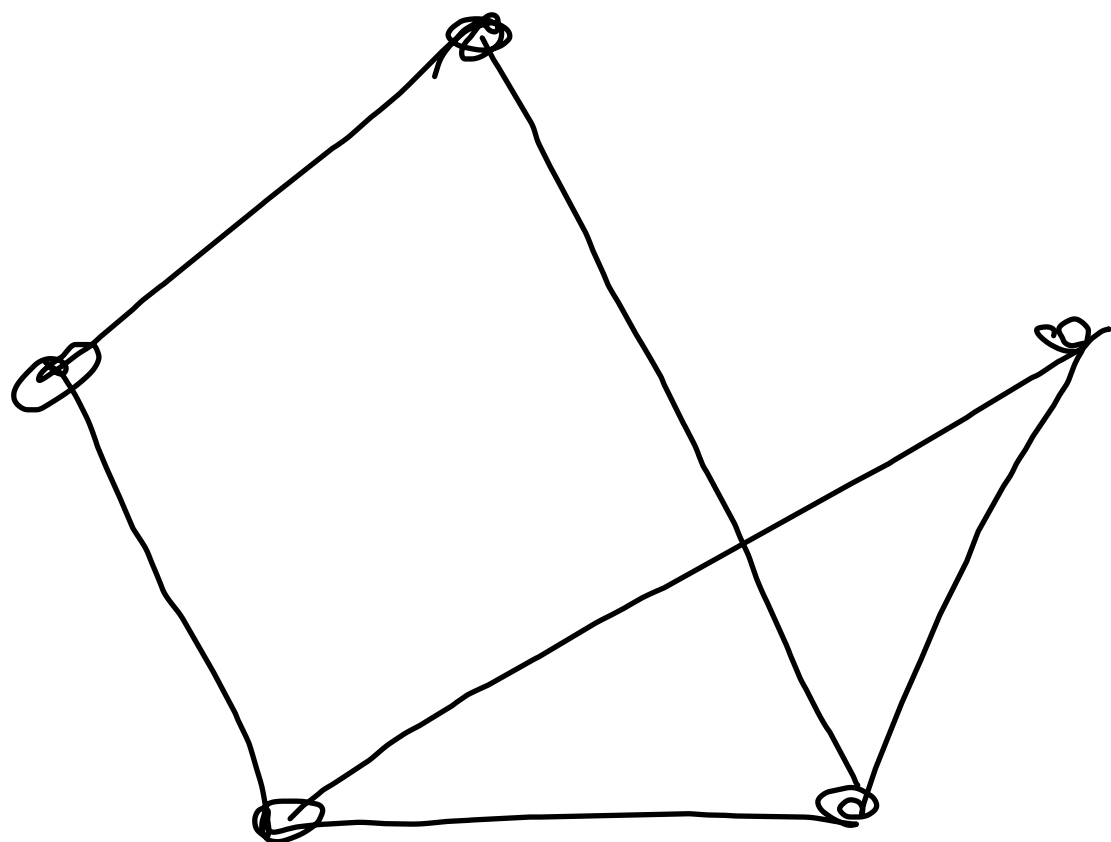
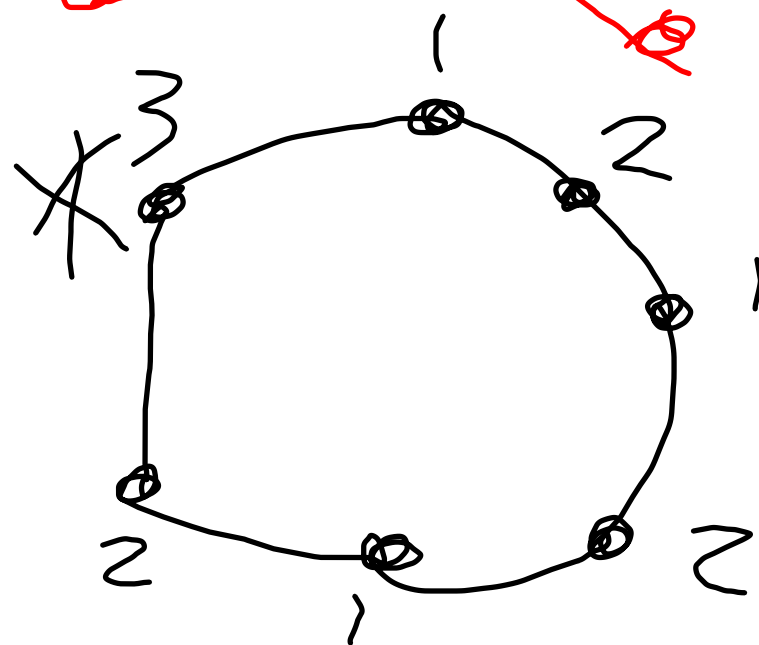
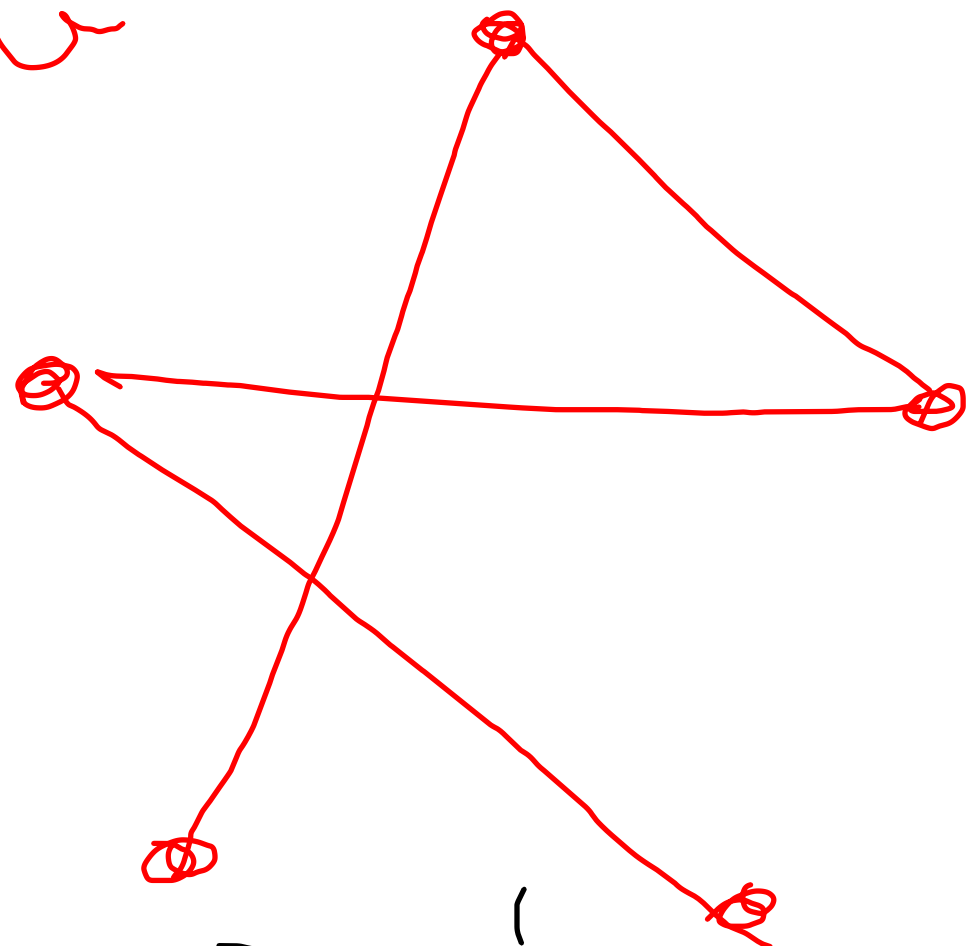


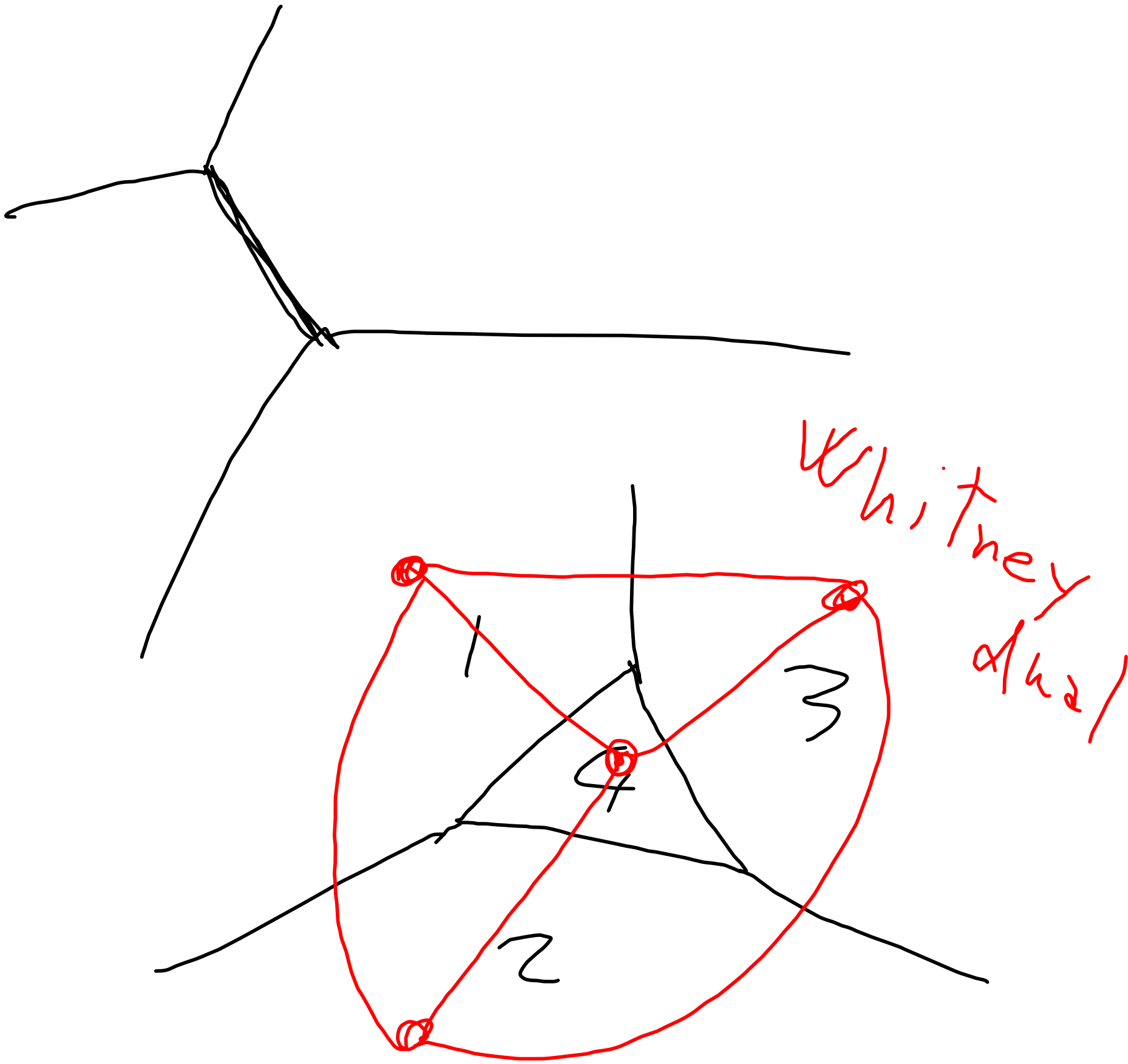
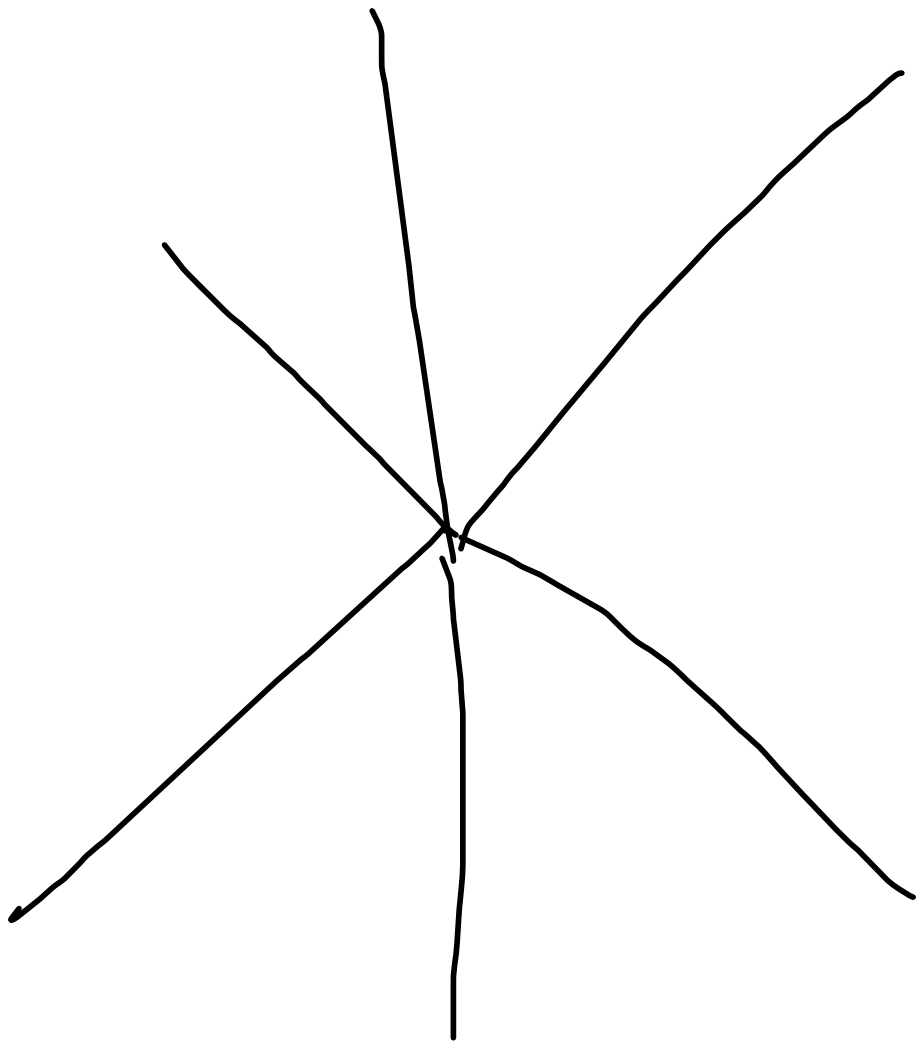
G



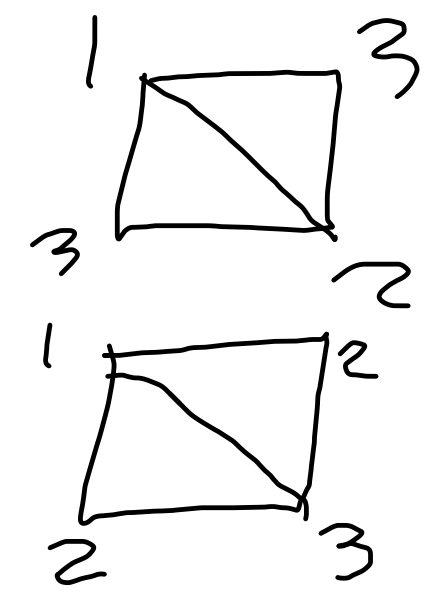
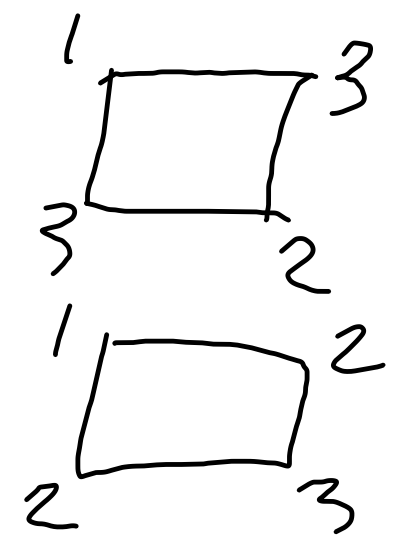
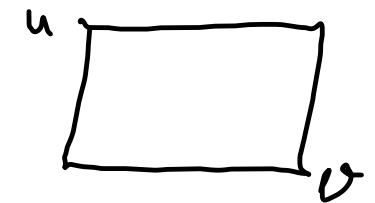
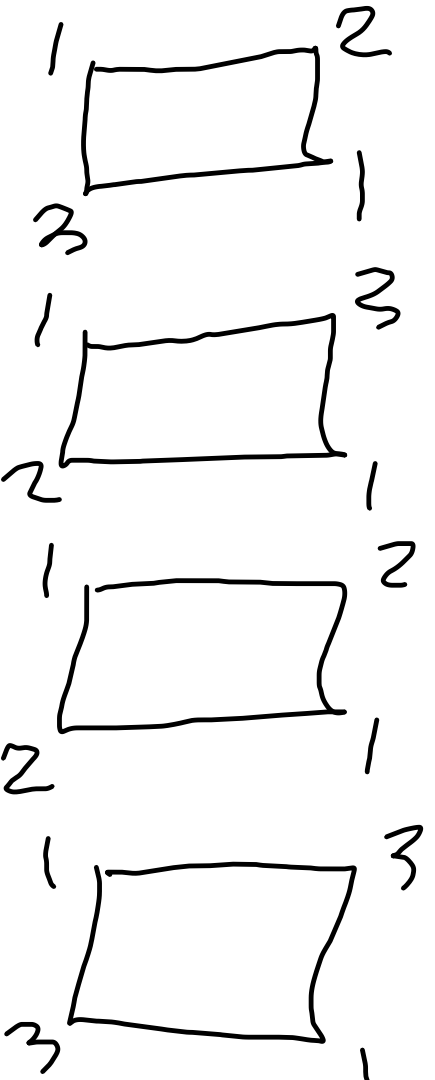
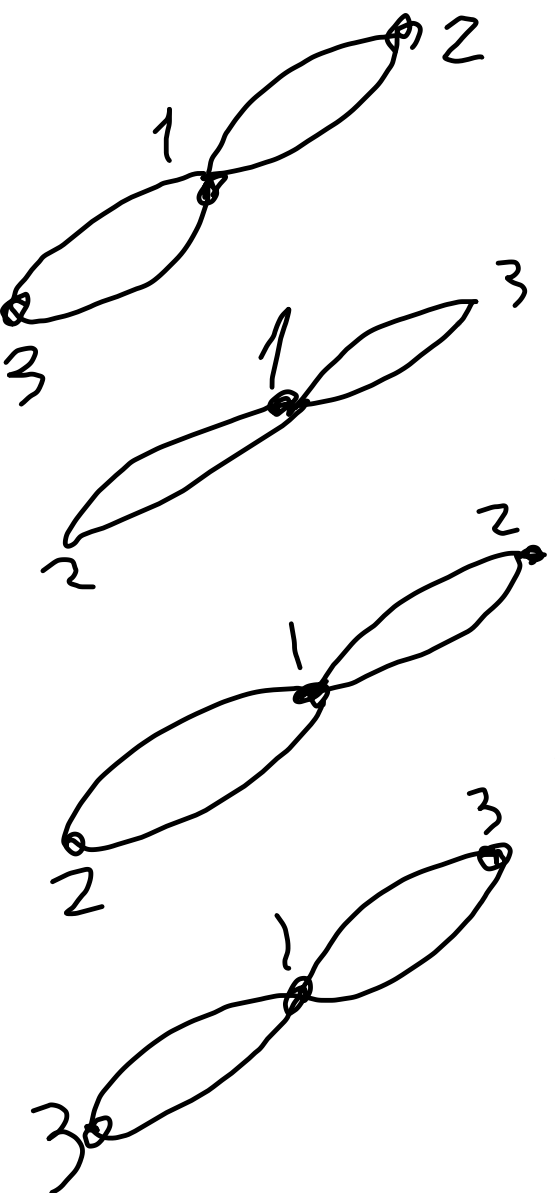
$$\Delta \geq k-1 \Leftrightarrow k \leq \Delta + 1$$

G'





$$\pi_k(G - e) = \pi_k(G) + \pi_k(G \cdot e)$$



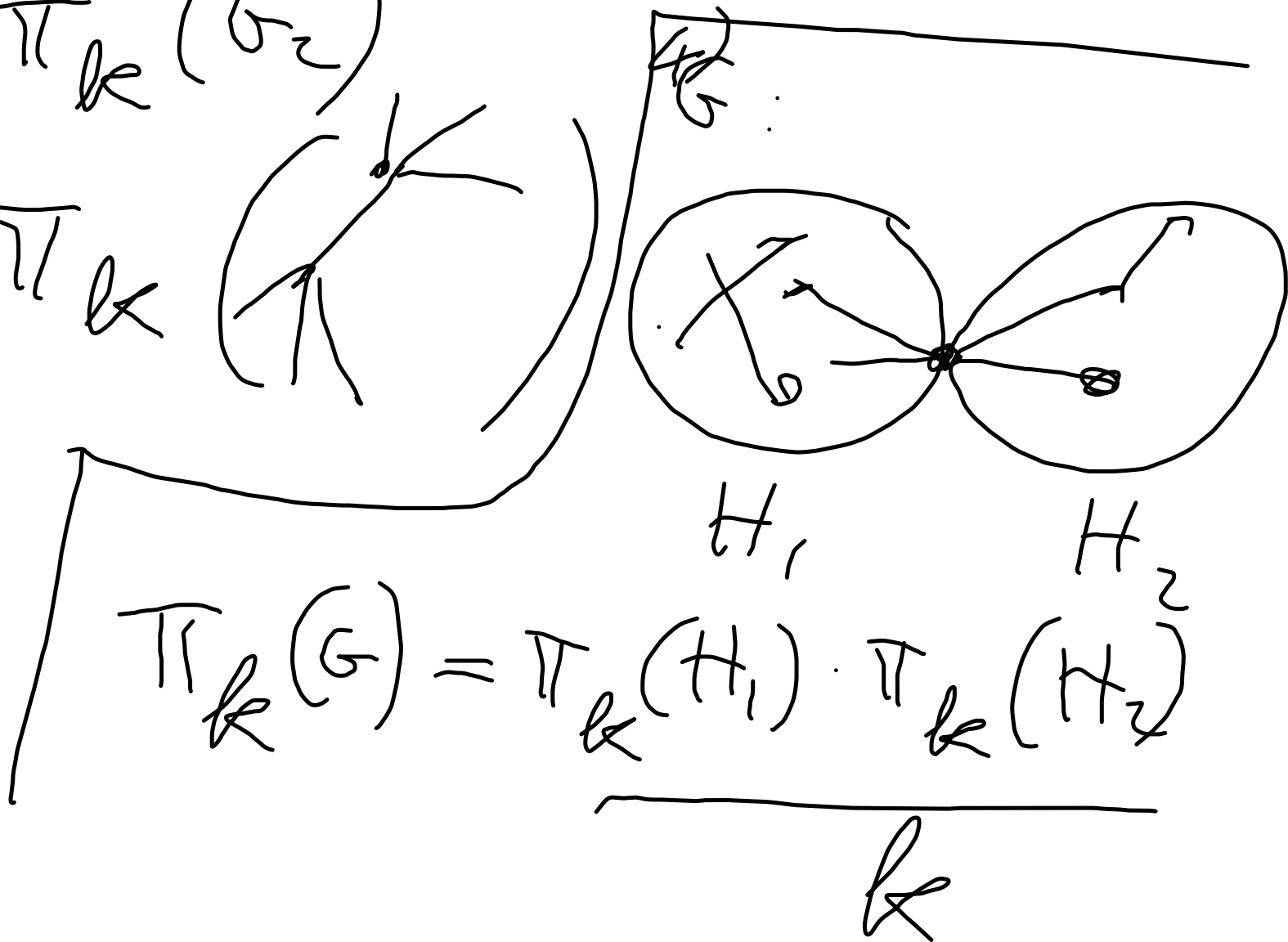
Shortcuts

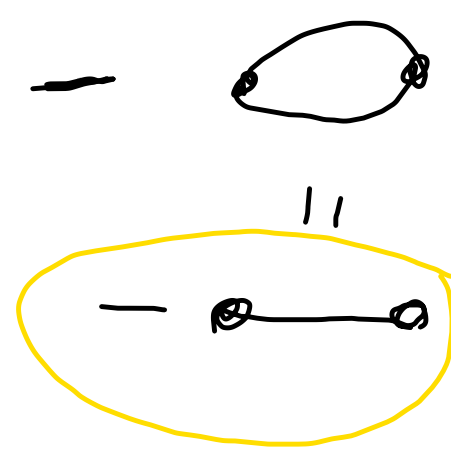
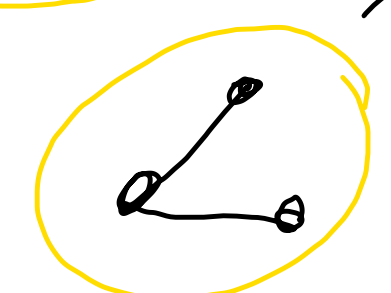
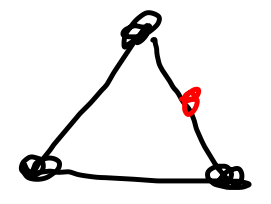
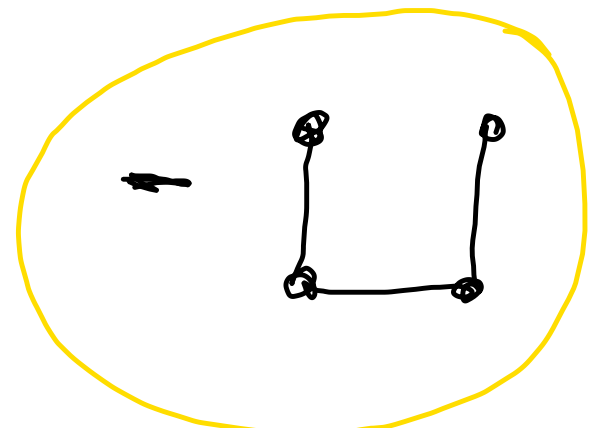
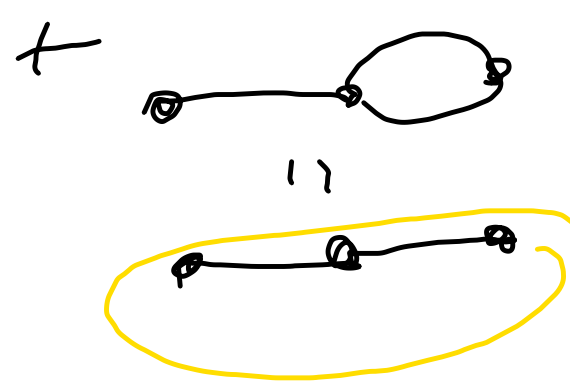
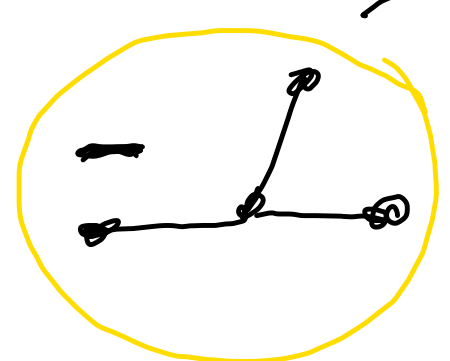
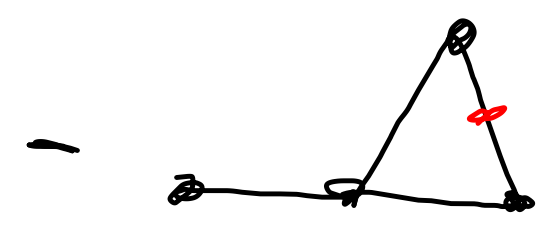
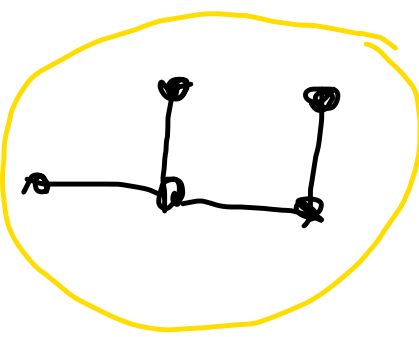
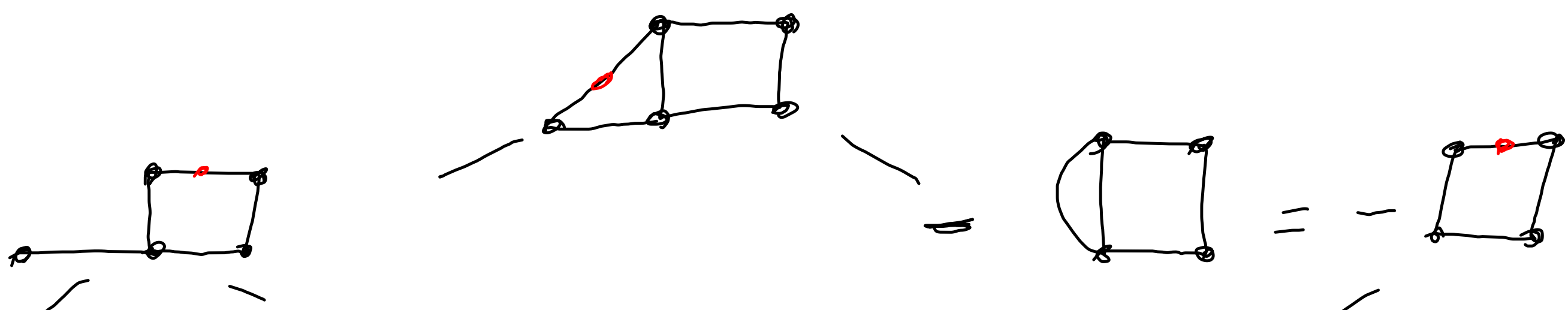
1) G has components G_1, G_2 , then

$$\pi_k(G) = \pi_k(G_1) \cdot \pi_k(G_2)$$

2) π_k (diagram of two overlapping circles) = π_k (diagram of two overlapping circles)

3) π_k (diagram of a single circle) = 0





$$k(k-1)^4 - 2k(k-1)^3 + 2k(k-1)^2 - k(k-1)$$

1 1
 1 2 1
 1 3 3 1
 1 4 6 4 1

$$\begin{aligned}
 &k^5 - 4k^4 + 6k^3 - 4k^2 + k + \\
 &- 2k^4 + 6k^3 - 6k^2 + 2k + \\
 &+ 2k^3 - 4k^2 + 2k + \\
 &- k^2 + k
 \end{aligned}$$

$$k^5 - 6k^4 + 14k^3 - 15k^2 + 6k$$

OK OK

OK OK

OK

OK