

DEF - Let  $X \neq \emptyset$  be a set. Let  $\mathcal{P}$  be a property which can hold or not hold for subsets of  $X$ .

$Y \subseteq X$  is said to be **maximal** for property  $\mathcal{P}$  if

- 1) property  $\mathcal{P}$  holds for  $Y$
- and 2) if  $Y \subsetneq Y' \subseteq X$  then property  $\mathcal{P}$  does NOT hold for  $Y'$

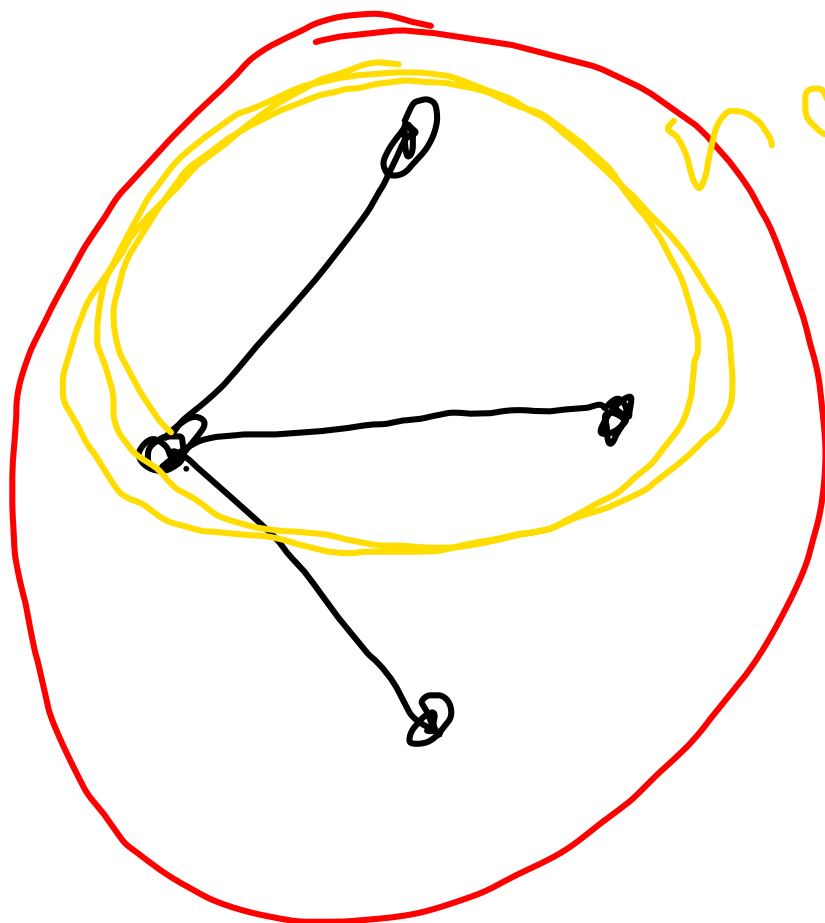
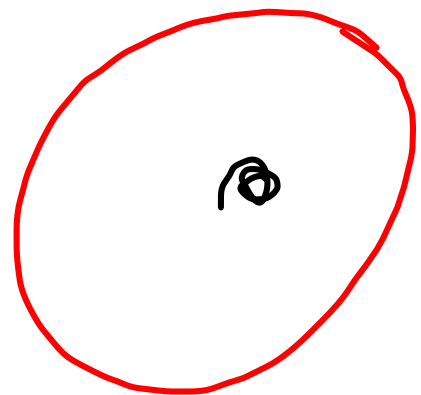
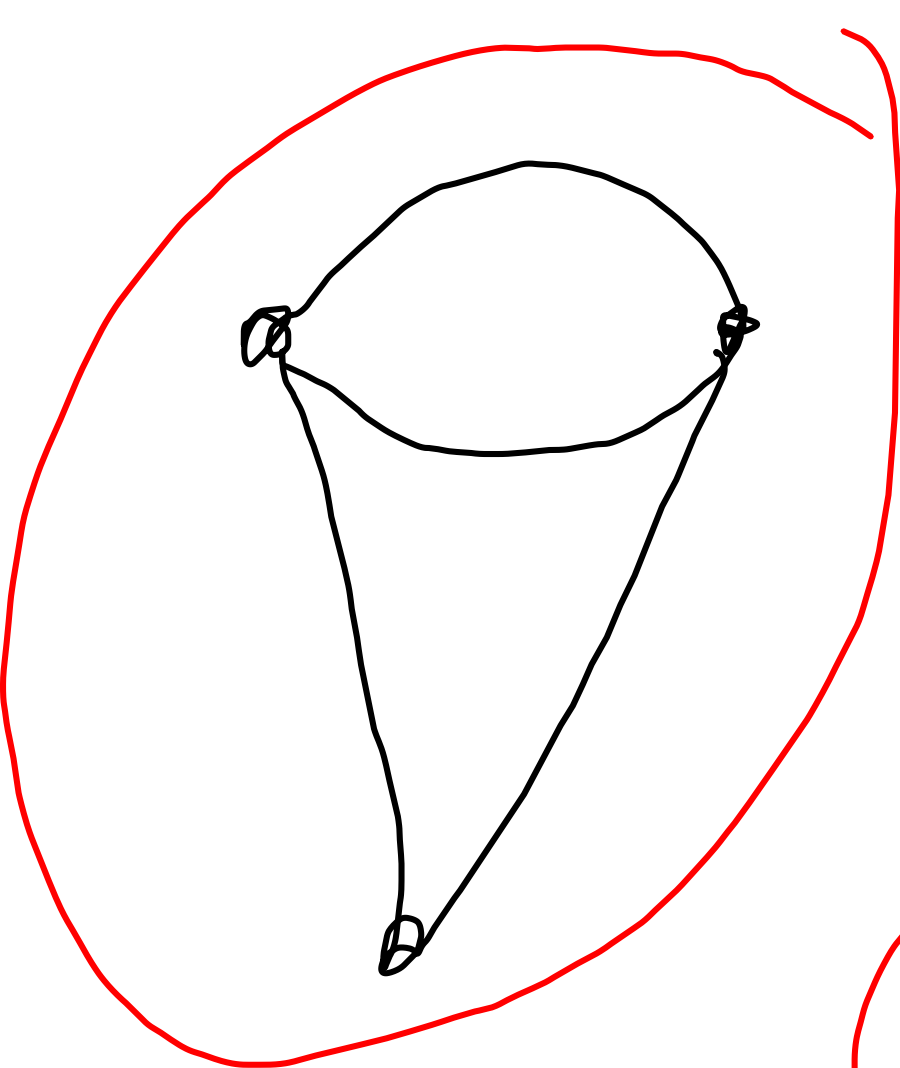
Alternative definitions of "connected graph"  
and of "component"

DEF - A graph  $G = (V, E, \mu)$  is said to be **connected** if  
 $\forall u, v \in V$  there exists at least one  $(u, v)$ -path.

DEF - Given a graph  $G$ , a subgraph  $H$  of  $G$   
is said to be a **component** of  $G$  if

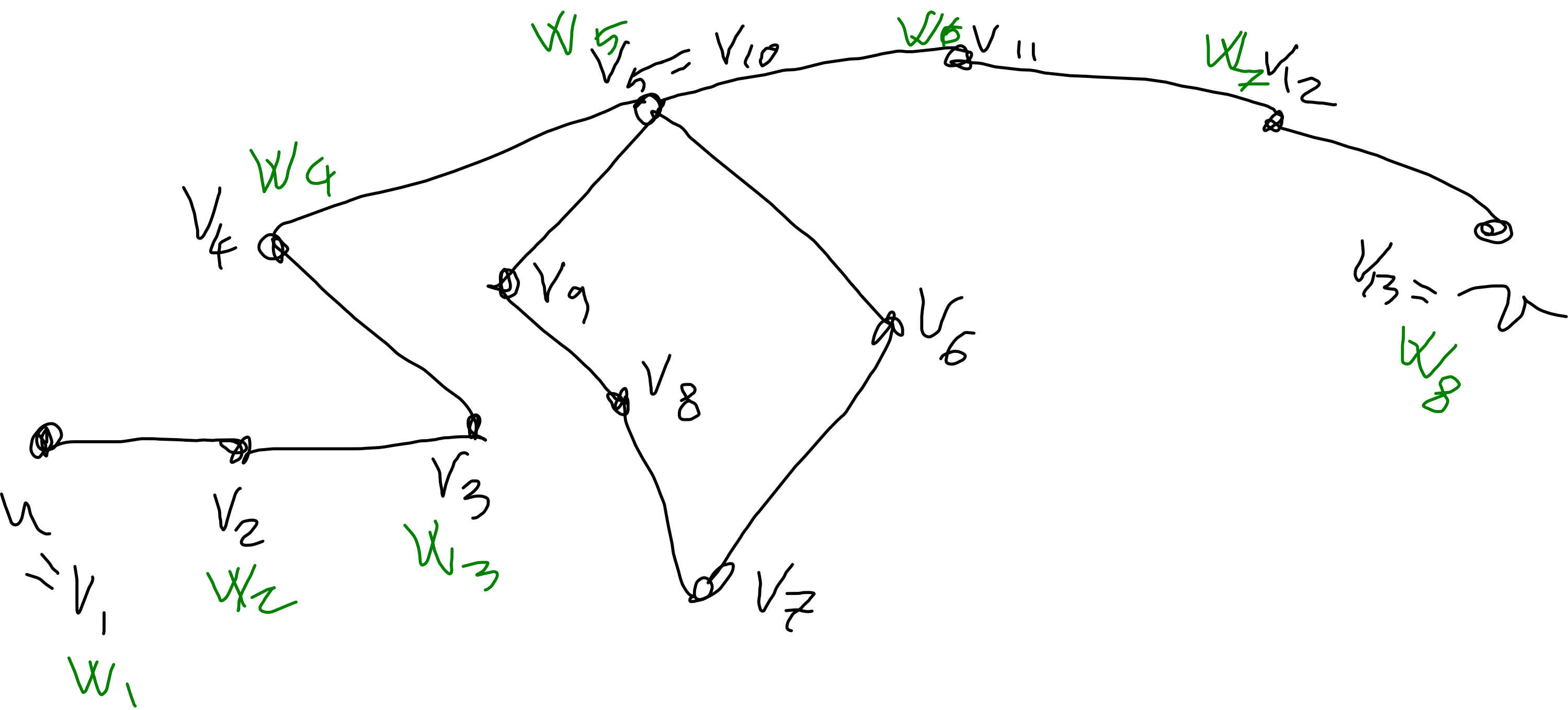
1)  $H$  is connected

and 2)  $H$  is maximal with respect to connectedness.



not a component

components



DEF - A **distance** in a set  $X \neq \emptyset$  is a function  $d: X \times X \rightarrow \mathbb{R}^{\geq 0}$  such that these three properties hold:

hold:  $d(a, b) \geq 0$  and  $d(a, b) = 0 \iff a = b$

1)  $\forall a, b \in X \quad d(a, b) = d(b, a)$

2) (triangular inequality)

3)  $\forall a, b, c \in X \quad d(a, c) \leq d(a, b) + d(b, c)$

NO

