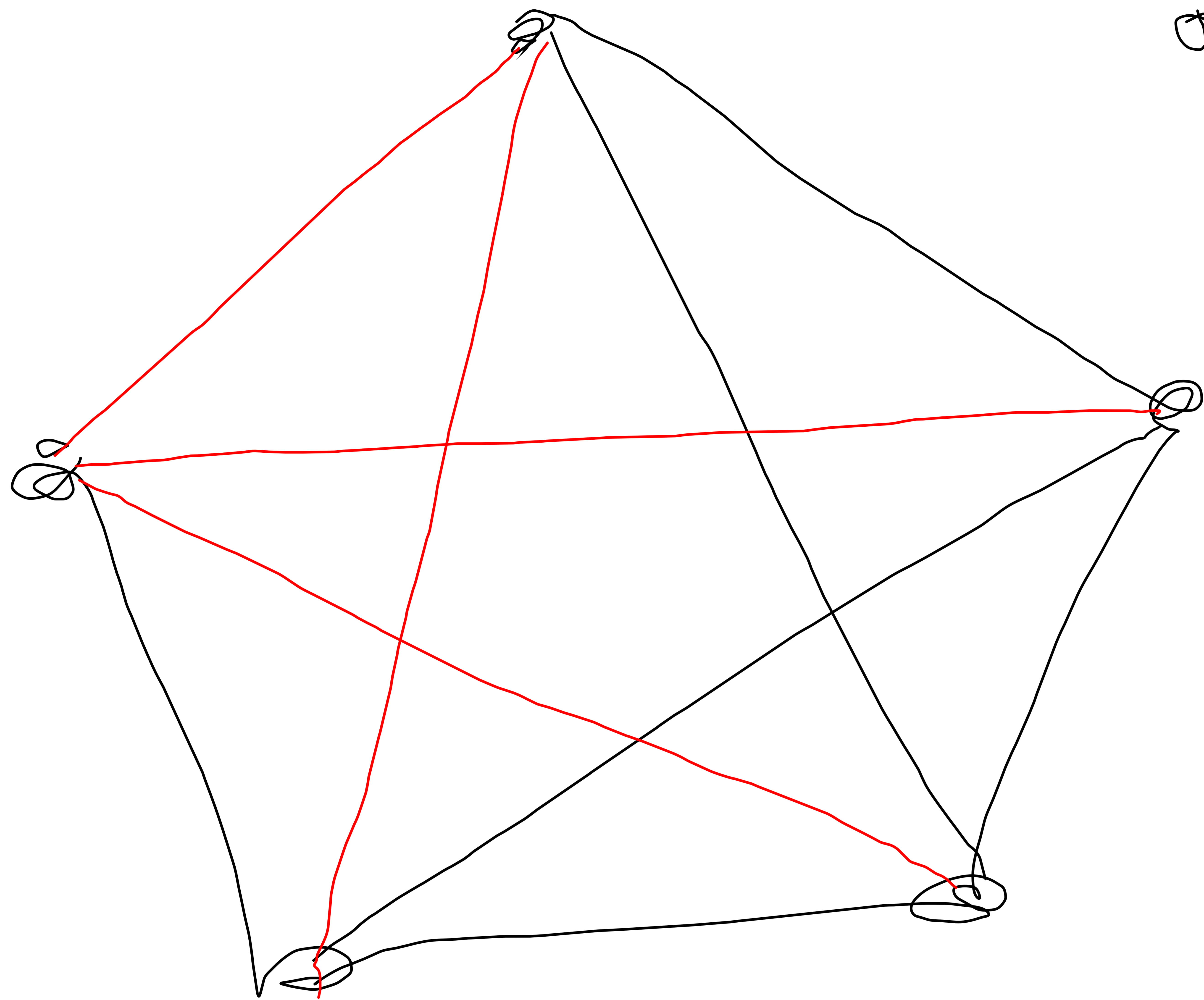
$$= ABD + ACE + BEC + BDE$$

Min cov's:  $\{A, B, D\}, \{A, C, E\}, \{B, C, E\}, \{B, E, D\}$

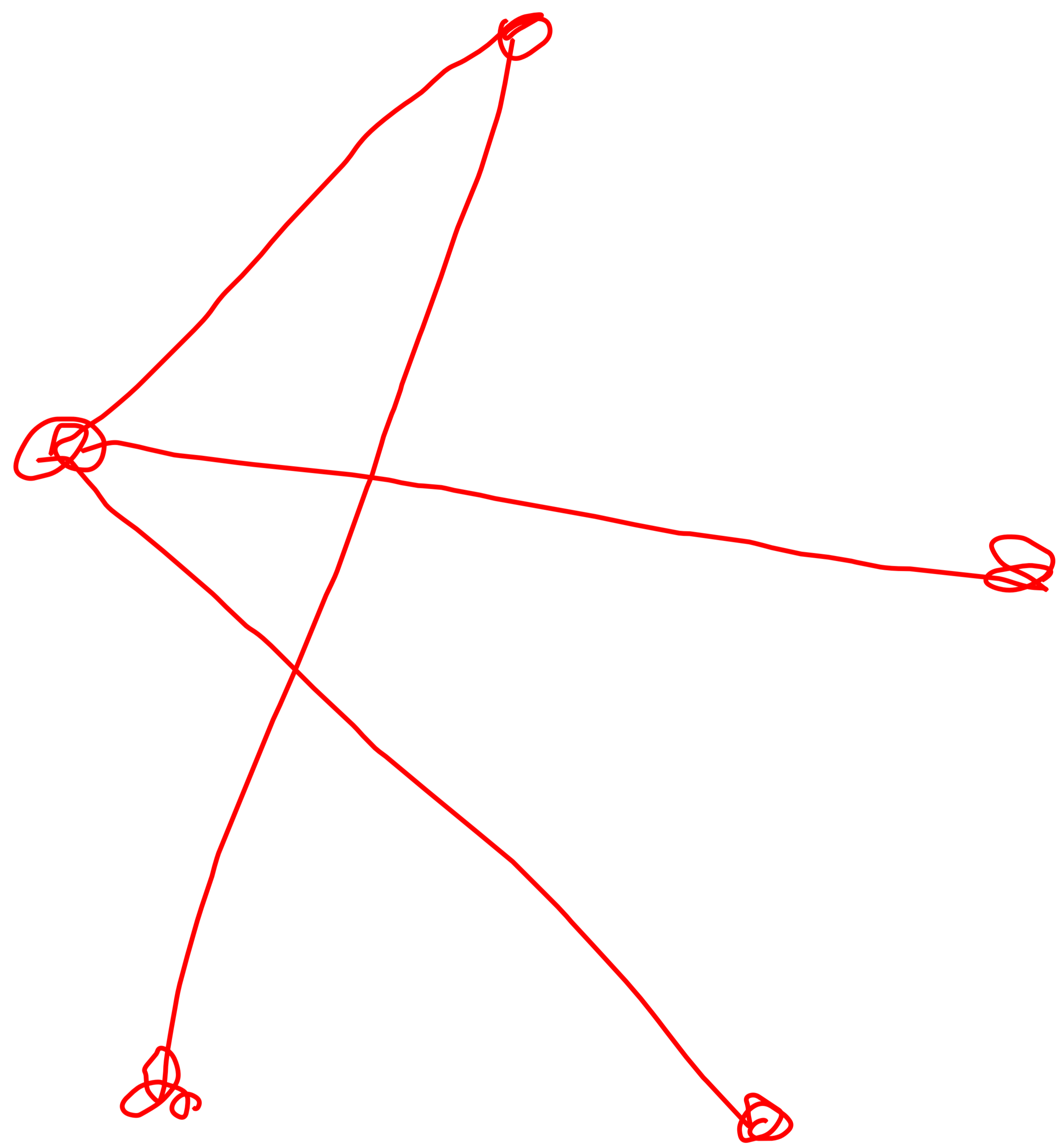
Max ind. sets:  $\{C, E\}, \{B, D\}, \{A, D\}, \{A, C\}$







④



⑤